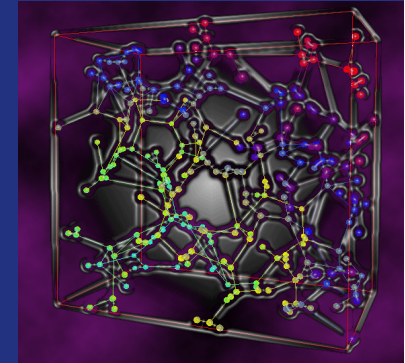


# MILIEUX CELLULAIRES OUVERTS : STRUCTURE ET PROPRIETES DE TRANSPORT



F. Topin

J.P. Bonnet

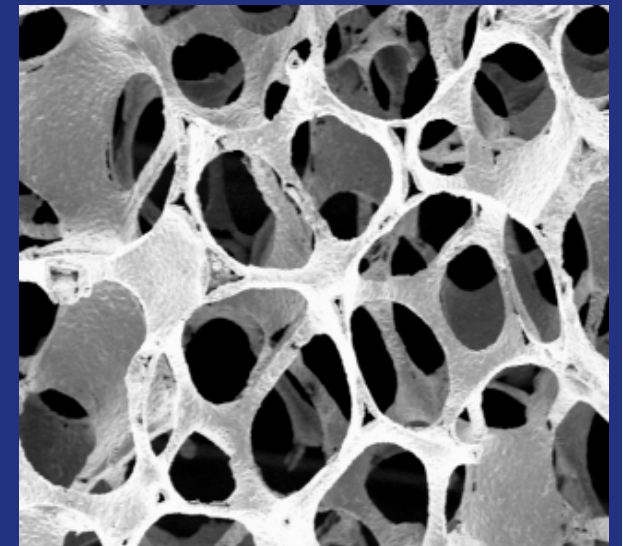
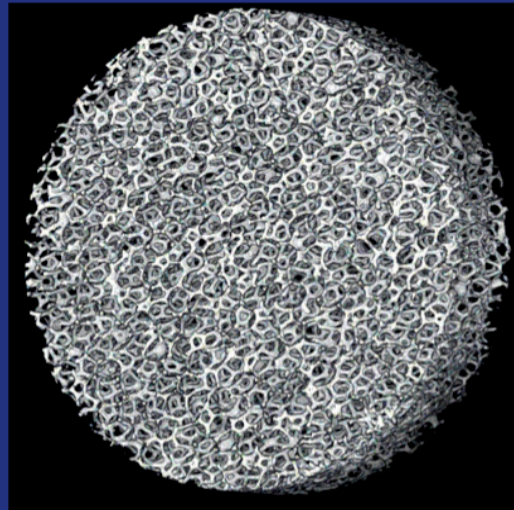
E. Brun

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# Contexte

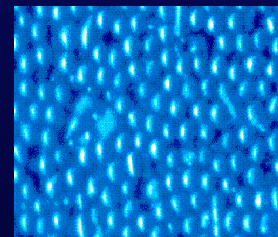
- Compréhension des transferts de chaleur et de masse dans les poreux
- Impact de la structure sur les propriétés thermophysiques et d'écoulement

## Expériences :

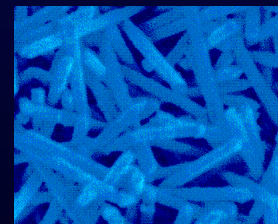
Configuration simplifiée  
Conditions contrôlées  
Structures modèles/Milieus réels

## Modèles :

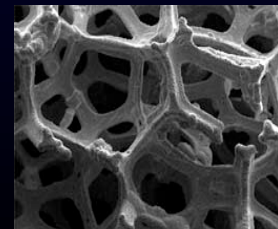
Physique à l'échelle du pore  
Couplages à l'échelle de l'échantillon



Lits de billes

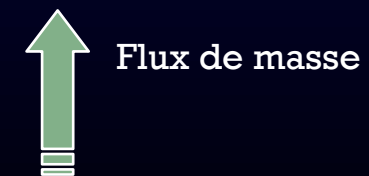
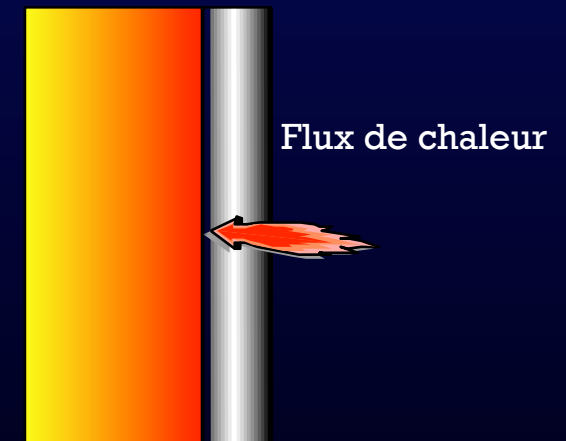


Fibreux



Mousses solides

Modèles physique

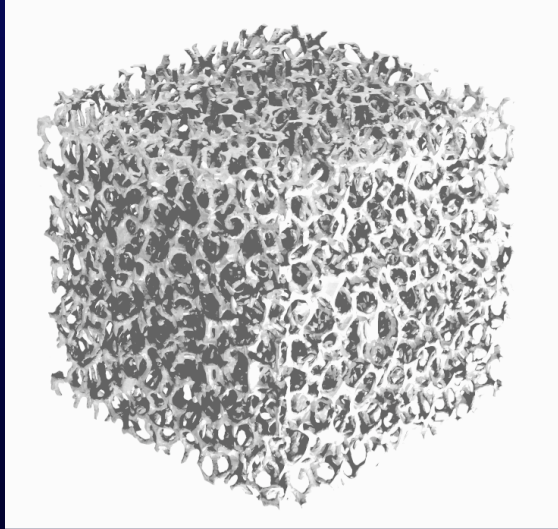


# Propriétés

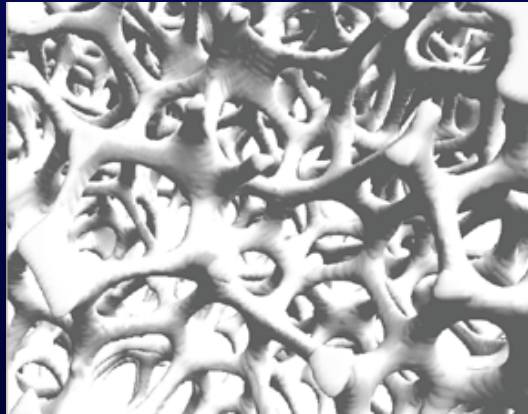
- ◉ Multiplicités des paramètres
- ◉ Géométriques
- ◉ Thermophysiques (conductivité, dispersion, coefficient d'échange)
- ◉ Lois d'écoulement (perméabilité, coefficient inertiel)
- ◉ Ecoulement polyphasiques (Modèles homogènes, à phases séparées)
- ◉ mouillabilité, pression capillaire ....
- ◉ Ebullition (courbe d'ébullition, CHF,....)
- ◉ Mécaniques
- ◉ Chimiques

# Quelques exemples de mousses

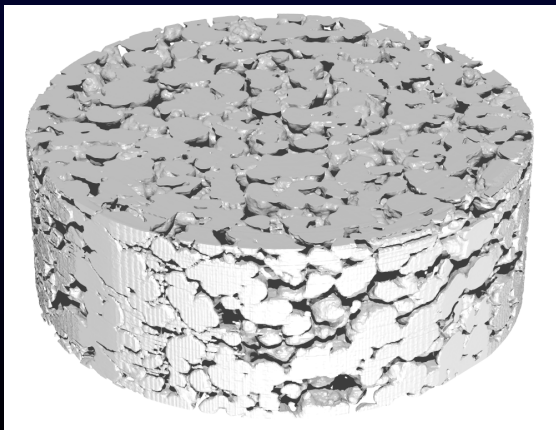
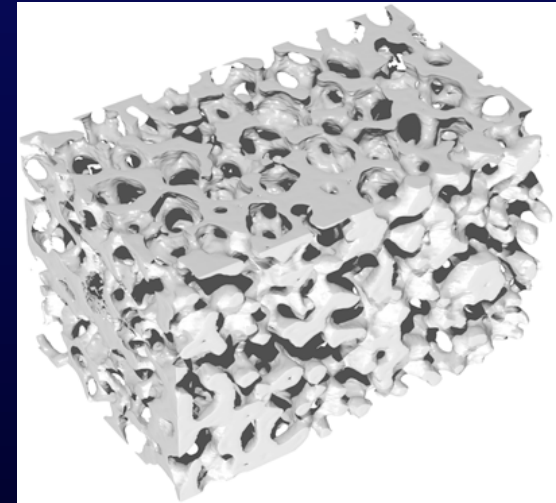
NiCr foams – Recemat  
(10,20,30,40,50,100 ppi)



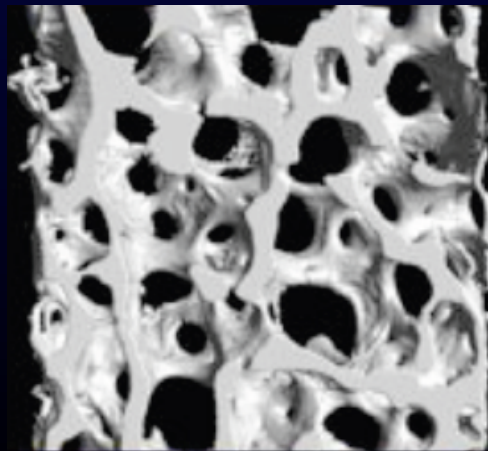
Al foams – ERG (5,10,20 ppi)



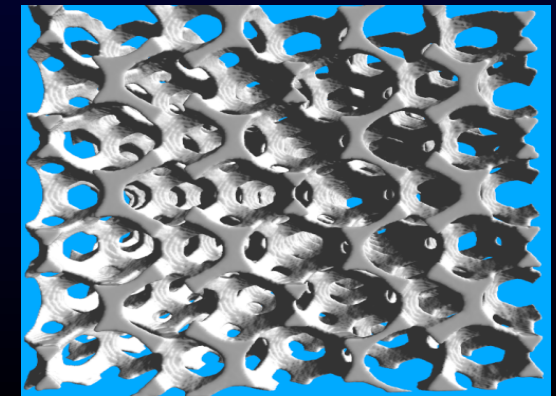
Ceramic foams



Sintered Polyethylene - Porvair

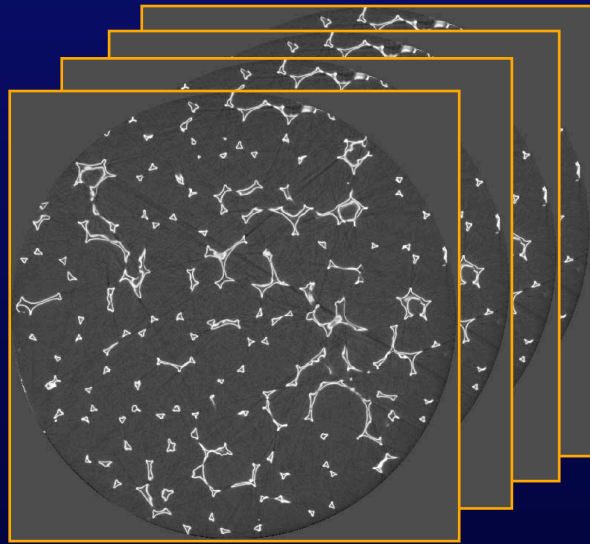


Trabecular bone



Kelvin cell -CTIF

# iMorph : Fonctionnalités



Segmentation des phases:  
solide/ fluide

Reconstruction 3D

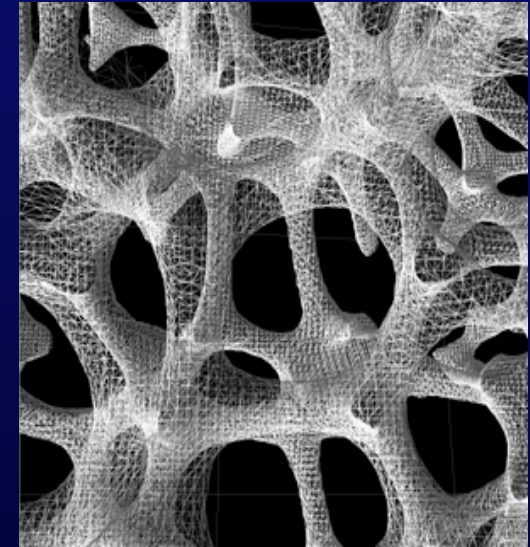
Tessellation de l'interface

Visualisation

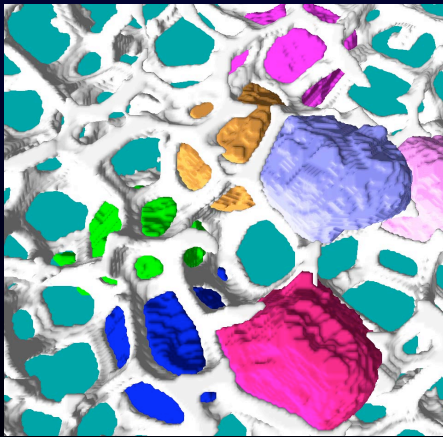
Porosité

Surface spécifique

Exportation vers les codes CFD

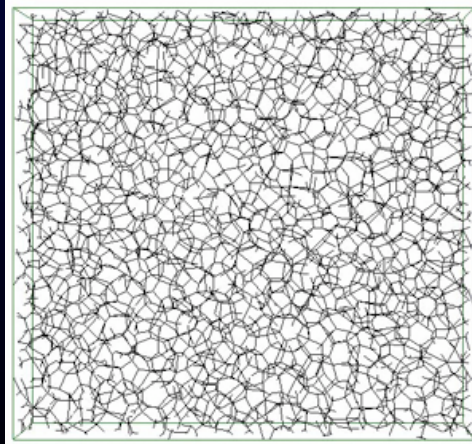


Extraction des éléments structurants  
Cellules



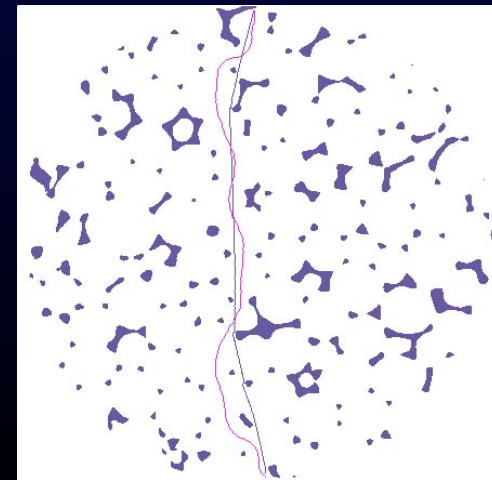
Porosimétrie  
Forme des pores  
Orientations

Réseau de brins



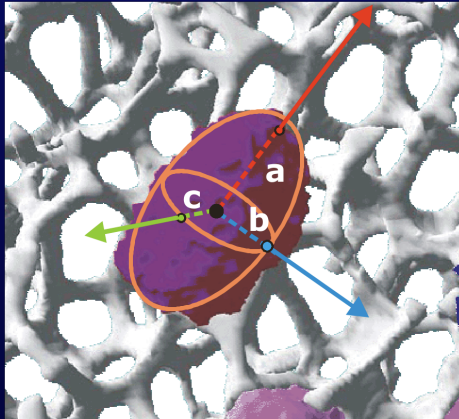
Orientations  
Connectivité  
Longueurs

Calculs Géodésiques



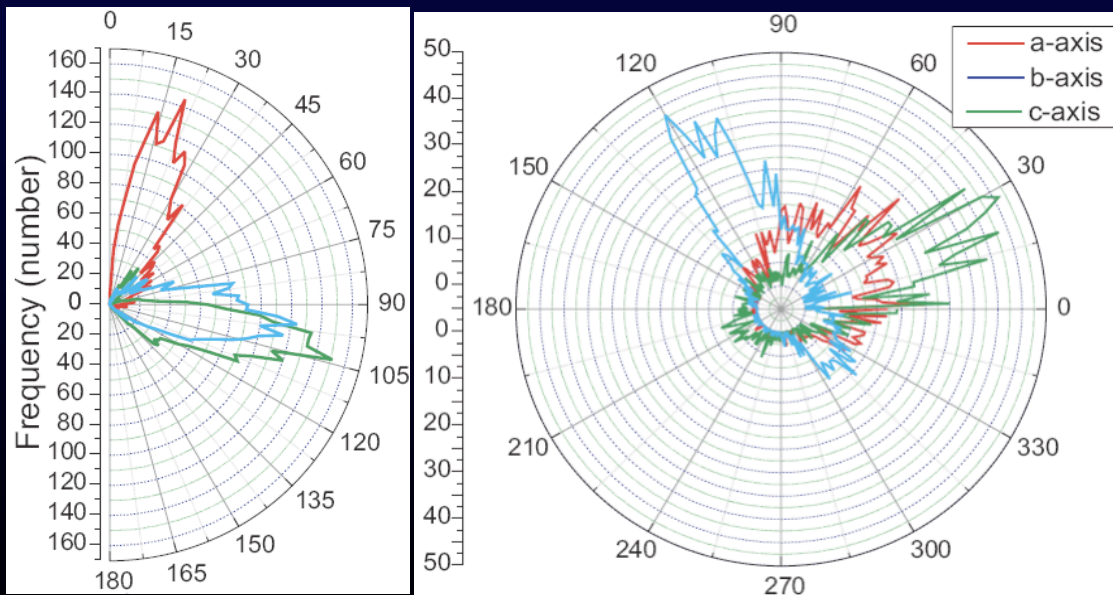
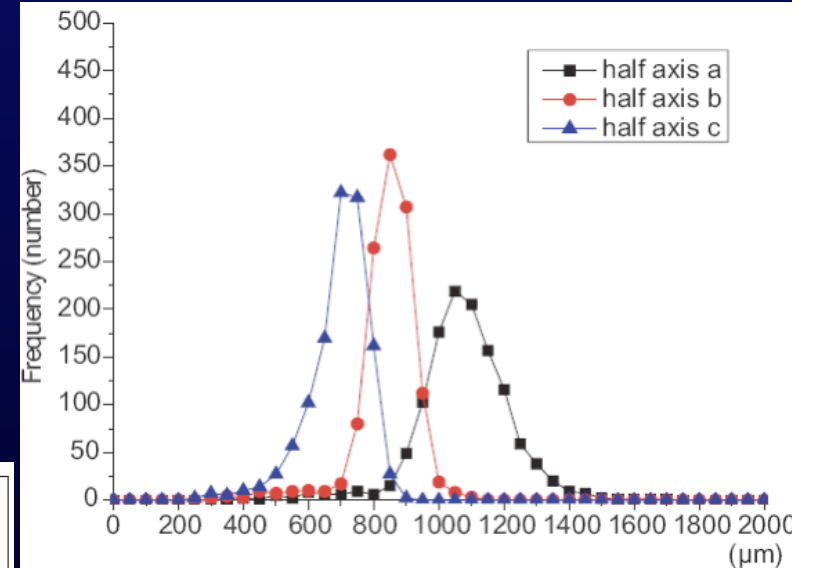
Plus courts chemins  
Tortuosité

# Forme et orientation des cellules



Mesure des ellipsoïdes équivalents (Matrice d'inertie du nuage de voxels)

Distribution des longueurs de demi-axes



Elevation

Azimuth

Cellules orientés de manière identique dans l'espace

Organisation → Anisotropie de l'espace poral

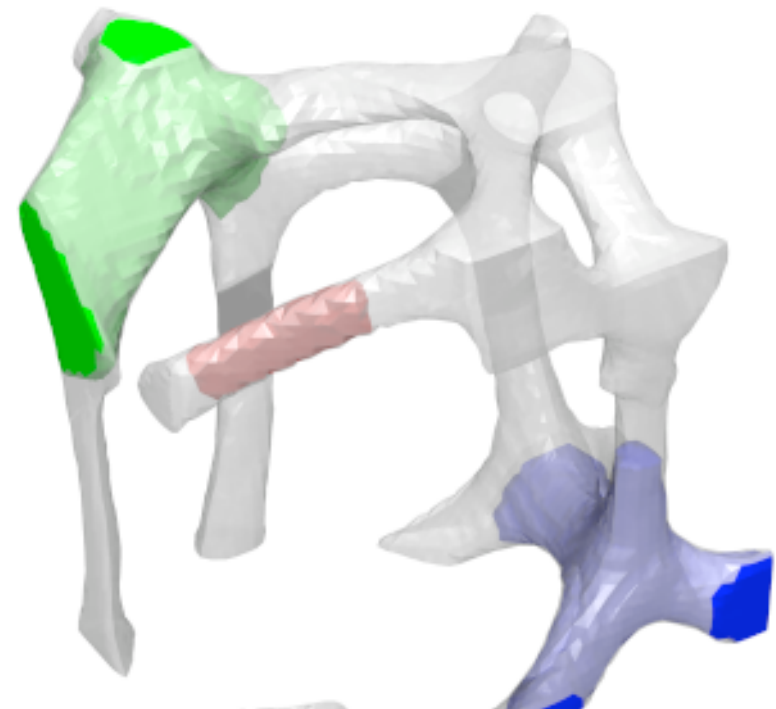
# Classification locale de formes

## Analyse classique

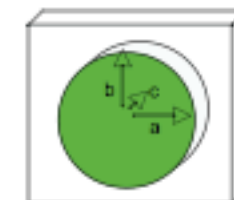
- Dans la littérature le point de départ est l'obtention de squelettes
- Squelette filaire pas toujours représentatif (pyramide, plaque)

## Identification des formes locales

- Identifier les voxels connexes à une certaine distance géodésique (Fast Marching)
- Matrice d'inertie du nuage de voxel obtenu
- Classification en objets élémentaires grâce aux moments d'inertie



Noeud  
 $a=b=c$



Plaque  
 $a=b \gg c$



Brin  
 $a \gg b=c$

# En Bref

- Cells present ellipsoid shape
- Cells organization induces anisotropy
- Geometrical tortuosity depends on orientation and organisation
- Foams are homothetic

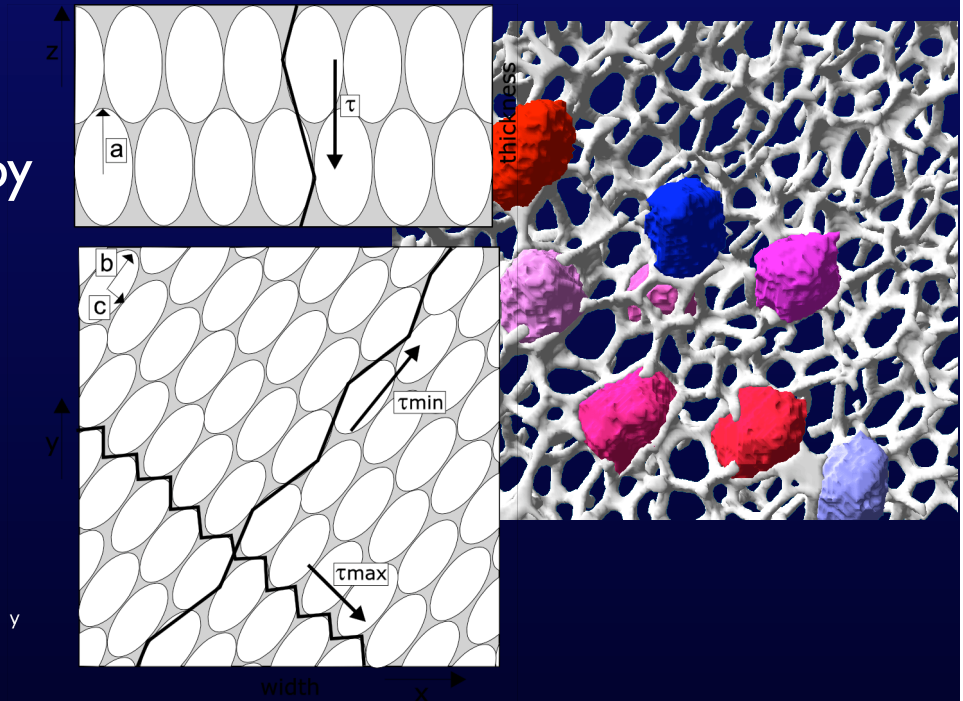


TABLE 1. Presentation of geometrical parameters

Samples	$\epsilon$	Sp.Surface ( $\text{m}^2/\text{m}^3$ )	$d_s$ (mm)	$d_l$ (mm)	$d_p^*$ (mm)
1	0.825	370.9	1.9	3.6	8.7
2	0.84	357.4	1.9	3.6	8.7
3	0.845	263.9	2.5	5.0	12.4
4	0.85	252.2	2.5	5.0	12.7

$d_p^*$ - calculated for equivalent included spherical diameter

## Structural dependencies

$$Sp = 3/d_{\text{Pore}}$$

$$d_{\text{Throat}} = 0.52 d_{\text{Pore}}$$

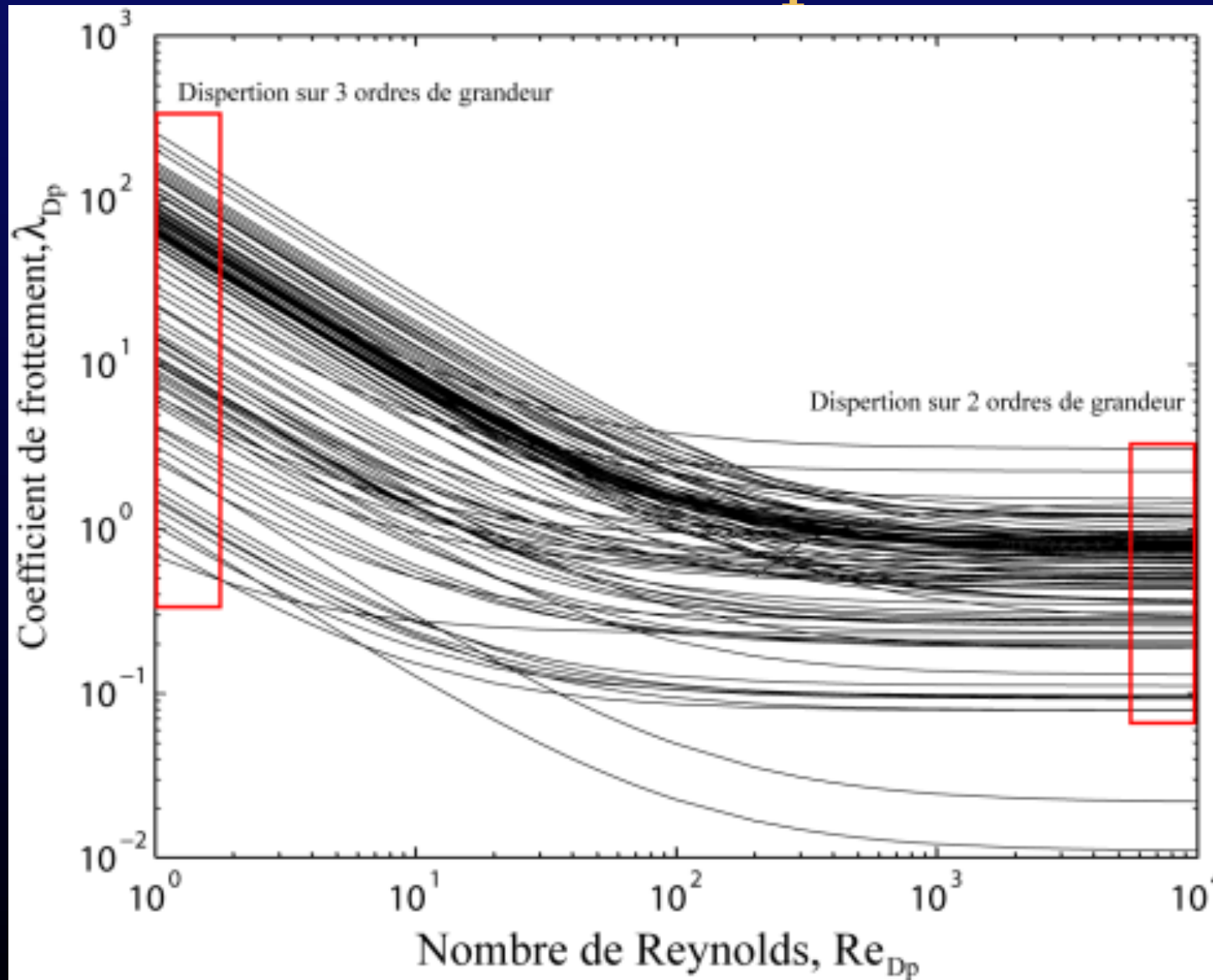
$$\text{Strut length} = 0.4 d_{\text{Pore}}$$



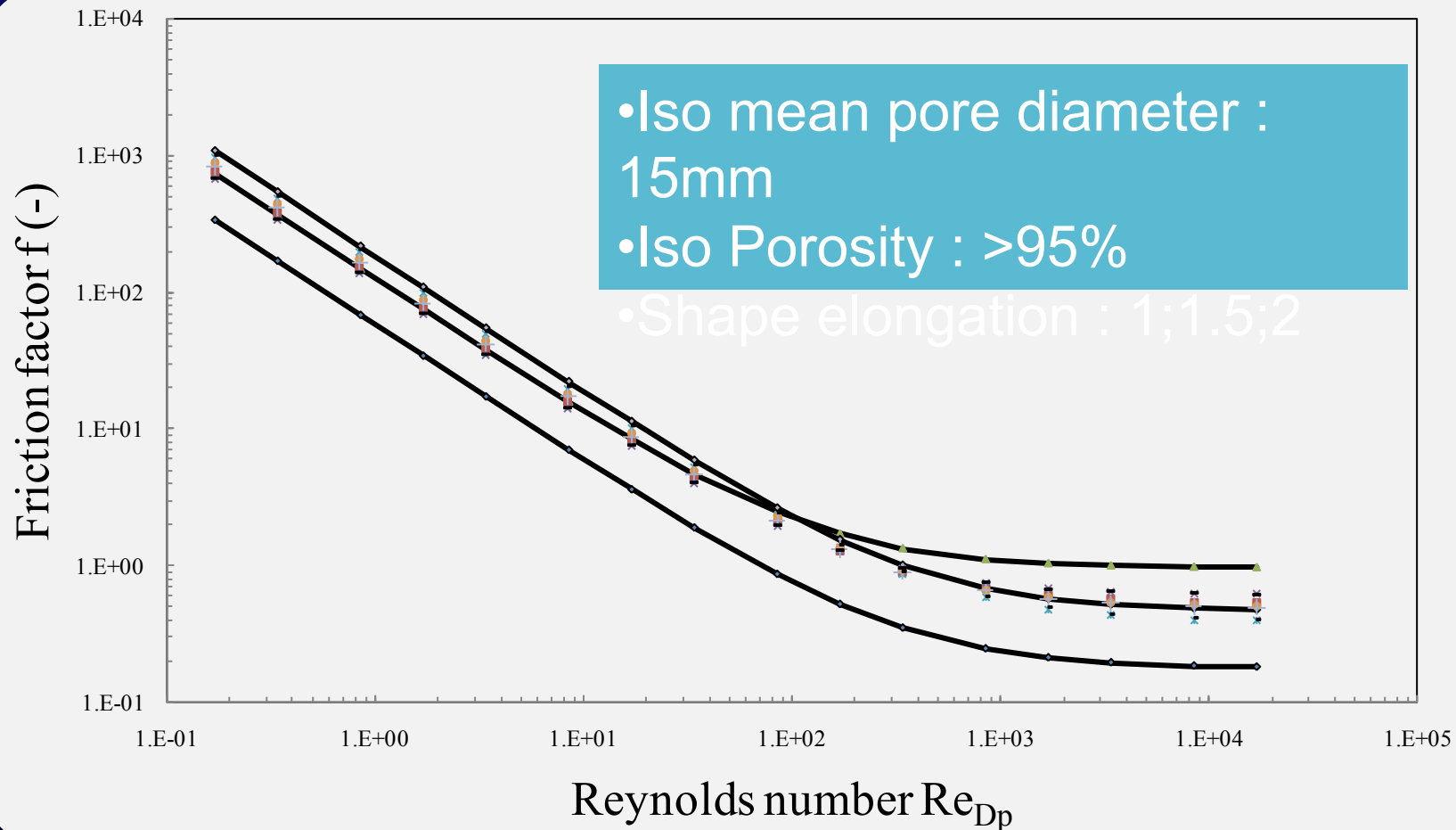
## What is known ?

- Effective conductivity  $l$  depends on porosity  $e$  and on tortuosity  $t$
- $l$  independent from  $D_p$ 
  - Pore shape depend on pore size
- Permeability  $K$  and Inertia coefficient  $b$  depend on  $D_p$  :  
 $K \sim D_p^2$  &  $b \sim D_p^{-1}$
- And other parameters ...

# Problématique écoulement



Dispersion des résultats

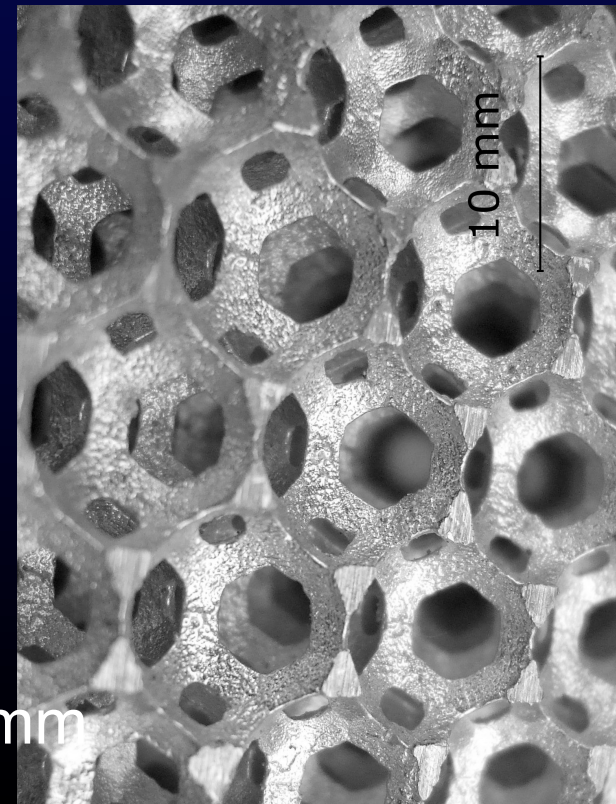


• Ergun like approach not adapted to describe flow law in foam

- Develop a model more accurate for foam
- Study influence of pore shape on properties

# Kelvin's cell

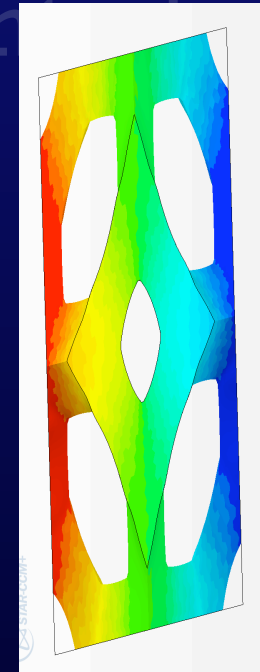
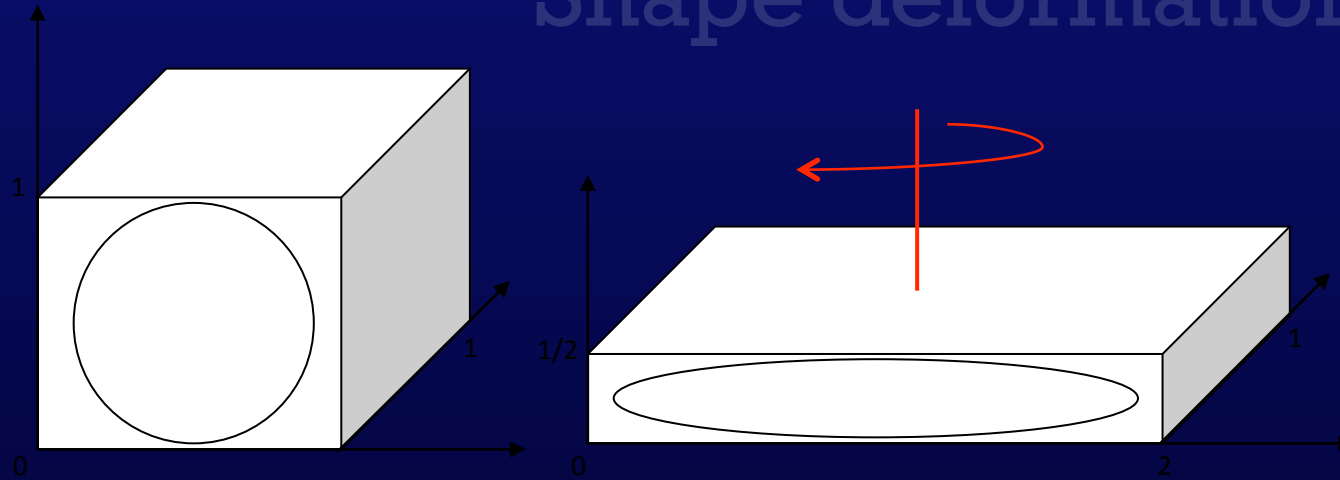
- Tetrakaleidon (14 faces)
- One of models that well describe metal foams
- Widely used
- Casted samples are available and characterized
- Periodic structure
- Isotropic material
- Both CAD and Tomography available



$e=87\%$   
 $D_p=14.2\text{mm}$

...

# Shape deformation control

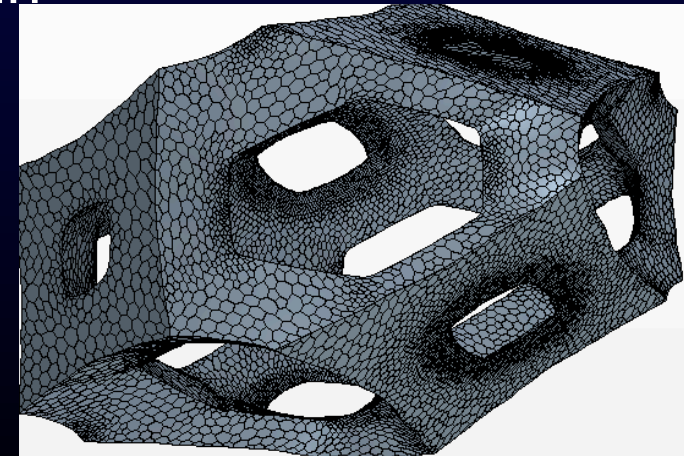


Stretching and shearing

Scaling factor  $a$  in  $x$  direction ;  $1/\sqrt{a}$  in  $Y$  and  $Z$  direction

Rotation around  $Z$  axis

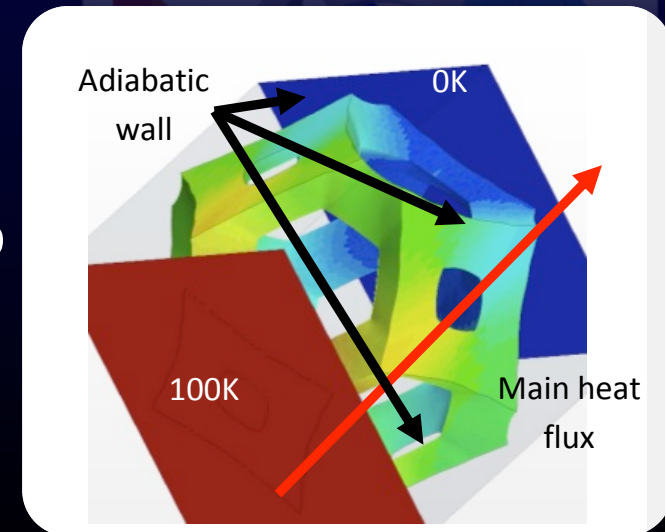
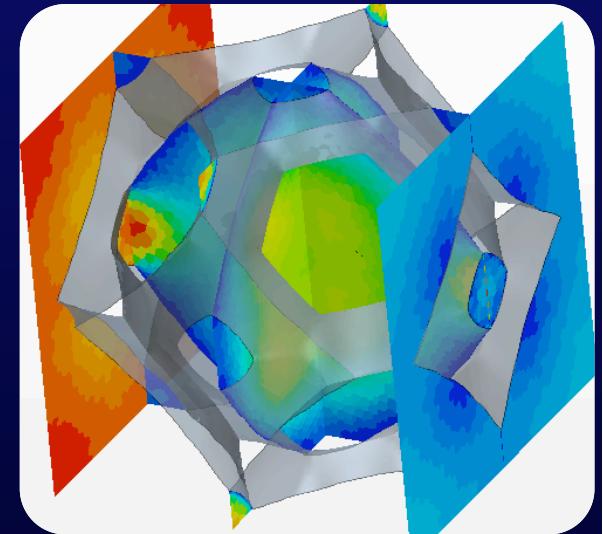
$0.4 < a < 4.0$  and  $0 < q < 45^\circ$   
20x45 Virtual samples produced



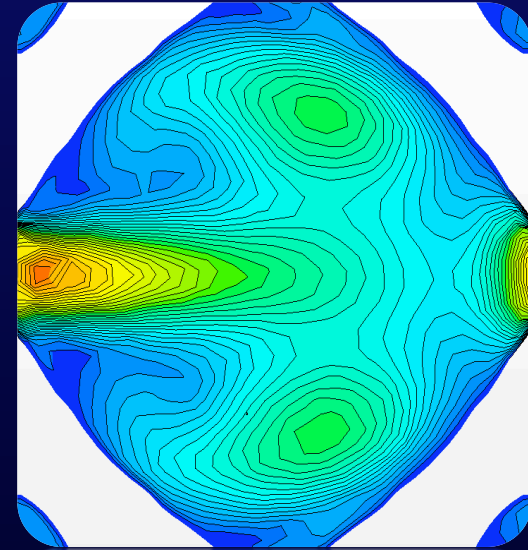
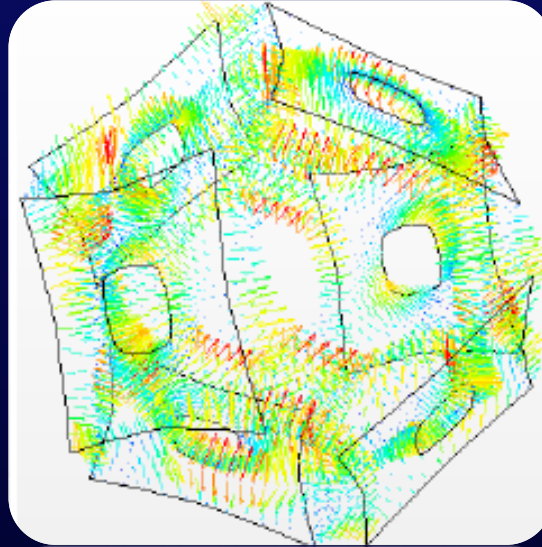
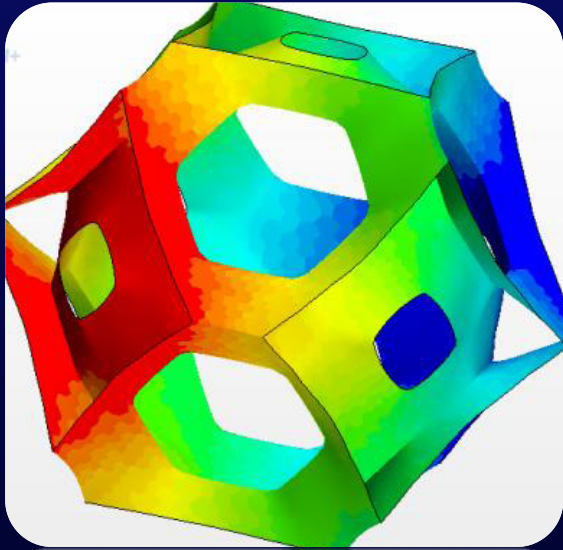
Porosity, pore equivalent volume sphere diameter are conserved

# Pore scale numerical simulation

- Mesh size : Polyhedral cell core + prism layers near the solid matrix surface
  - About 400.000 cells
- Fluid phase conductivity is equal to  $10\text{W/mK}$  ,  $100\text{W/mK}$  for solid phase
- Navier-Stokes and energy balance equations are solved in steady condition
  
- Boundary conditions :
  - permeameter conditions (flux in one direction, no flux on other face):
    - Temperature difference imposed on two opposite faces, adiabatic on other face
    - Pressure difference imposed on two opposite faces, slip condition on other faces



# Volume averaging technique



$$\vec{\varphi} = \overline{K_{eff}} \cdot \nabla \langle T \rangle$$

Similar correlation for  
Darcy's law

$$\nabla \langle T_x \rangle = \frac{1}{V} \int_V \overline{\nabla T(x)} \cdot \vec{n}_x \cdot dV$$

Simplification  
on

$$\nabla T_x = \frac{1}{V} \int_S T(x) \cdot \vec{i} \cdot \vec{n}_x \cdot dS = \frac{\Delta \langle T_x \rangle}{\Delta x}$$

$$\varphi_x = \frac{1}{V} \int_S x \cdot \overline{\varphi(x)} \cdot \vec{n}_x \cdot dS = \frac{P_x}{S_x}$$

# Full tensors determination

- Samples are anisotropic → thermo-physical parameters are tensors

$$\overline{\overline{K_{\text{eff}}}} = \begin{bmatrix} K_{xx} & K_{xy} & K_{xz} \\ K_{yx} & K_{yy} & K_{yz} \\ K_{zx} & K_{zy} & K_{zz} \end{bmatrix}$$

- Tensors are positive and symmetric :  $\begin{bmatrix} K_{xx} & K_{xy} & K_{xz} \\ K_{yx} & K_{yy} & K_{yz} \\ K_{zx} & K_{zy} & K_{zz} \end{bmatrix}$

- Experiment is repeated in each direction X, Y and Z

- 9 equations square

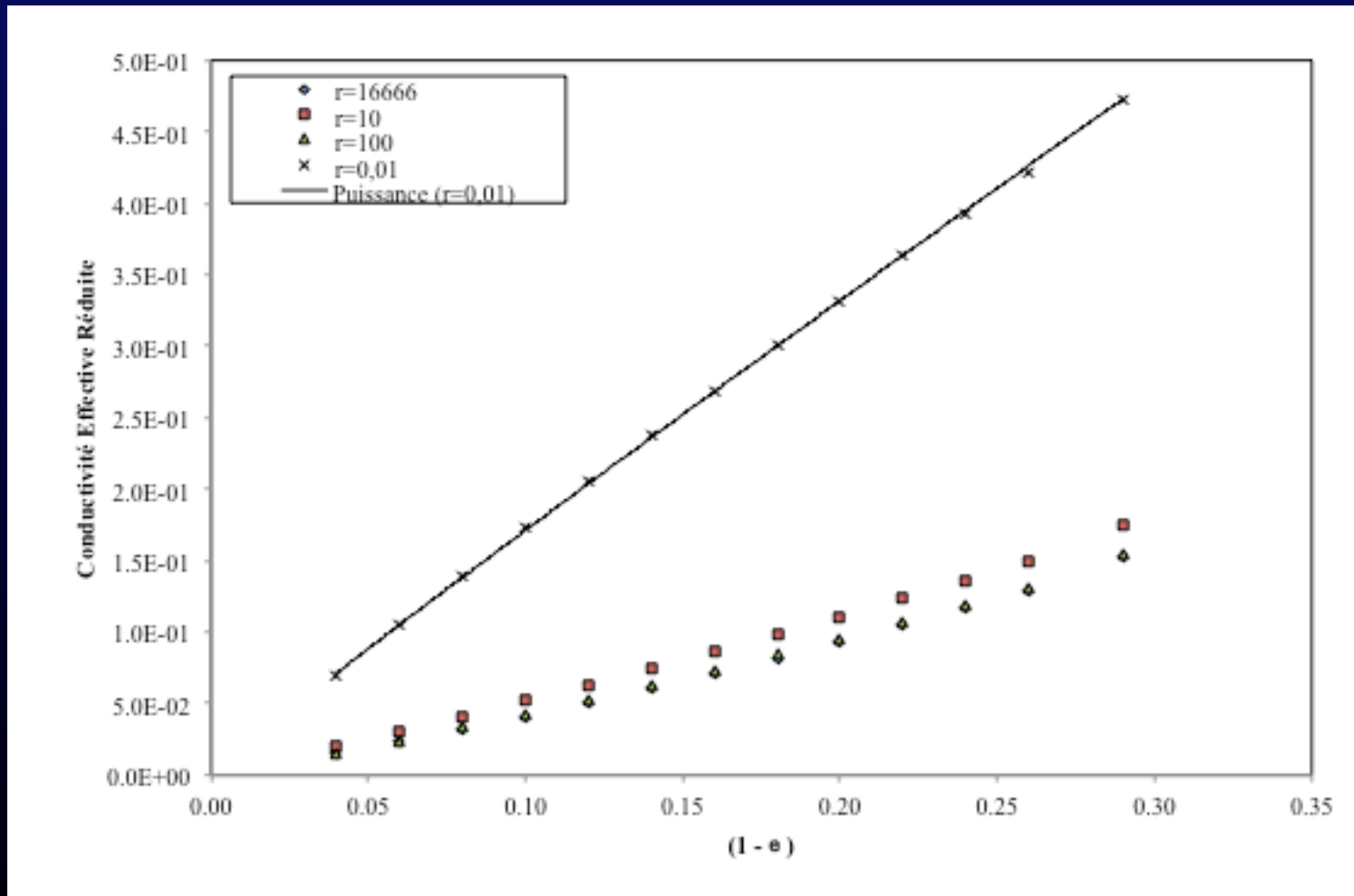
$$\begin{bmatrix} K_{xx} \\ K_{xy} \\ K_{xz} \\ K_{yx} \\ K_{yy} \\ K_{yz} \\ K_{zx} \\ K_{zy} \\ K_{zz} \end{bmatrix} = \begin{bmatrix} \nabla T_x^1 & \nabla T_y^1 & \nabla T_z^1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \nabla T_x^1 & \nabla T_y^1 & \nabla T_z^1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \nabla T_x^1 & \nabla T_y^1 & \nabla T_z^1 \\ \nabla T_x^2 & \nabla T_y^2 & \nabla T_z^2 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \nabla T_x^2 & \nabla T_y^2 & \nabla T_z^2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \nabla T_x^2 & \nabla T_y^2 & \nabla T_z^2 \\ \nabla T_x^3 & \nabla T_y^3 & \nabla T_z^3 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & \nabla T_x^3 & \nabla T_y^3 & \nabla T_z^3 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & \nabla T_x^3 & \nabla T_y^3 & \nabla T_z^3 \end{bmatrix}^{-1} \begin{bmatrix} \varphi_x^1 \\ \varphi_y^1 \\ \varphi_z^1 \\ \varphi_x^2 \\ \varphi_y^2 \\ \varphi_z^2 \\ \varphi_x^3 \\ \varphi_y^3 \\ \varphi_z^3 \end{bmatrix}$$

by least



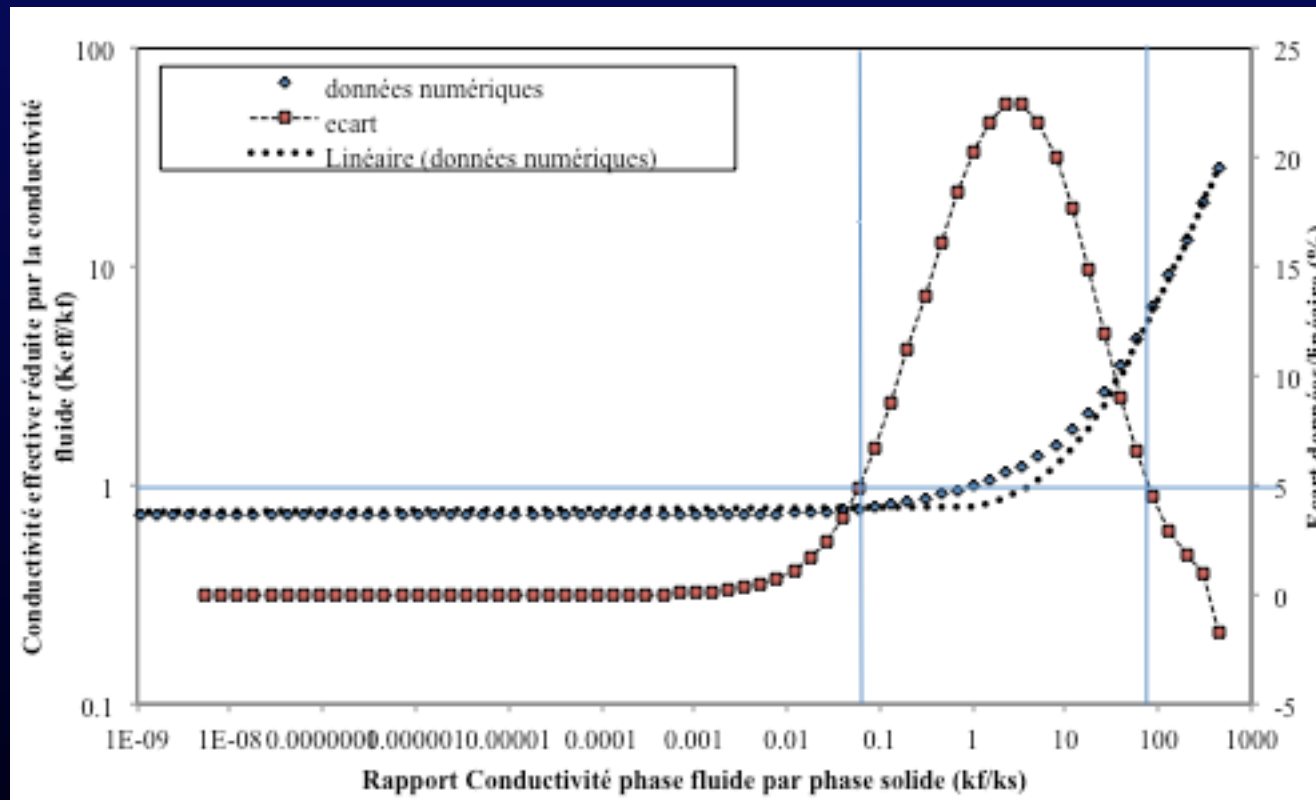
Results

# Conductivité effective réduite des cellules de Kelvin en fonction de la porosité



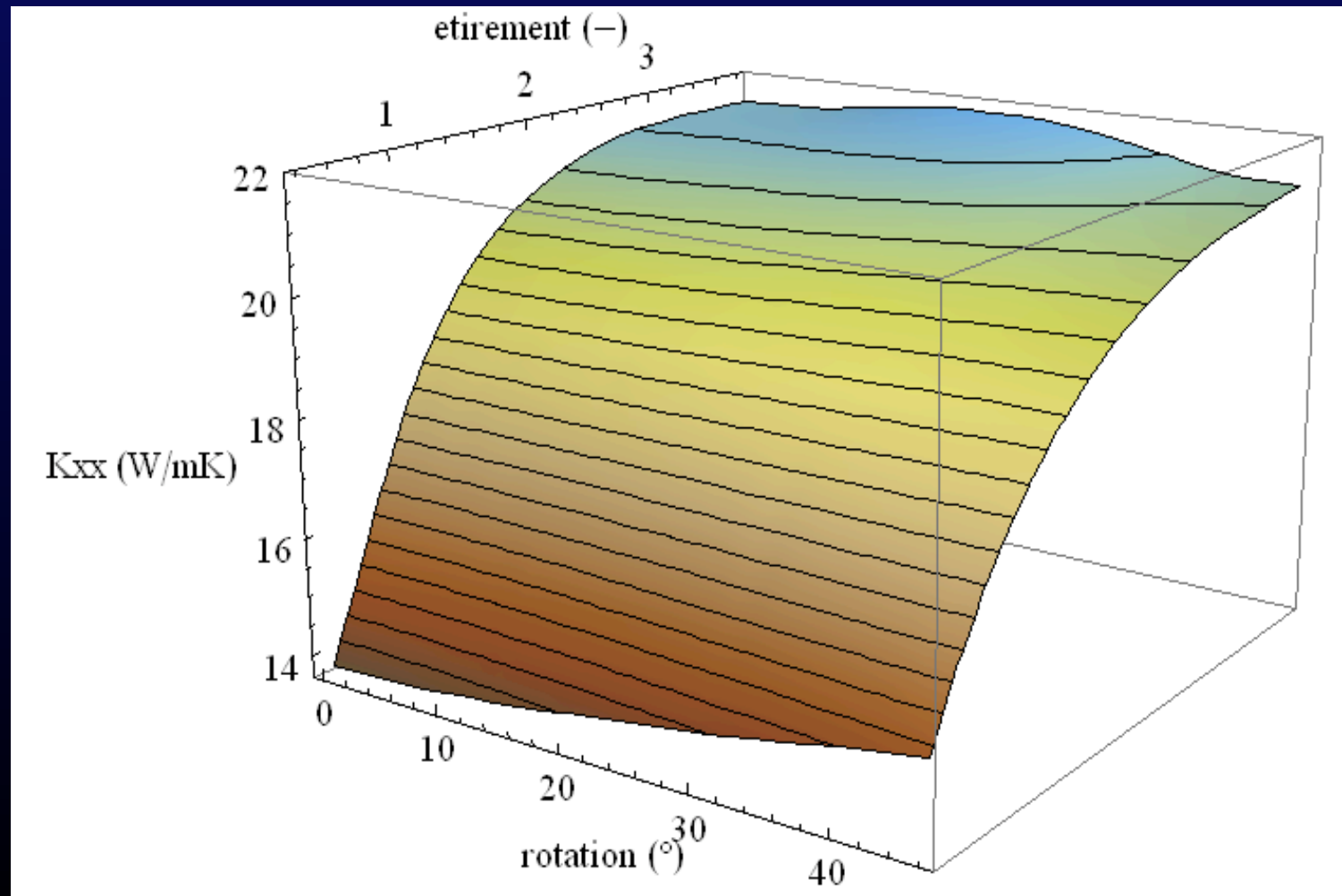
*pour 4 rapports de conductivité fluide/solide  $r$*

# Effet du rapport de conductivité

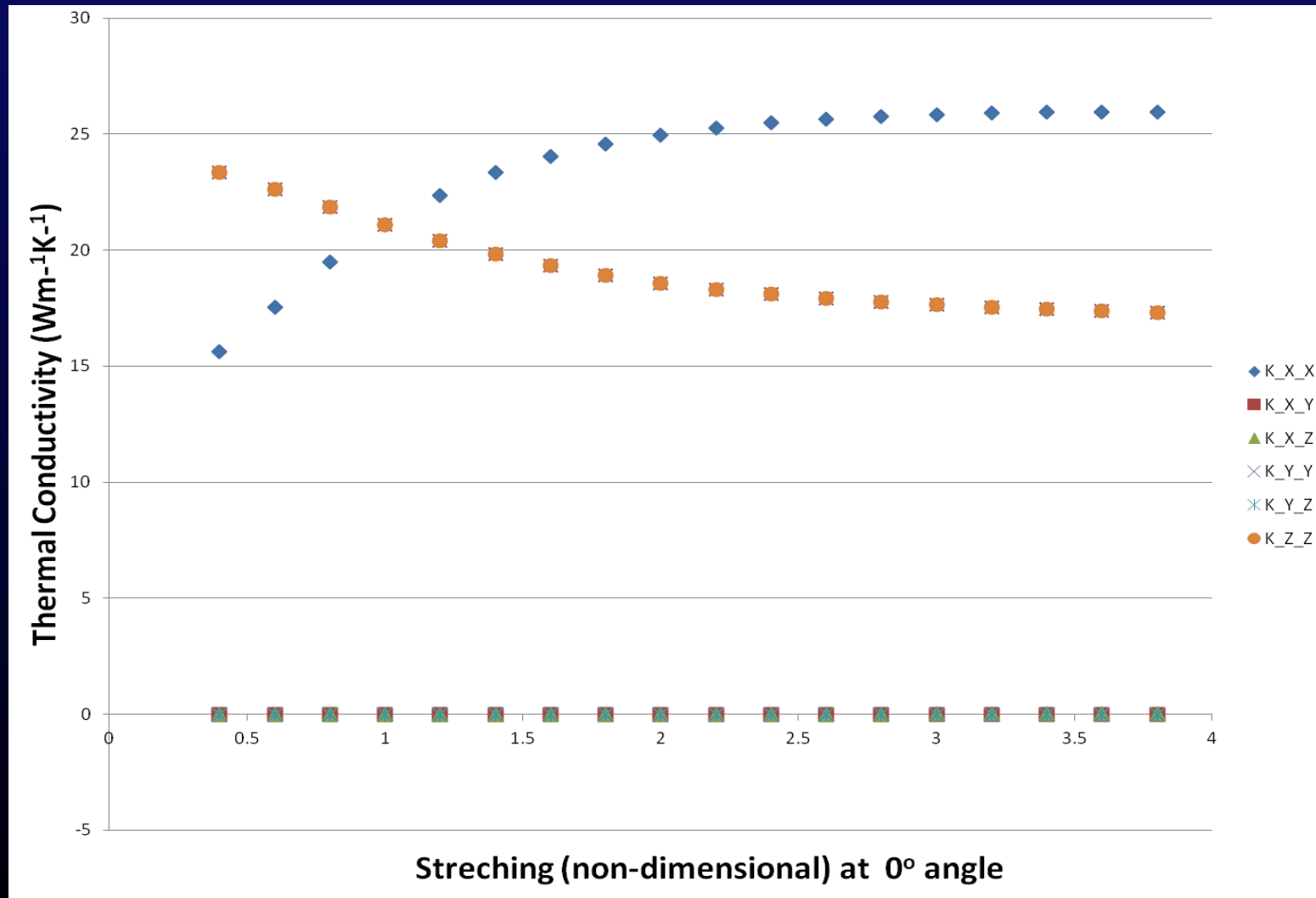


$$\lambda_e \neq \lambda_{eff}^s + \lambda_{eff}^f$$

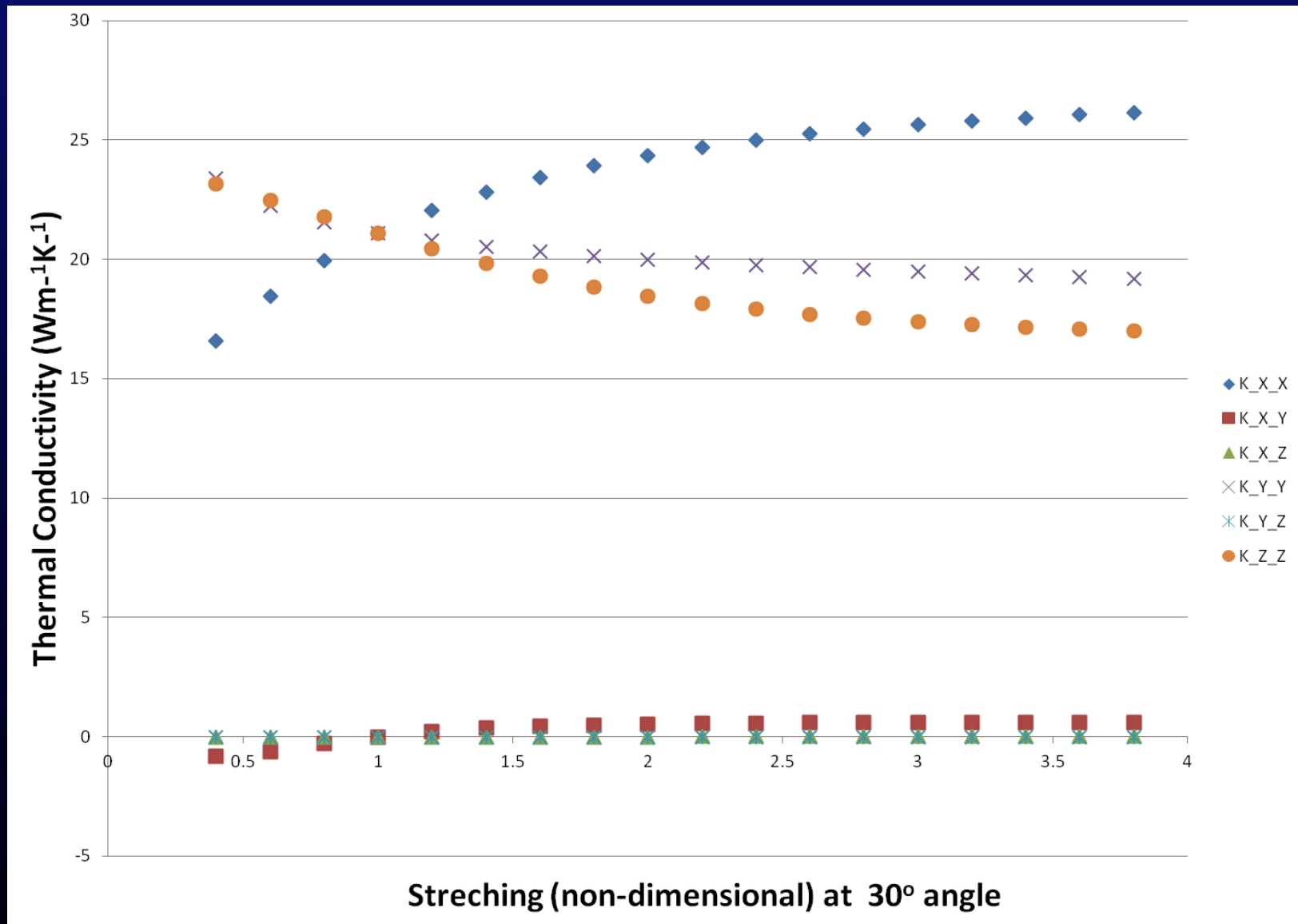
# Composante $K_{xx}$



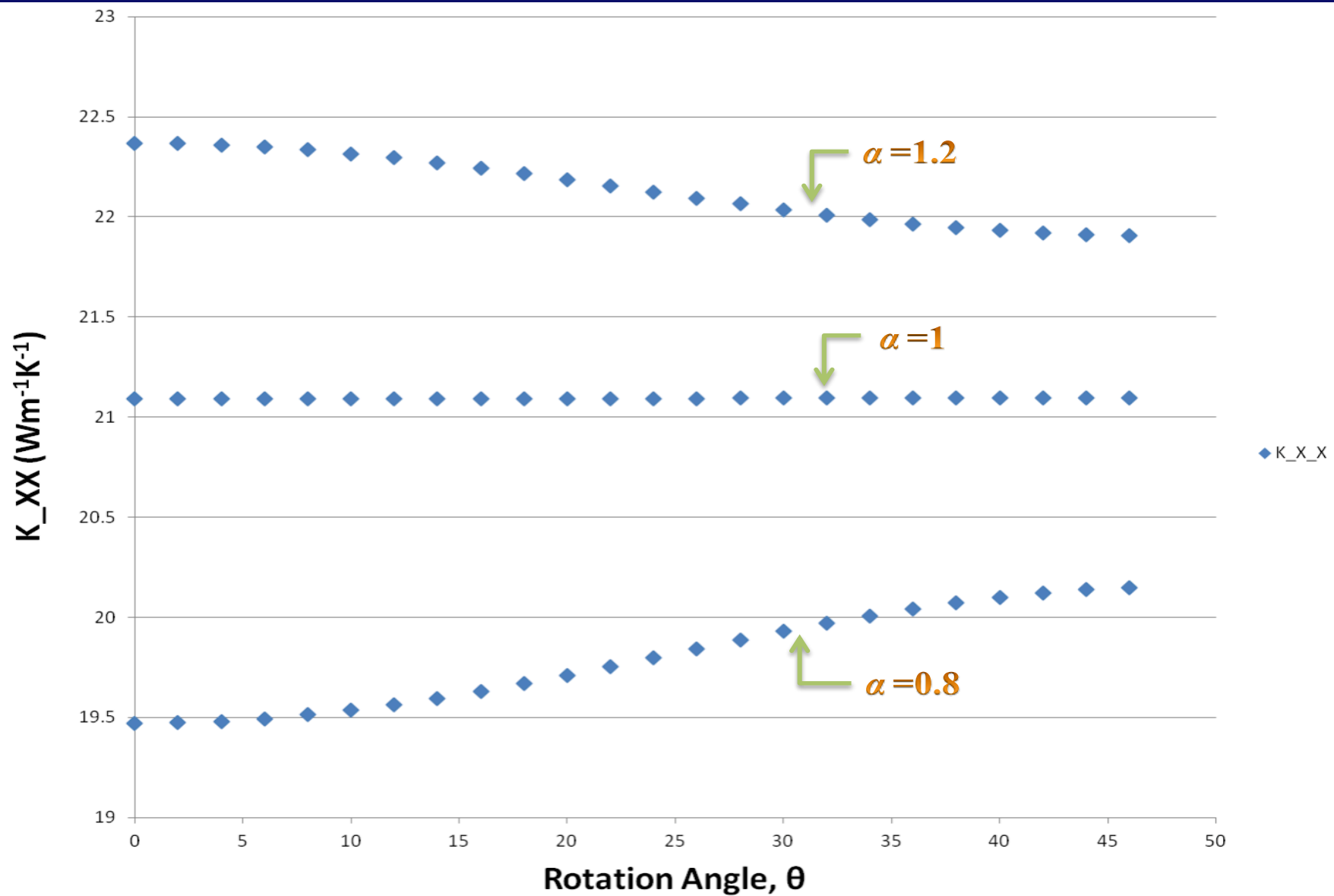
# Results on Effective Thermal Conductivity



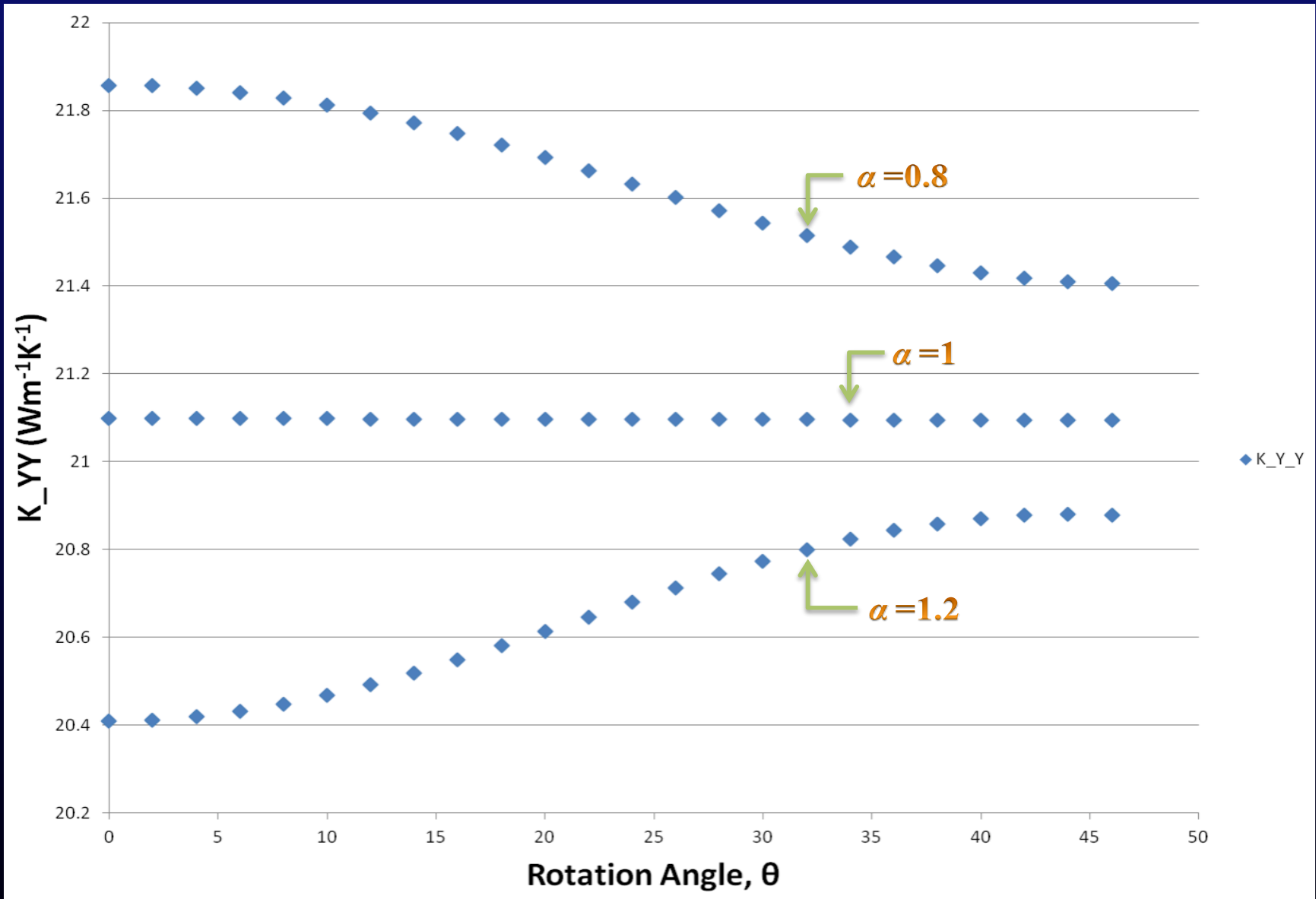
*Thermal conductivity plot at  $0^\circ$  angle for various  $\alpha$  for 80% porosity*



*Thermal conductivity plot at  $30^\circ$  angle for various elongations for 80% porosity*

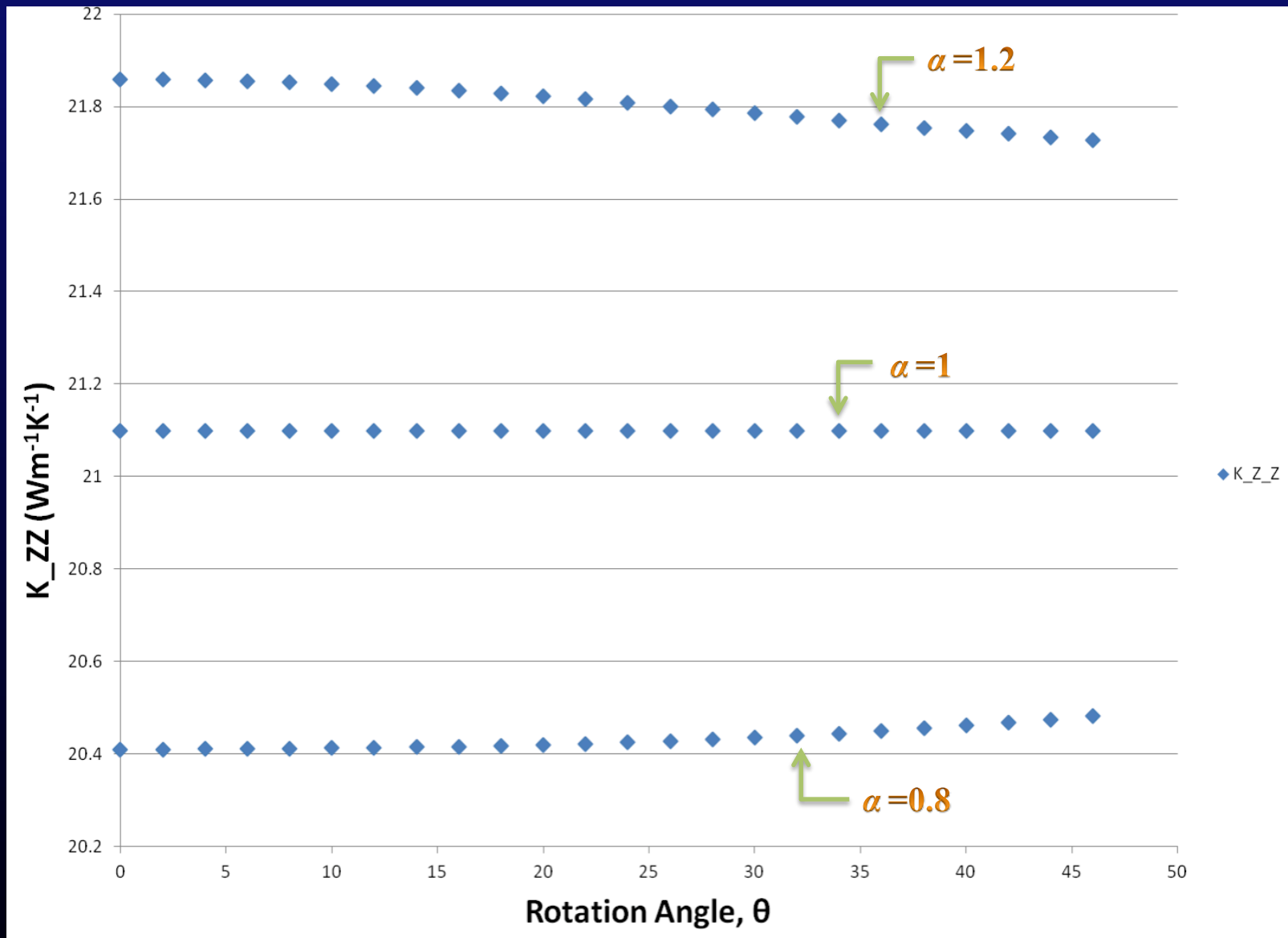


*Effect of elongation ratio,  $\alpha$  on  $K_{XX}$  with rotation angle for 80% porosity*



*Effect of elongation ratio,  $\alpha$  on  $K_{YY}$  with rotation angle for 80% porosity*

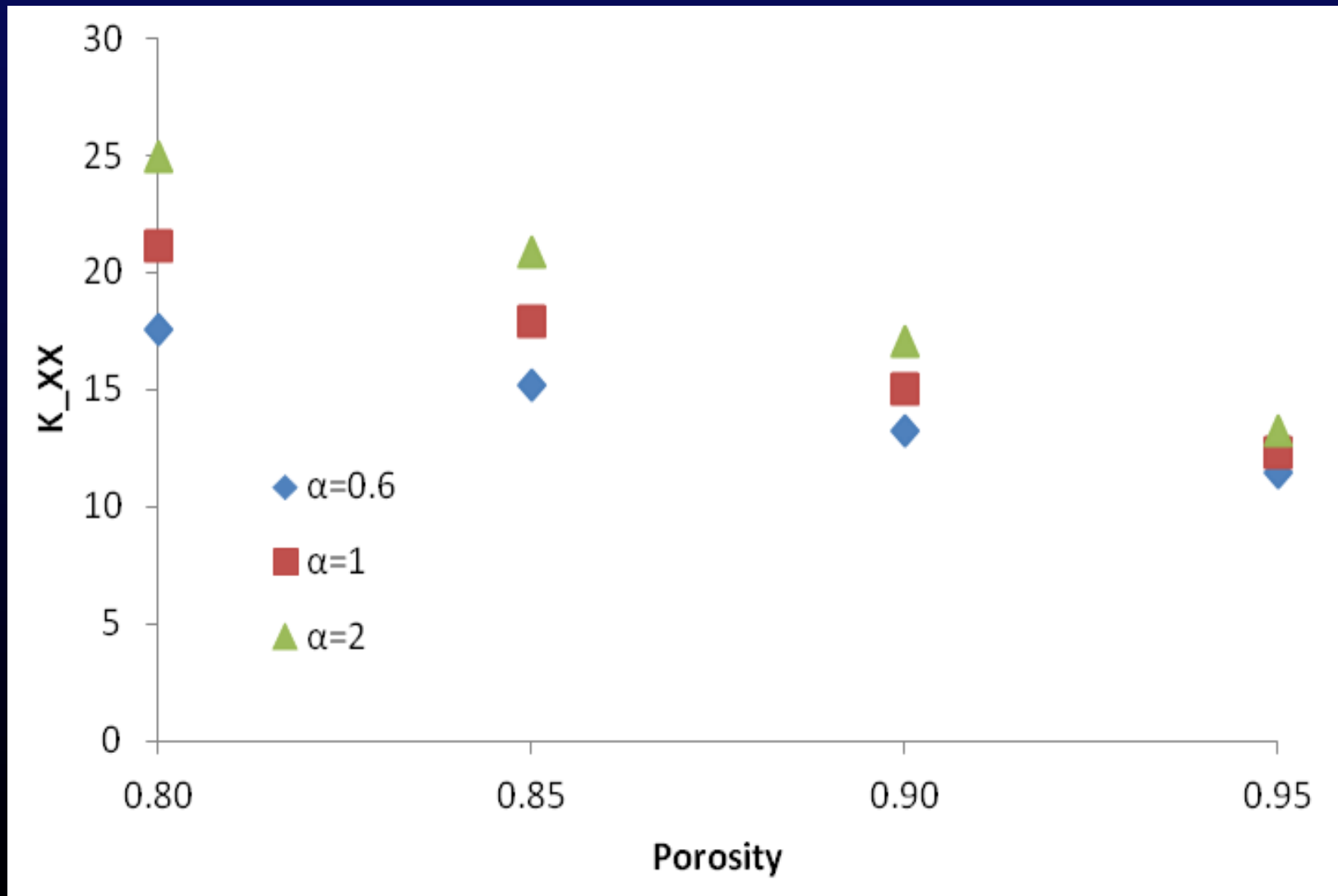




*Effect of elongation ratio,  $\alpha$  on  $K_{ZZ}$  with rotation angle for 80% porosity*

# Influence of porosity

- Comparisons are made at no-rotation



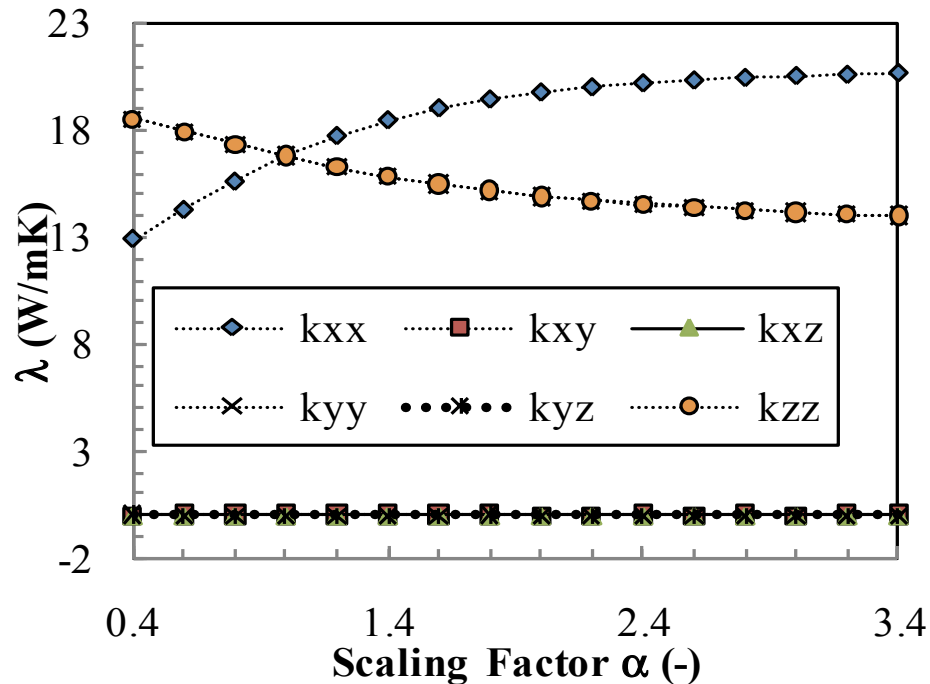
# Pore Elongation

For  $q = 0^\circ$

Increasing scaling factor  $X$

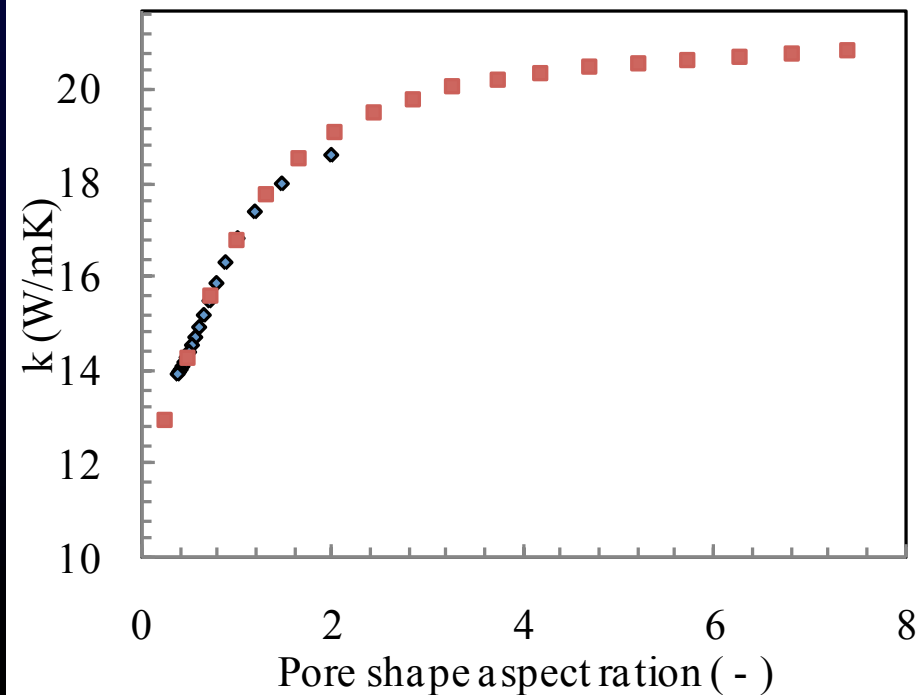
direction :

→ increase conductivity in  $X$

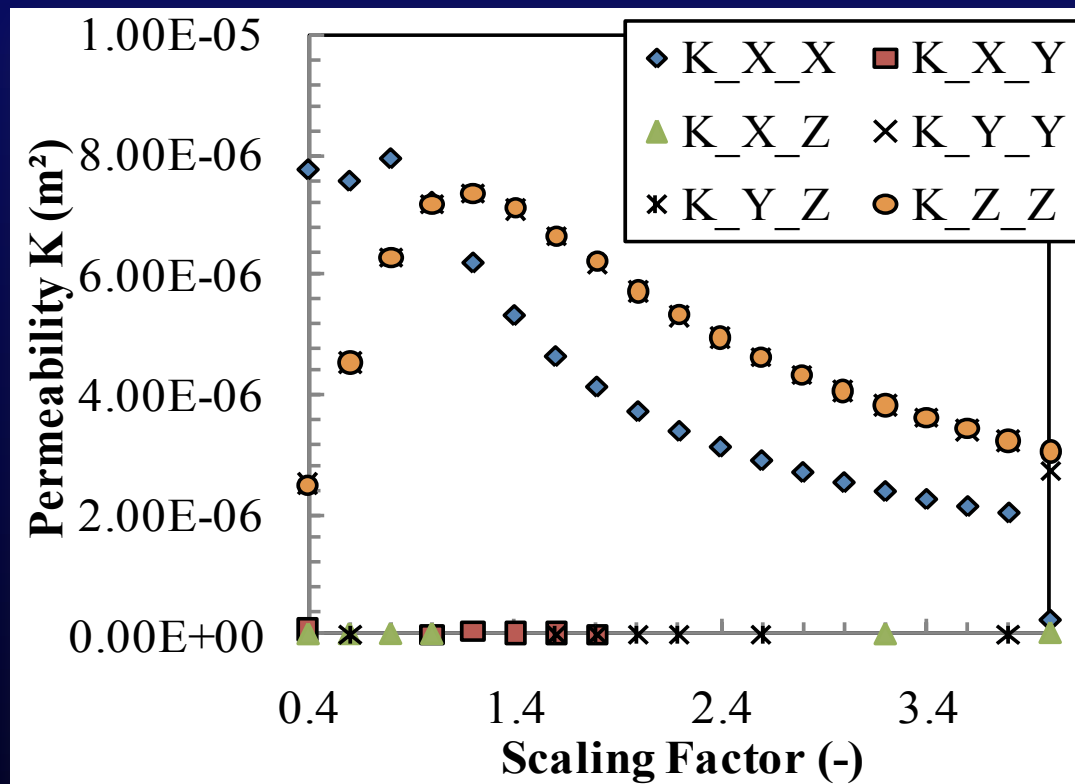


Effective conductivity followed pore shape aspect ratio and thus tortuosity

$$Aspect\ Ratio_i = \frac{Scale_i}{\sqrt{Scale_j Scale_k}}$$



# Permeability



For  $q = 0^\circ$

Increasing scaling factor X

direction :

→ decrease

permeability in X direction

→ increases

conductivity in Y and Z direction

Permeability in X direction follows pore hydraulic diameter

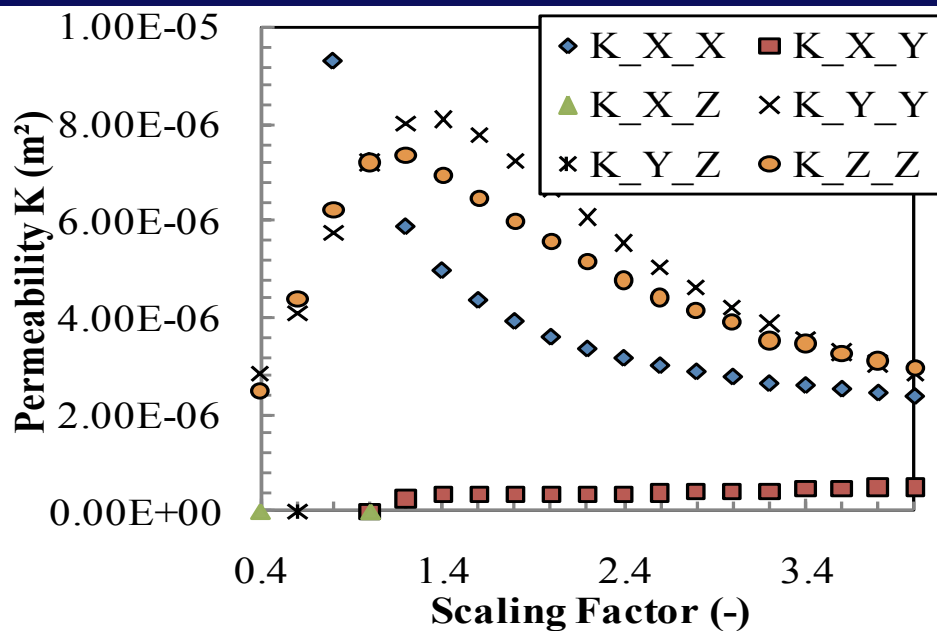
$$D_{h_x} = \frac{2 \text{ Scale Y Scale Z}}{\text{Scale Y} + \text{Scale Z}}$$

# Permeability

For  $q = 40^\circ$

Behavior is completely changed

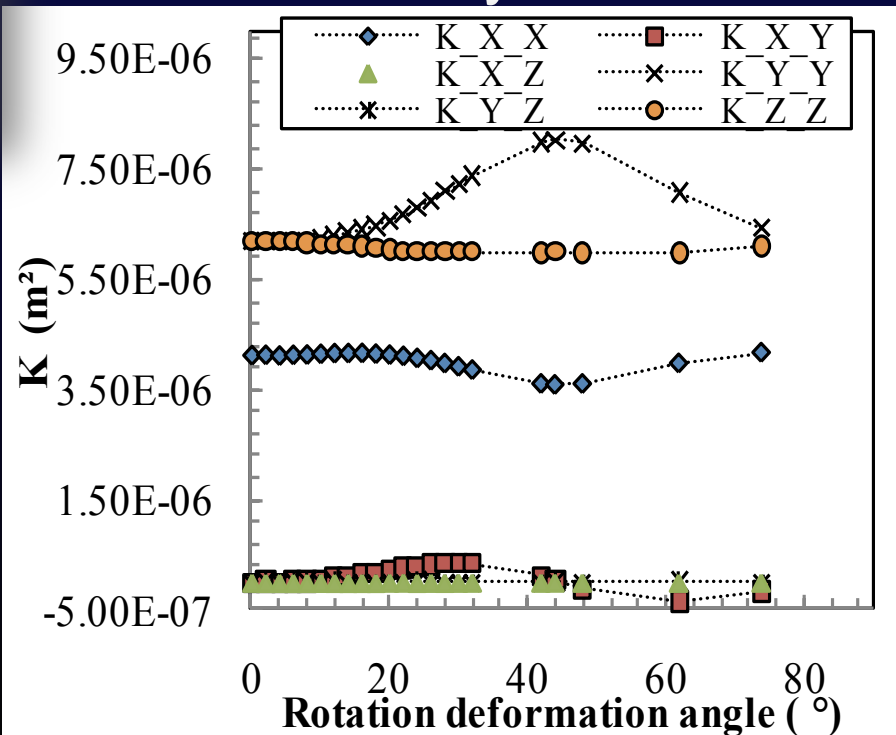
→ Permeability is on Y is



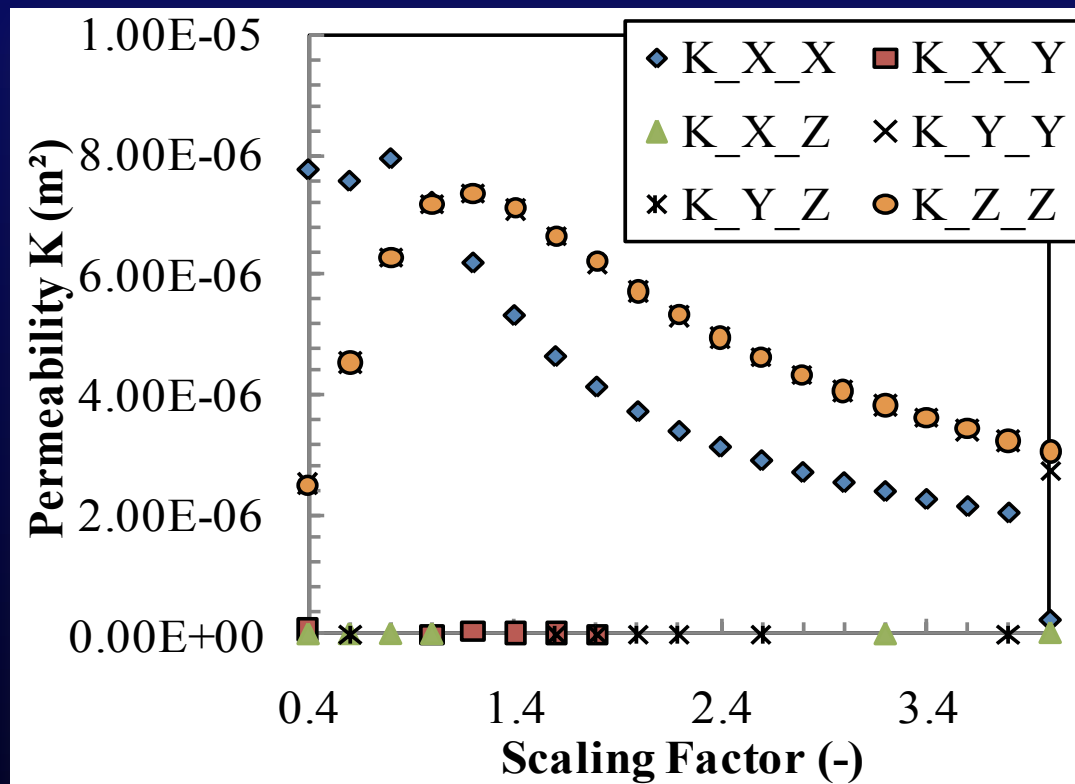
For  $a = 1.8$

→  $45^\circ$  is geometric symmetry plane

→ Non diagonal term appears



# Permeability



For  $q = 0^\circ$

Increasing scaling factor X

direction :

→ decrease

permeability in X direction

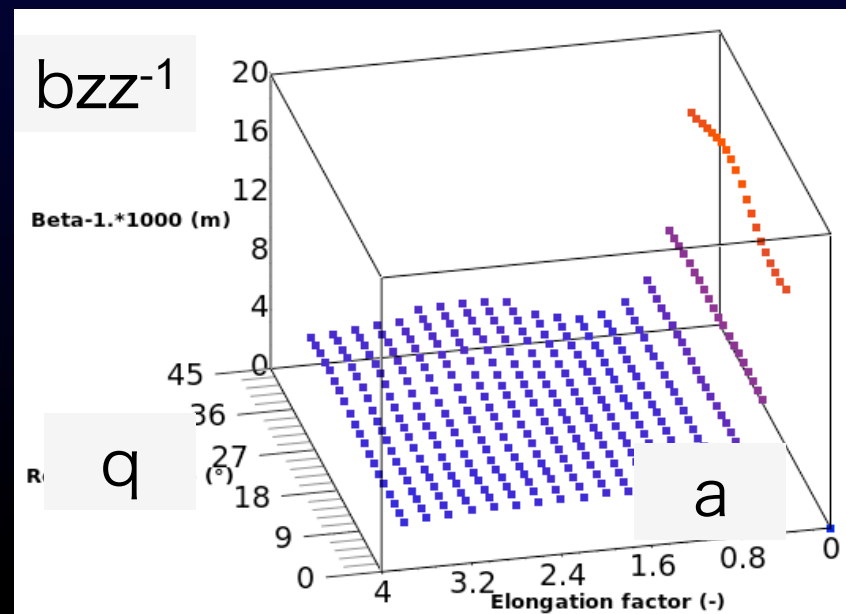
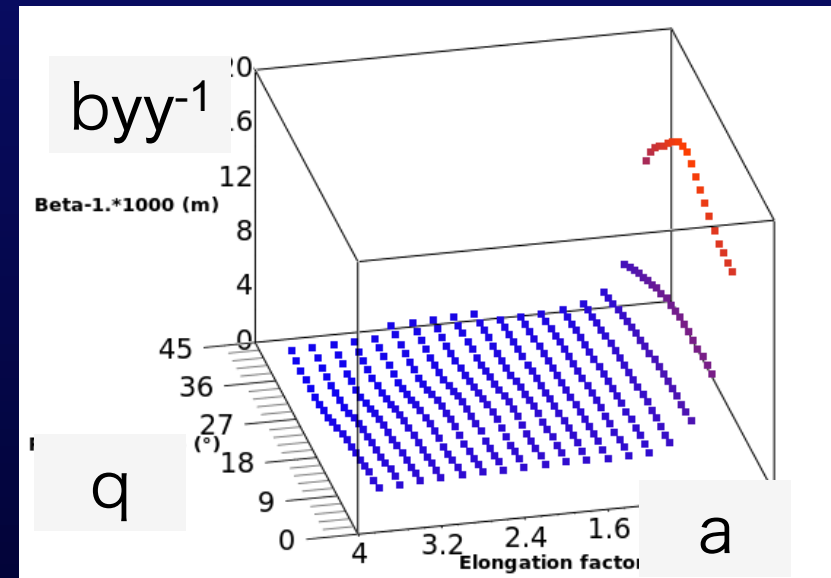
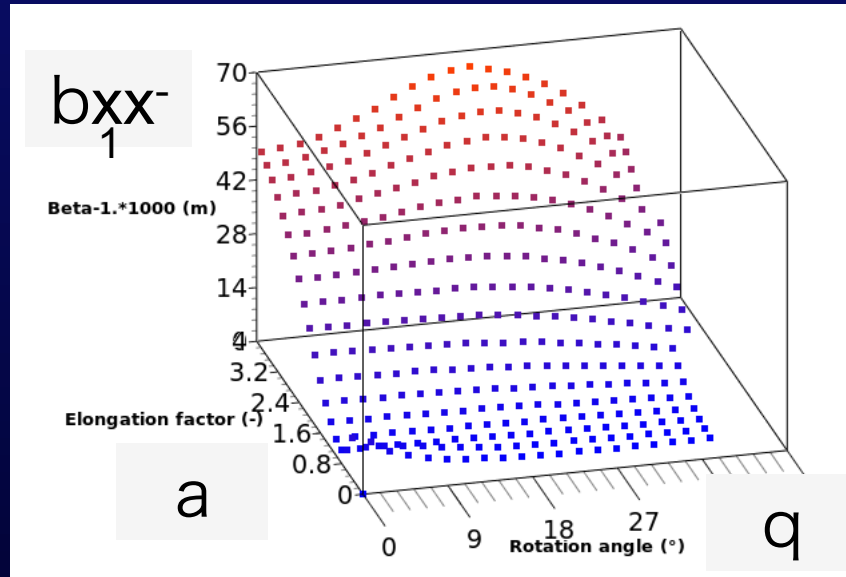
→ increases

conductivity in Y and Z direction

Permeability in X direction followed pore shape hydraulic diameter

$$D_{hx} = \frac{2 \text{ Scale } Y \text{ Scale } Z}{\text{Scale } Y \text{ Scale } Z}$$

# Inertia Coefficient



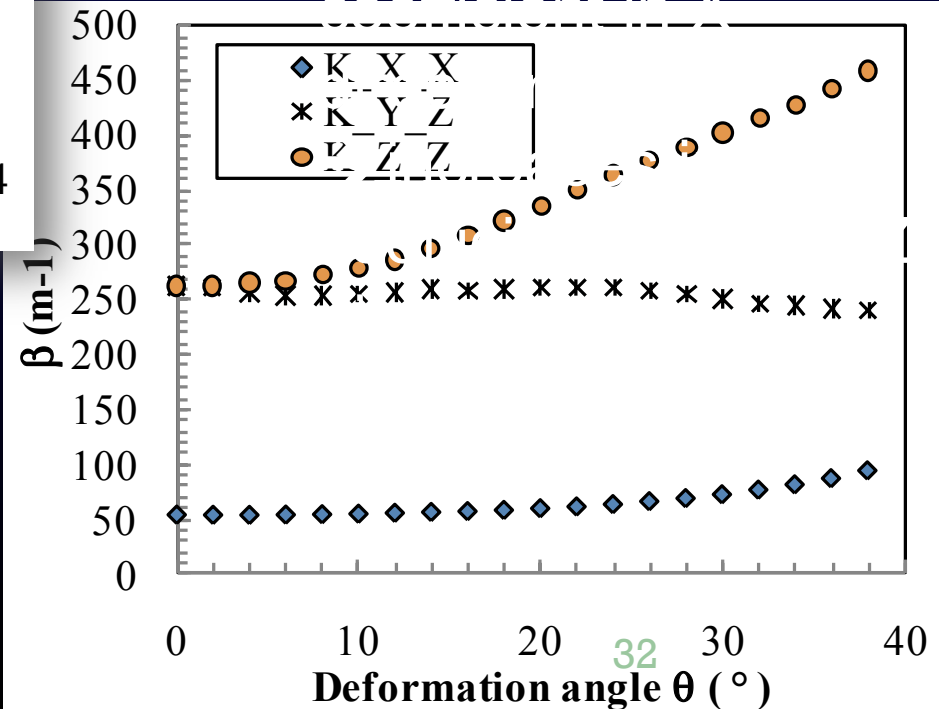
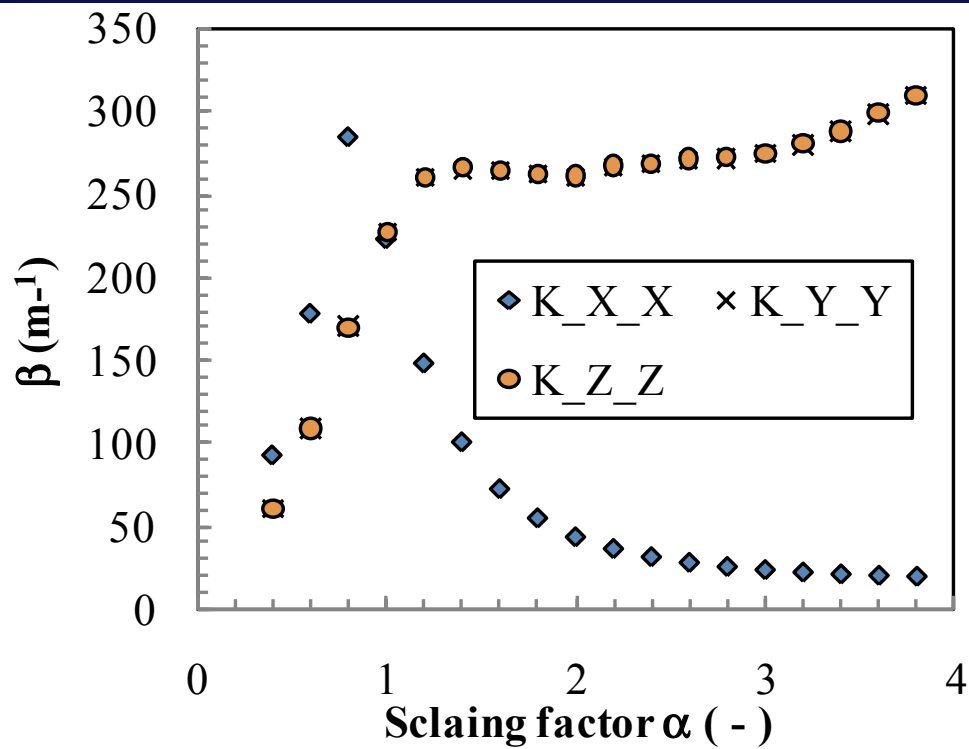
# Inertia Coefficient

For  $q = 0^\circ$

Increasing scaling factor X

direction :

→ decrease inertia coefficient in X





# Conclusion

- Propriétés de transports dépendent de la forme
- pour chaque type d'objet il existe des corrélations
- compréhension des relations encore insuffisante
- dispersion des résultats
- multiplicité des paramètres

# Thank You For Your Attention !

## 주령구

연회장에서 흥을 돋우기 위한 놀이기구의 하나로, 육각형이 8면, 정사각형이 6면인 14면체로써, 참나무로 만들었다. 각 면에는 주령구를 굴린 사람에게 어떤 행동을 지시하는 글이 새겨져 있다. 글의 내용을 모두 이해하기는 어려우나, 이를 통하여 당시 신라왕실과 귀족들의 풍류를 짐작할 수 있다.

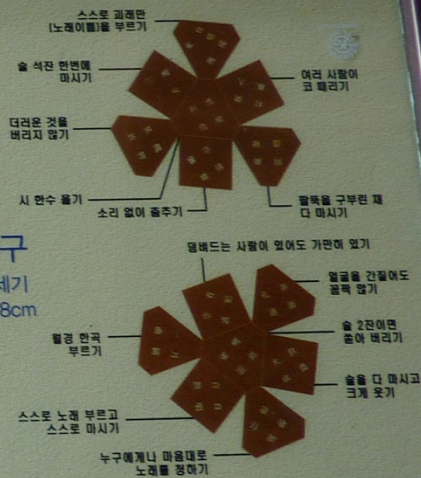
This musical instrument was used to boost the party atmosphere. Made with oak, it has a total of 14 sides: 8 hexagons and 6 squares. On each side, it has an instruction for the person who rolls the Juryeonggu. Although it is difficult to comprehend the instruction, we can make a guess about the elegance of Silla's royalty and aristocracy.

酒令具는宴會上助興用的遊戲工具，共有16面，其中8面為六角形，6面為正方形，椴木製成。酒令具各面上刻有指示遊戲參與者做某種行為的文字。雖然其中部分文字的內容現在已難以理解，但這件文物從一個側面為我們展示了當時新羅王室和貴族的“瀟灑”生活。

宴會の場を盛り上げるための遊具の1つで、8面の六角形と6面の正方形からなる14面体をなし、クヌギの木で作られている。各面には酒令具を転がした人になんらかの行動を指示する文が刻まれている。文の内容を全て判読することは難しいが、これを通して当時の新羅王室と貴族たちの優雅な宴を察することができる。

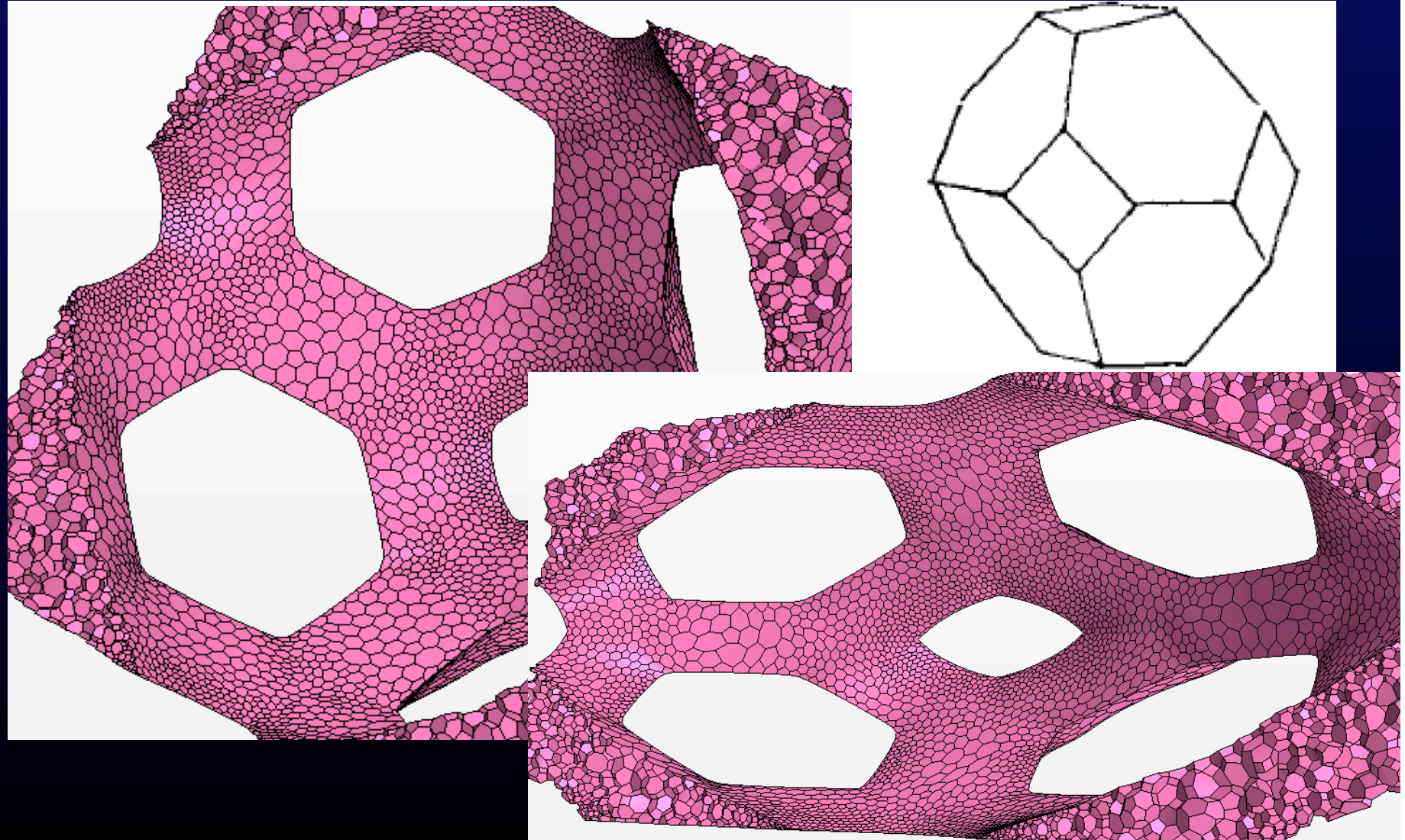


주령구  
8~9세기  
높이 4.8cm



주령구 펼친 그림

# La cellule unitaire



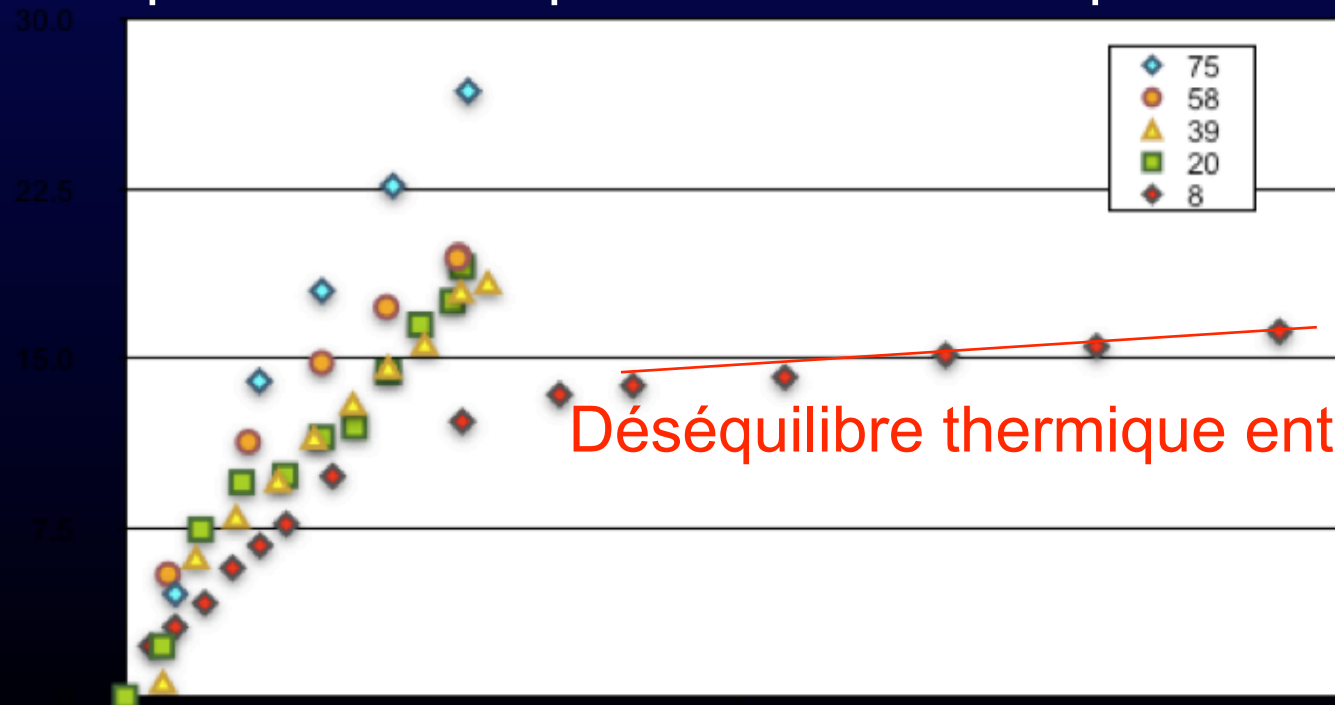
# Courbe d'ébullition

Apparition de l'ébullition pour des surchauffes très faibles

Flux critique très important

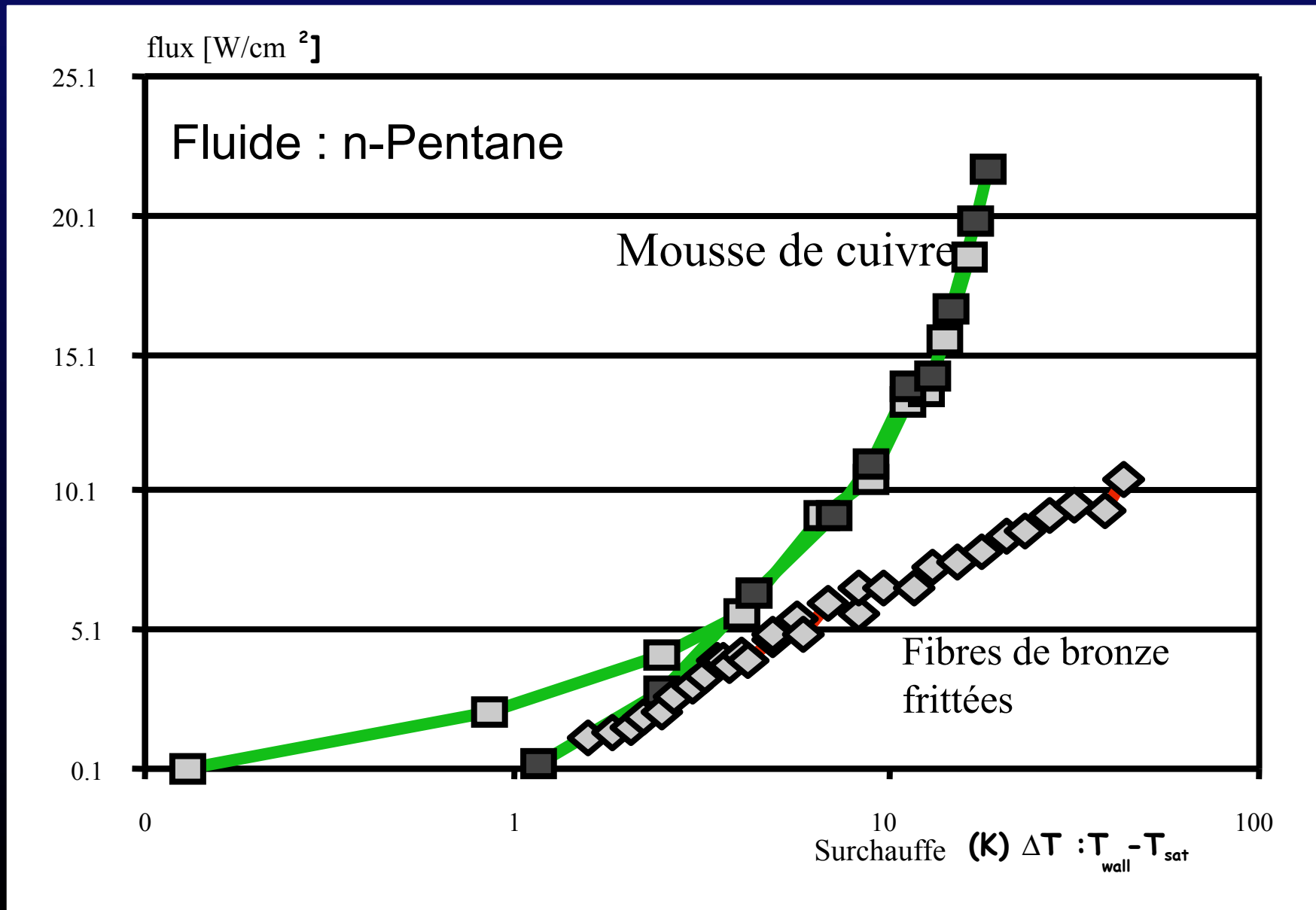
$$G > 10 \text{ kgm}^{-2}\text{s}^{-1}, Q_c > 30 \text{ W cm}^{-2}$$

Déséquilibre thermique observable uniquement pour les plus

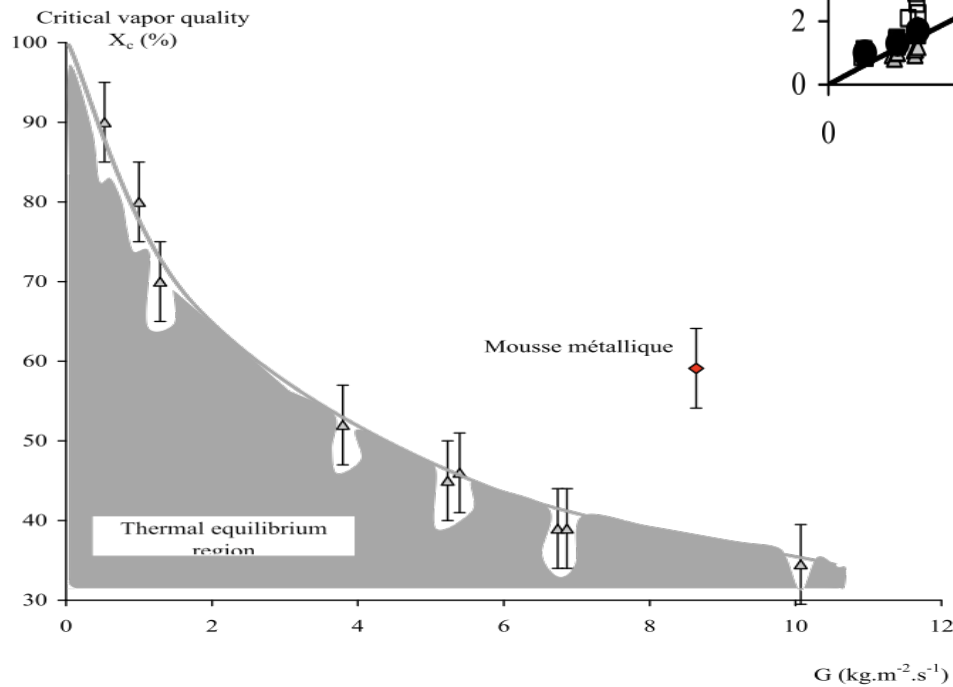
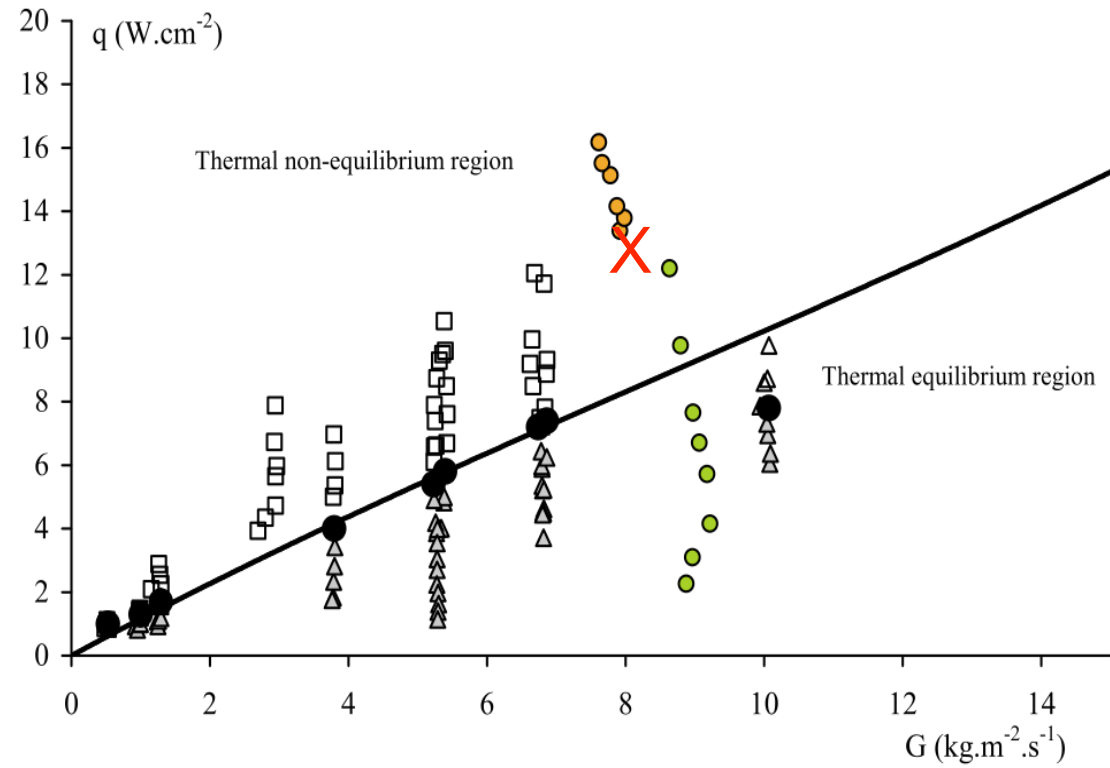


Déséquilibre thermique entre fluides

# Courbe d'ébullition Comparaison mousse - fibres



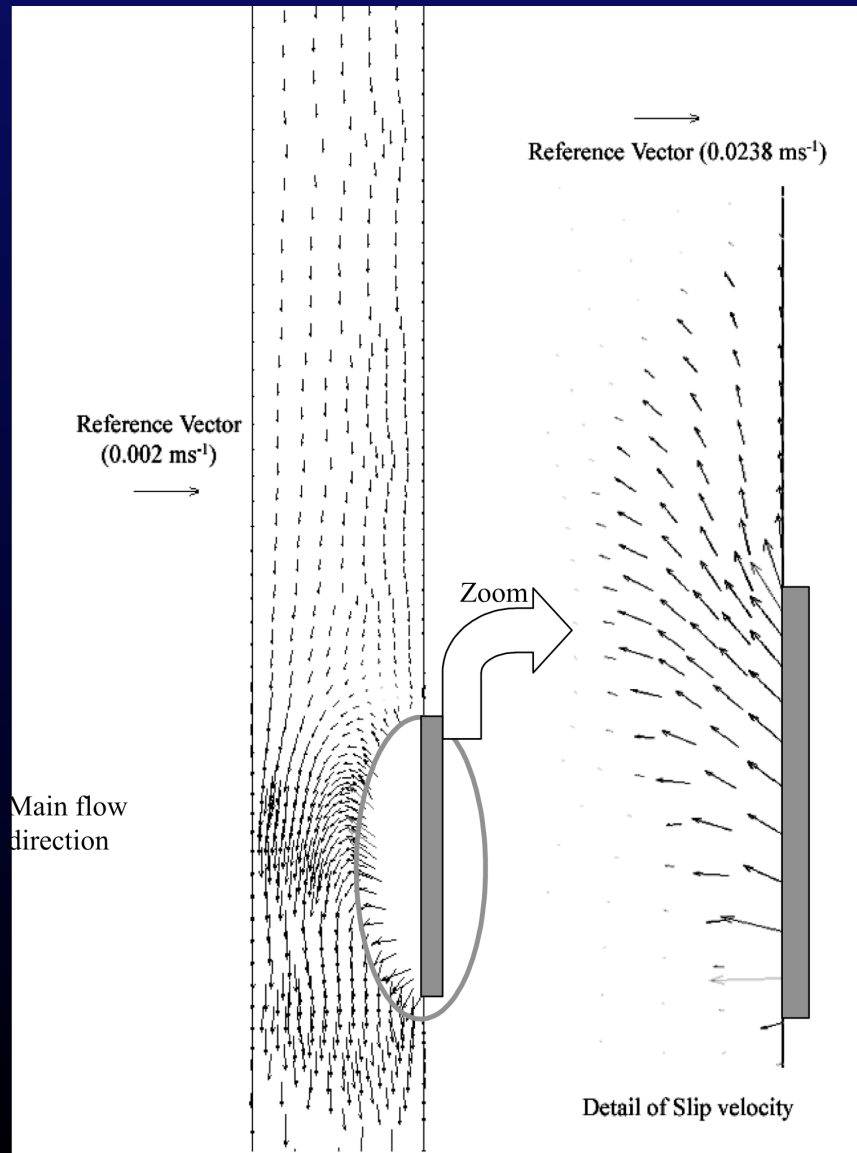
# Courbe critique



# Intensification des transferts

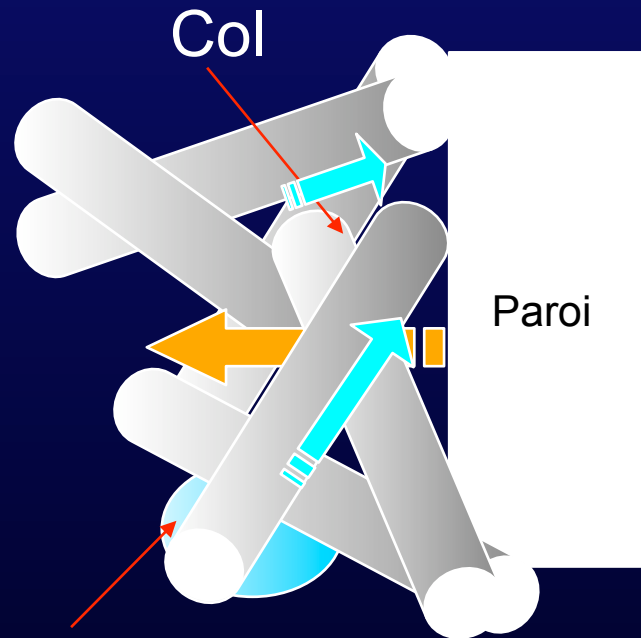
## Mécanismes

- Changement de phase au voisinage de la paroi
- Réalimentation en liquide
- Evacuation de la vapeur
- Effet ailette de la matrice solide
  - Apport thermique au cœur de l'écoulement
  - Accroissement des surfaces d'évaporation



Vitesse de glissement

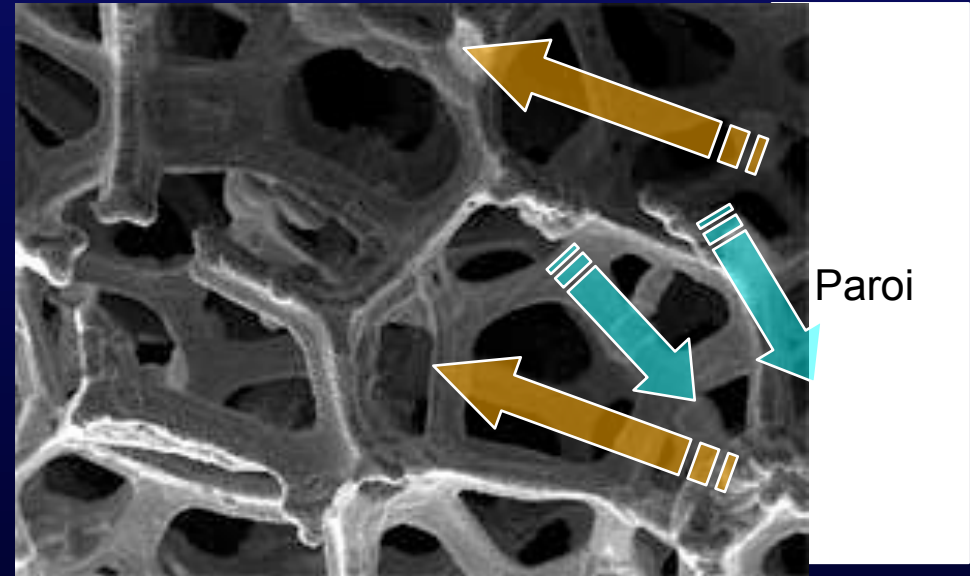
# Interprétation « hydrodynamique »



Goutte au voisinage du contact/col

Cols limitent écoulements  
(blocage par bulle ou  
goutte

Forme convexe ? films  
liquide



Pas de constriction :  
écoulements liquide  
vapeur à contre courant

Forme concave favorise  
l'alimentation par des  
films liquide