

Lecture 5 -A

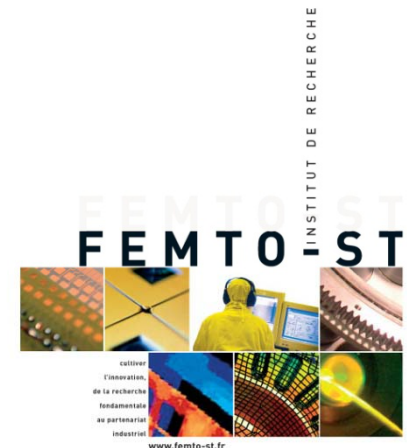
Measurements with contact in heat transfer: principles, implementation and pitfalls

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Metti⁵



Lecture 5-A

Part 1 : F. Lanzetta

Measurements with contact : temperature and (micro)thermocouples

Part 2 : B. Garnier

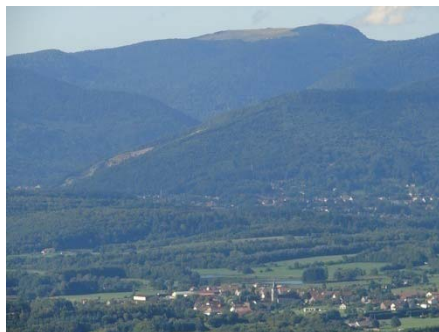
Measurements with contact : temperature and heat flux

Lecture 5-A

Part 1 : F. Lanzetta

Measurements with contact : temperature and (micro)thermocouples

BELFORT



**Belfort's Lion
(A. Bartholdi)**



Ballon d'Alsace - Vosges (1247 m)

Last week...

... and ...

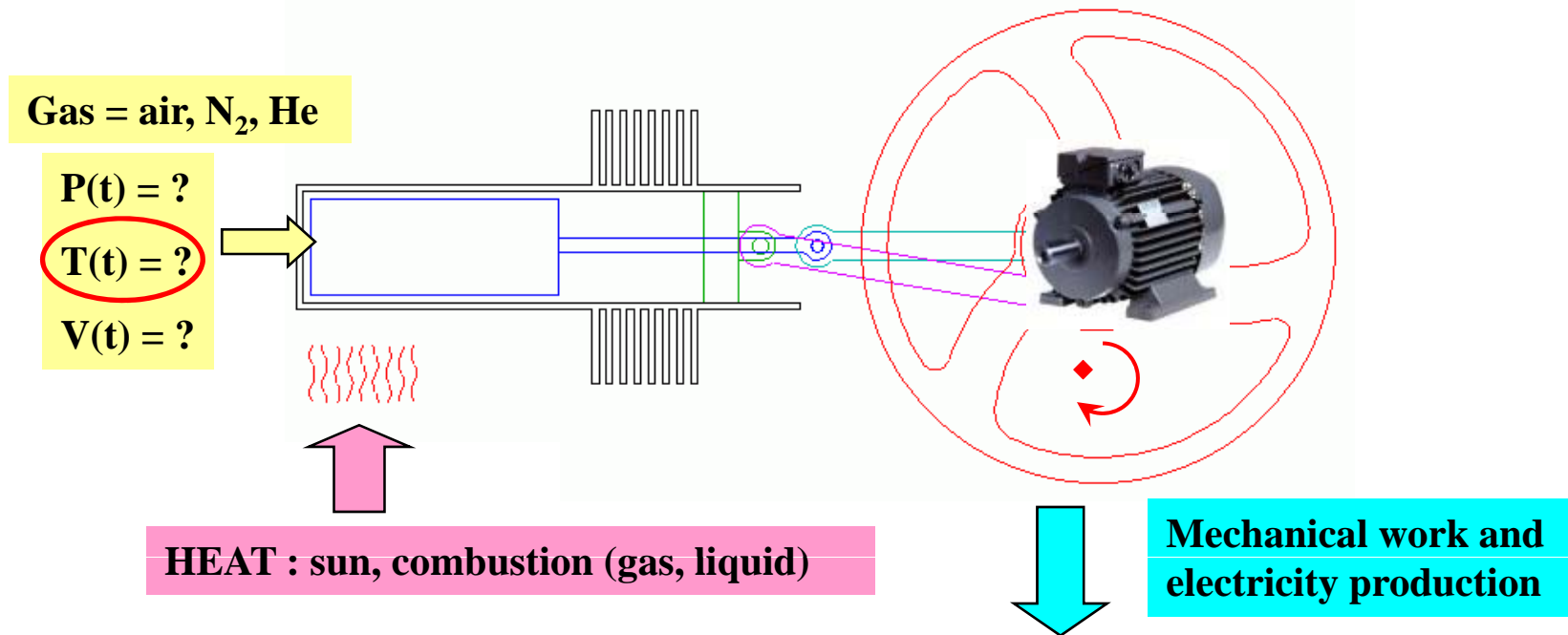
Next winter ?

My researches deal with machines like :

1) Stirling engine, cogeneration systems, regenerators (exchangers)

Oscillating flows : pressure, temperature, volume, velocity =f(time)

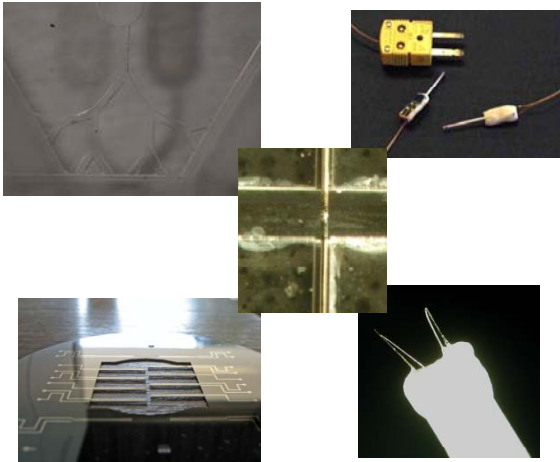
Convection coefficient $h_{cv}(\diamond)$ between gas/wall ? $Nu(\diamond) = ?$



2) Development of Instruments :

Temperature $T(t)$:

- microthermocouples,
- IR measurement



Fluid velocity $V(t)$:

- optical methods (PIV, LDV, etc...)
- microthermocouples



Pressure $P(t)$: commercial sensors



The (micro)thermocouple

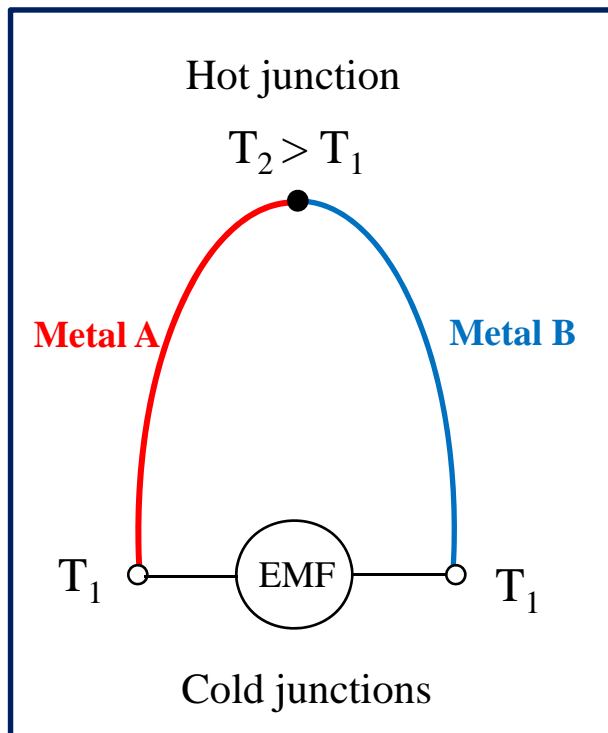
Introduction

- 1 The (micro)sensor
- 2 Theoretical model for transient measurements
- 3 Dynamic characterization
 - Convective calibration
 - Radiative calibration
 - Shock tube calibration

Conclusion

How does a thermocouple work ?

In 1821 T.J. Seebeck observed the existence of an electromotive force, EMF (V or μV) at the junction formed between two dissimilar metals (Seebeck effect) submitted to a temperature difference ($T_2 - T_1$).



Seebeck effect is actually the combined result of two other phenomenon, Thomson and Peltier effects.

Peltier discovered that temperature gradients along conductors in a circuit generate an EMF.

Thomson observed the existence of an EMF due to the contact of two dissimilar metals and the junction temperature.


Thomson effect is normally much smaller in magnitude than the Peltier effect and can be minimized and disregarded with proper thermocouple design.

How does a thermocouple work ?

$$E_{AB}(T_2, T_1) = \underbrace{\Pi_{AB}^{T_1} - \Pi_{AB}^{T_2}}_{\text{Peltier effect}} + \underbrace{\int_{T_2}^{T_1} (\tau_A - \tau_B) dT}_{\text{Thomson effect}}$$

Seebeck effect

$$E_{AB}(T_1, T_2) = \sigma_{AB}(T_2 - T_1)$$



$\diamond_{AB} = \text{Seebeck coefficient } (\mu\text{V} \cdot ^\circ\text{C}^{-1})$

 $\sigma_{AB} = \frac{dE}{dT}$

\diamond_{AB} depends on the two materials A and B

$$\diamond_{AB} = \text{Seebeck coefficient } (\mu\text{V}\cdot^{\circ}\text{C}^{-1})$$

Material	Seebeck coefficient ($\mu\text{V}\cdot^{\circ}\text{C}^{-1}$)	Material	Seebeck coefficient ($\mu\text{V}\cdot^{\circ}\text{C}^{-1}$)
Bismuth	-72	Silver	6.5
Constantan	-35	Copper	6.5
Alumel	-17.3	Gold	6.5
Nickel	-15	Tungsten	7.5
Potassium	-9	Cadmium	7.5
Sodium	-2	Iron	18.5
Platinum	0	Chromel	21.7
Mercury	0.6	Nichrome	25
Carbon	3	Antimony	47
Aluminium	3.5	Germanium	300
Lead	4	Silicium	440
Tantalum	4.5	Tellurium	500
Rhodium	6	Sélenium	900

K type = Chromel/Alumel

$$\diamond = 21.7 - (-17.3) = 39 \mu\text{V}\cdot^{\circ}\text{C}^{-1} @ 0^{\circ}\text{C}$$

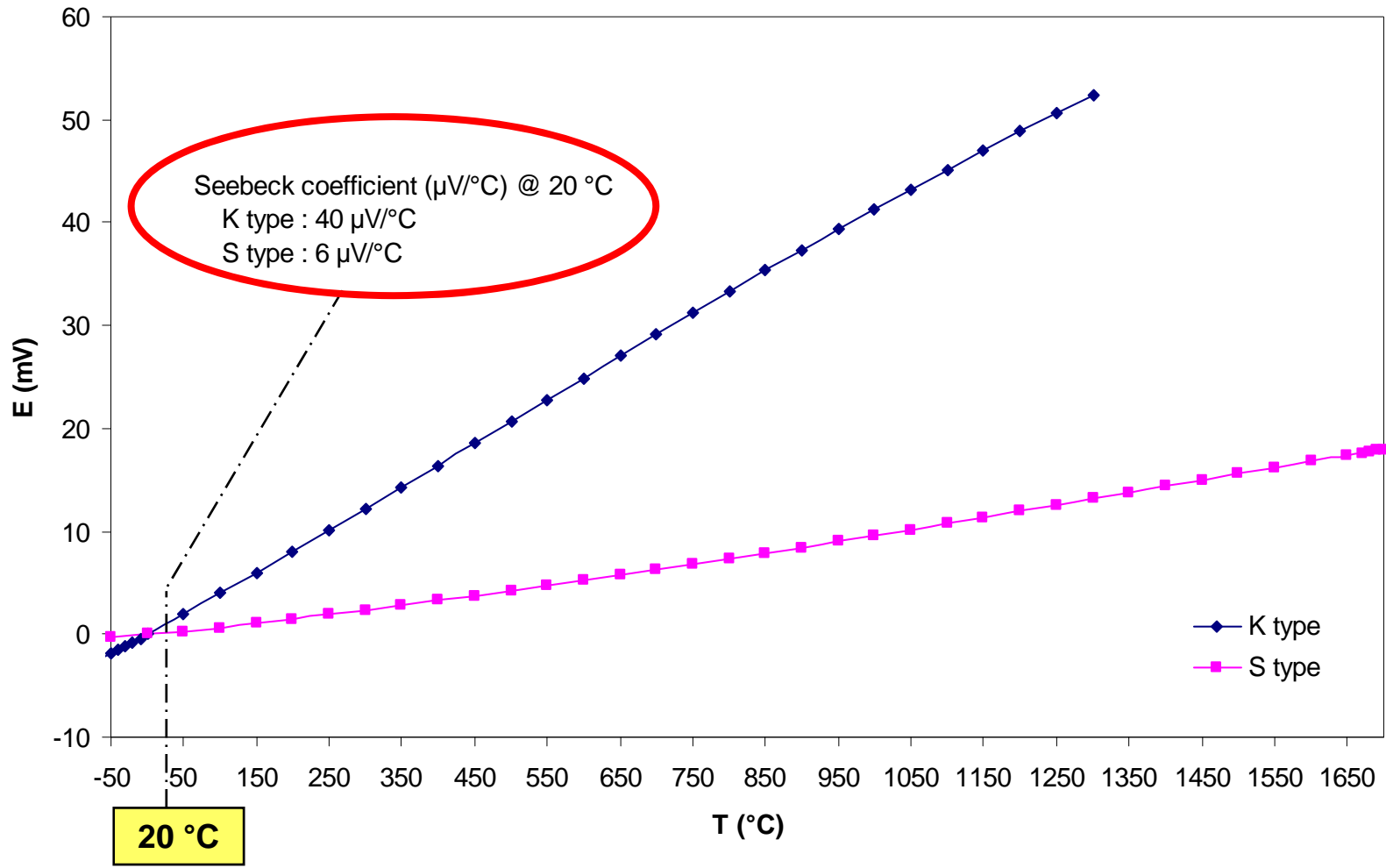
T type = Copper/Constantan

$$\diamond = 1.7 - (-37.3) = 49 \mu\text{V}\cdot^{\circ}\text{C}^{-1} @ 0^{\circ}\text{C}$$

« Mettler » type = Nickel/Silicium

$$\diamond = 440 - (-15) = 455 \mu\text{V}\cdot^{\circ}\text{C}^{-1} @ 0^{\circ}\text{C} !!!$$

Seebeck coefficient versus temperature



Electromotive force versus temperature for S type and K type thermocouples (ITS-90)

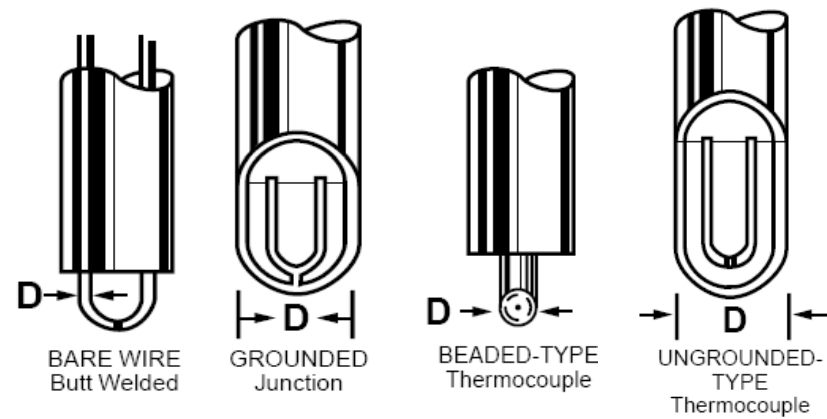
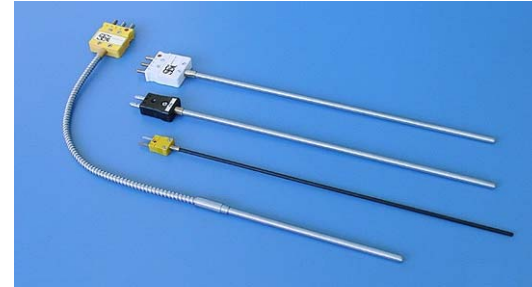
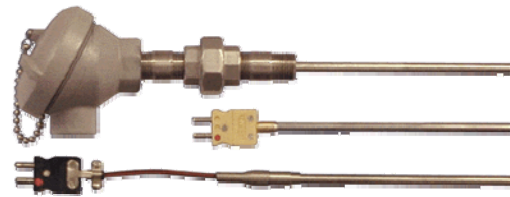
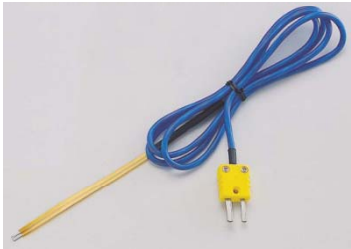
Advantages of Thermocouples

- Cheap
- Wide temperature range ($-270\text{ }^{\circ}\text{C}$ to $2100\text{ }^{\circ}\text{C}$)
- Small (...down to $0.5\text{ }\mu\text{m}$)
- Easy to integrate into automated data systems

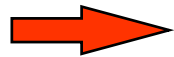
Disadvantages of Thermocouples

- Small signals, limited temperature resolution (from 0.1 to 1 K)
- Thermocouple wires must extend from the measurement point to the readout. Signal generated wherever wires pass through a thermal gradient.
- At higher temperatures, thermocouples may undergo chemical and physical changes, leading to loss of calibration.
- Recalibration of certain types of thermocouples or in certain applications is very difficult.

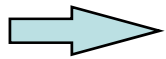
Commercial thermocouples



From thermocouples to microthermocouples...



Temperature fluctuations measurement = microthermocouples



Micronic and sub-micronic thermocouples

- S type : Platinum/Platinum-Rhodium 10% : **6 $\mu\text{V}/^\circ\text{C}$** at 20 $^\circ\text{C}$

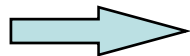
- **diameters = 0.5 ; 1.27 and 5.3 μm**

- K type : Chromel/Alumel : **40 $\mu\text{V}/^\circ\text{C}$** at 20 $^\circ\text{C}$

- **diameters = 7.6 ; 12.7 ; 25.4 ; 53 μm**



Spatial resolution and dynamic response



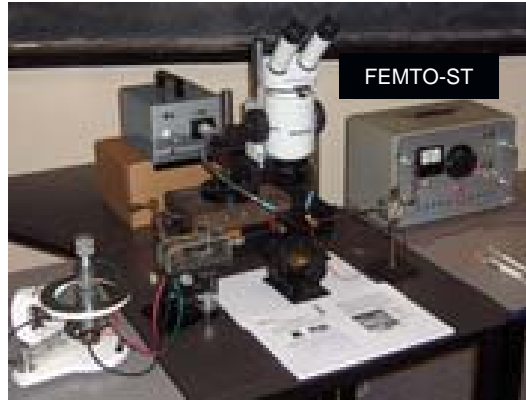
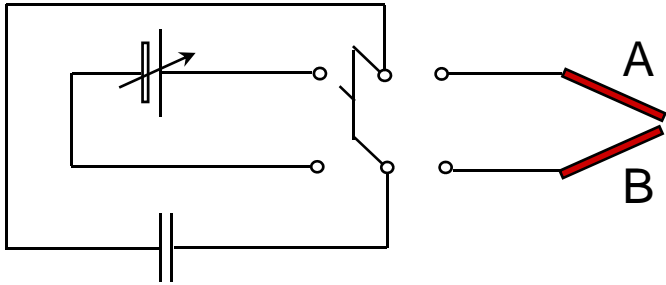
Dynamic calibration methods : time constant ?

- convective calibration

- radiative excitation

- shock tube

1 The (micro)sensor

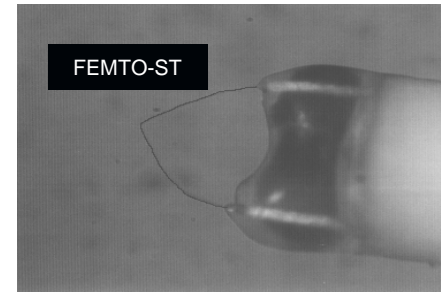


Circuit for beading by
condenser-discharge method
tension : 0 - 250 V
capacitance : 0 - 5 μ F

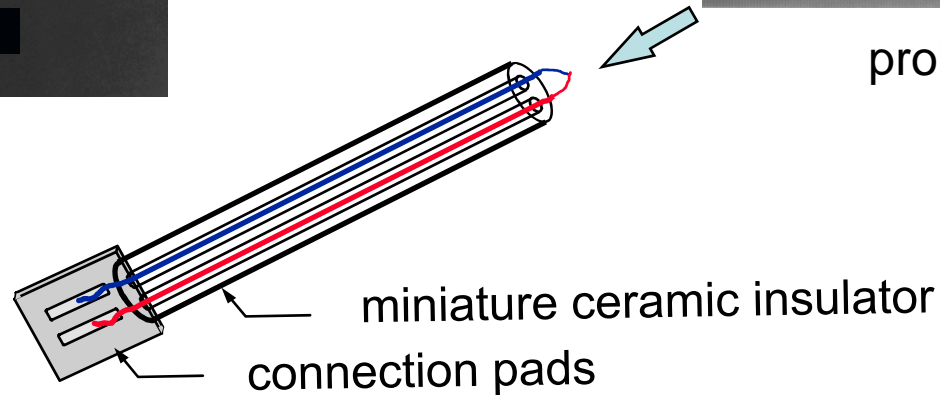


junction

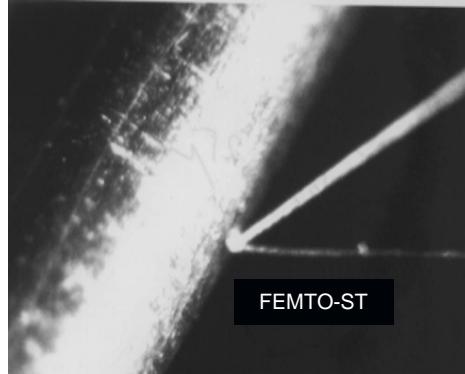
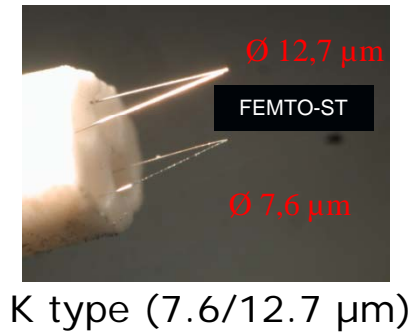
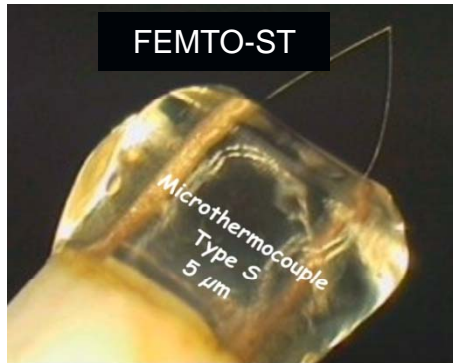
S type
thermocouple
 ϕ 1.27 μ m
6 μ V/ $^{\circ}$ C at 20 $^{\circ}$ C



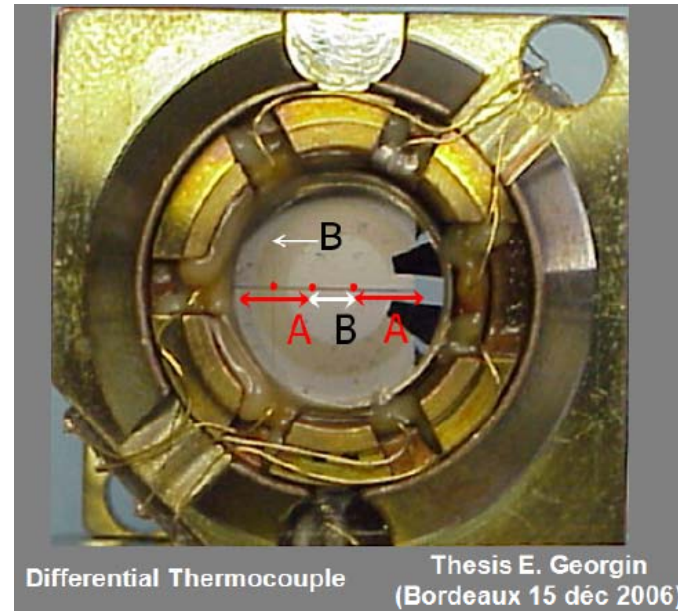
probe



Different microthermocouples

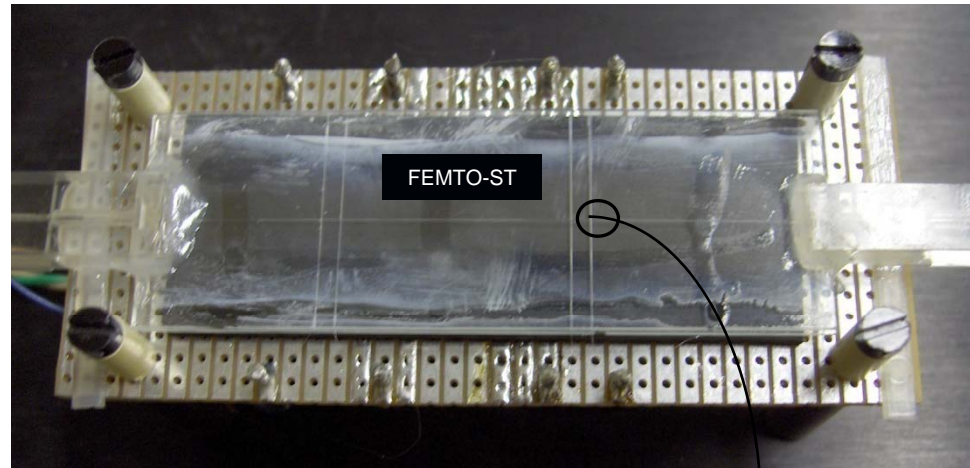
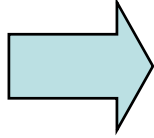


K type 25.4 µm
directly welded on a
solid surface (inox)



Temperature and flow measurements

N₂ flow



Microfluidics gas flow

K type 25.4 μm

Channel :

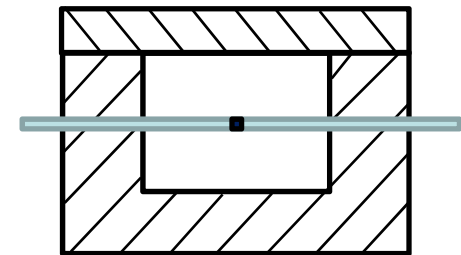
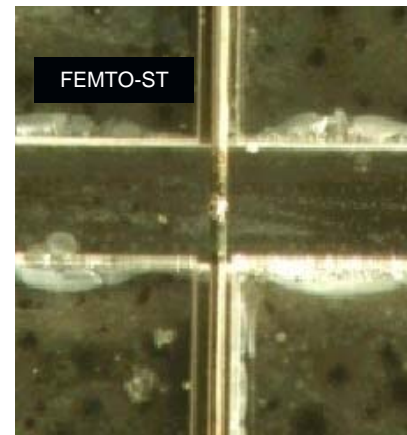
Materials :

- PMMA (transparent thermoplastic)
- Glass

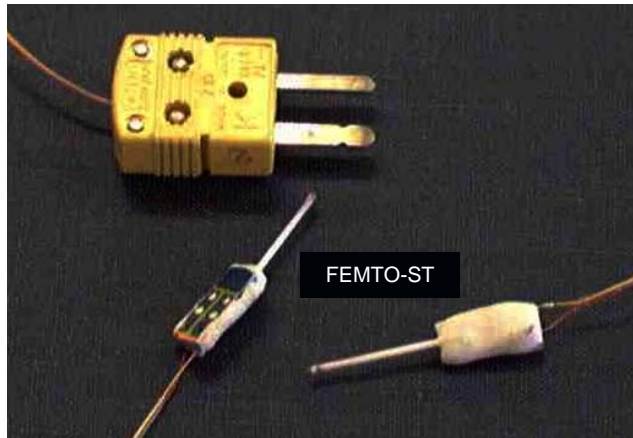
Length = 50 mm

section = 150 μm X 200 μm

(hydraulic diameter = 170 μm)



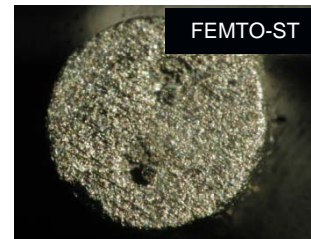
Surface temperature measurements in heat engines



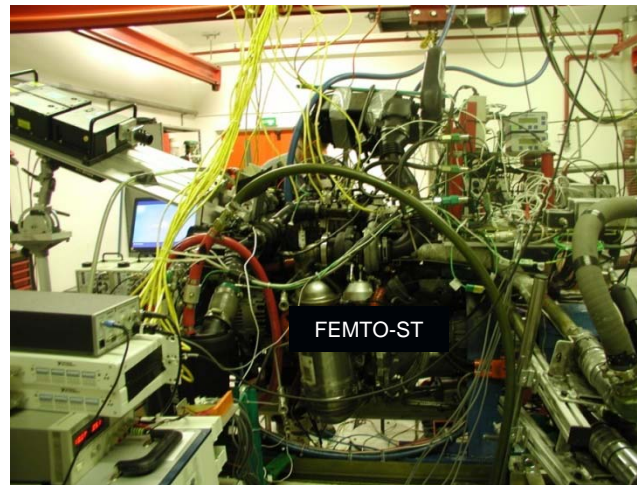
Thin film junction on wires thermocouple

K type wires : diam = 12,7 μm

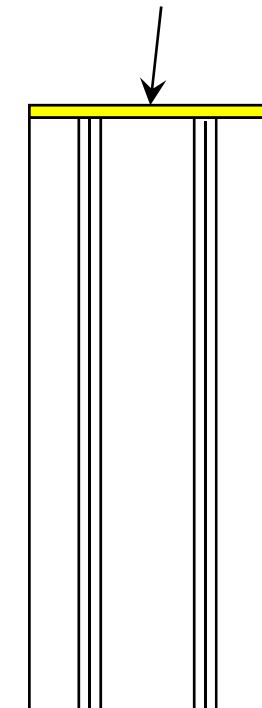
Thin film (hot junction) = gold, tungsten, ...



Tungsten thin film

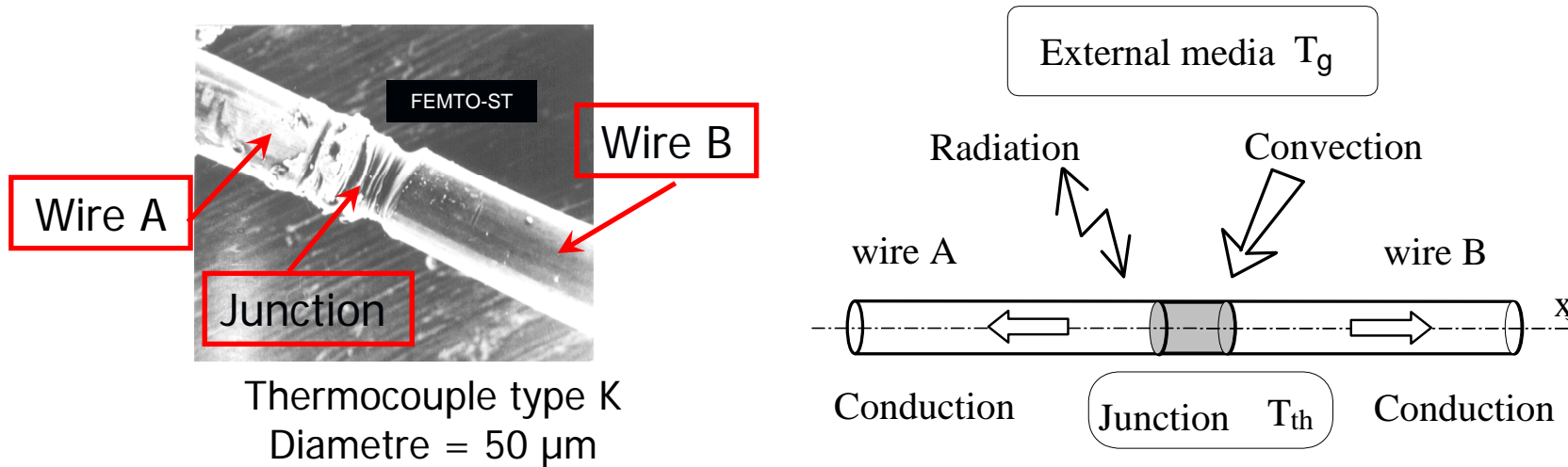


Gold thin film



wires

2 Theoretical model for transient measurements



Heat balance :

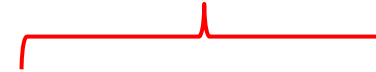
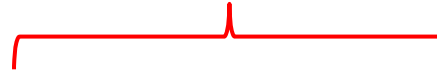
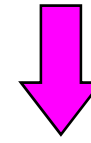
- convection in the boundary layer around the thermocouple
- conduction along the wires
- radiation between the wires and the external medium
- contribution of another source of energy (a laser source in our work)

HEAT BALANCE

Heat accumulated

Convection

Conduction



$$\rho_{th} c_{th} \frac{\pi d^2}{4} \frac{\partial T_{th}}{\partial t} = Nu \lambda_g \pi (T_g - T_{th}) + \lambda_{th} \frac{\pi d^2}{4} \frac{\partial^2 T_{th}}{\partial x^2}$$

$$- \sigma \varepsilon(T_{th}) (T_{th}^4 - T_w^4) \pi d + \sqrt{\frac{2}{\pi}} \frac{(1 - \bar{R})}{a} P_L \operatorname{erf} \left[\frac{d}{a\sqrt{2}} \right] \exp \left[-2 \frac{x^2}{a^2} \right]$$



Radiative heat transfer

External heat flux (laser beam)

Gas temperature measurement $T_g(t)$?

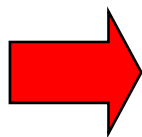
The sensor measures

$$T_g(t) = T_{th}(t) + \tau_{cv}$$

I need to determine

$$\left[\begin{array}{l} \frac{\partial T_{th}}{\partial t} - \frac{\lambda_{th}}{\rho_{th} c_{th}} \frac{\partial^2 T_{th}}{\partial x^2} + \frac{4 \sigma \varepsilon(T_{th})}{\rho_{th} c_{th} d} (T_{th}^4 - T_w^4) \\ - \frac{4}{\rho_{th} c_{th} d^2} \sqrt{\frac{2}{\pi}} \frac{(1-\bar{R})}{a} P_L \operatorname{erf} \left[\frac{d}{a\sqrt{2}} \right] \exp \left[-2 \frac{x^2}{a^2} \right] \end{array} \right]$$

Convection time constant \blacklozenge_{cv} :



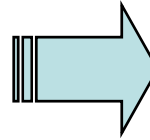
$$\tau_{cv} = \frac{\rho_{th} c_{th} d^2}{4 Nu \lambda_g} = \frac{\rho_{th} c_{th} d}{4 h}$$

Influenced by :

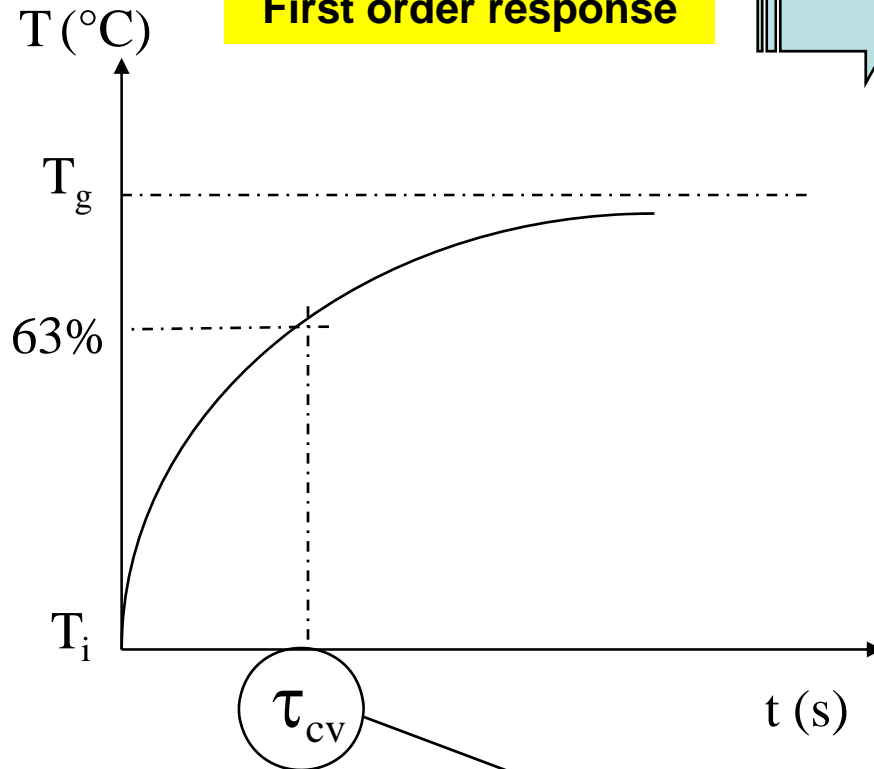
- diameter d
- convection coefficient h

Step unit response (see Tutorial T4)

First order response



Heat balance with convection only !!



$$\rho_{th} c_{th} \frac{\pi d^2}{4} \frac{\partial T_{th}}{\partial t} = Nu \lambda_g \pi (T_g - T_{th})$$

$$T_g = T_{th} + \tau_{cv} \frac{\partial T_{th}}{\partial t}$$

$$\frac{T_g - T_{th}}{T_g - T_i} = \exp\left[-\frac{t}{\tau_{cv}}\right]$$

Time constant (s)

$$\tau_{cv} = \frac{\rho_{th} c_{th} d^2}{4 Nu \lambda_g} = \frac{\rho_{th} c_{th} d}{4 h}$$

Cut-off frequency (Hz)
(Bandwidth)

$$f_c = \frac{1}{2 \pi \tau_{cv}}$$

Global time constant \diamond_g ?

ASTM (1993)

$$\frac{T_g - T_{th}}{T_g - T_i} = K_1 \exp\left[-\frac{t}{\tau_1}\right] - K_2 \exp\left[-\frac{t}{\tau_2}\right] - \dots - K_n \exp\left[-\frac{t}{\tau_n}\right]$$

\diamond_i = time constant of each heat transfer mode

Lanzetta et al. (2001) : thermoelectric anemometry (velocity measurement)

$$\frac{1}{\tau_g} = \frac{1}{\tau_{cv}} + \frac{1}{\tau_{rad}} + \frac{1}{\tau_{Jeff}}$$

\diamond_{cv} = « convection » time constant


\diamond_{rad} = « radiation » time constant

\diamond_{Jeff} = « Joule effect » time constant

**Global “time constant” is not a constant !! =
function of the heat transfer modes : convection, radiation, conduction, etc...**

It is a *characteristic time*

3 Dynamic characterization

Reality is more complex  ~~response = first order~~

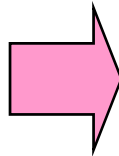
What is the real time constant τ ?

Response : it depends on the application !!

How to determine τ ?

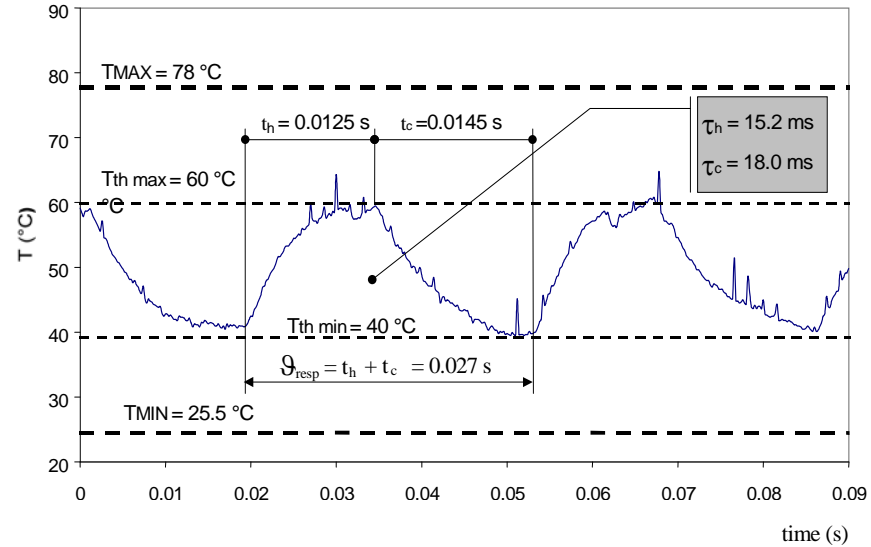
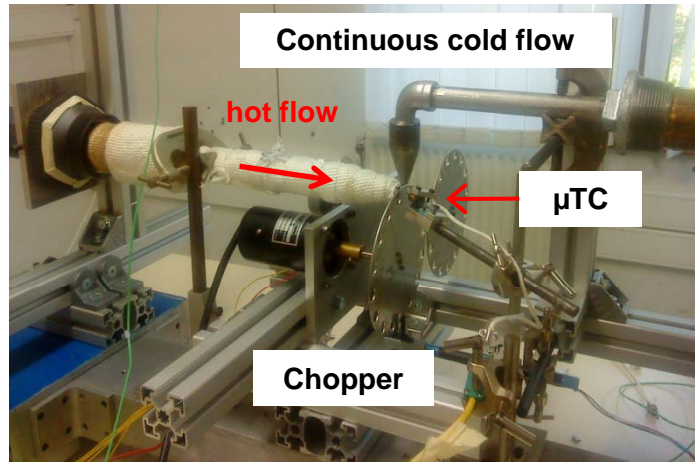
One response : experimental way

Experimental
characterization
of the dynamic
response

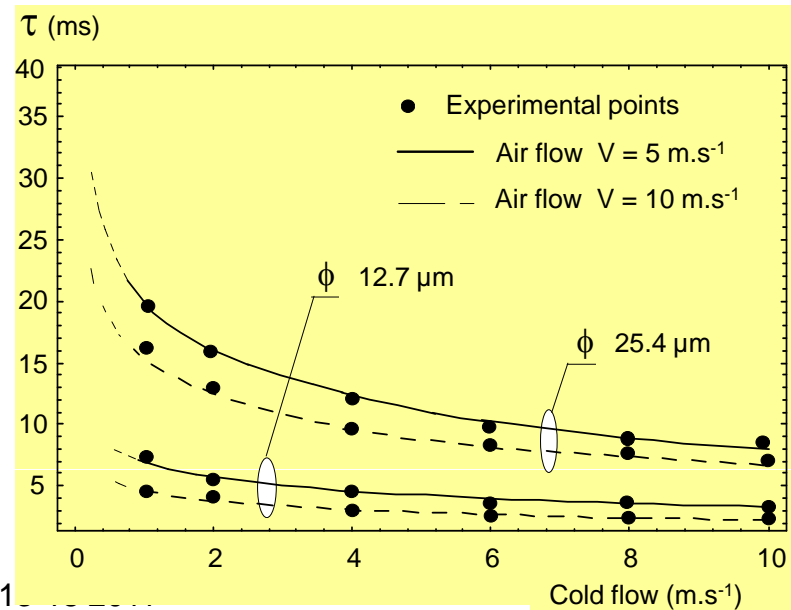


- ① Convective characterization
- ② Radiative characterization
- ③ Shock tube characterization

① Convective calibration

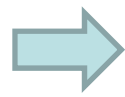


Junction diameter	Air velocity : 13 m.s ⁻¹			Air velocity : 23 m.s ⁻¹	
	d (μm)	τ _{cv} (ms)	Δf (Hz)	τ _{cv} (ms)	Δf (Hz)
S	0.5	—	—	—	—
	1.27	—	—	—	—
	5	2.9	55	2.2	72
K	12.7	15.2	10.5	8.5	18.7
	25	20	8	17	9.4
	250	32	5	25	6.4

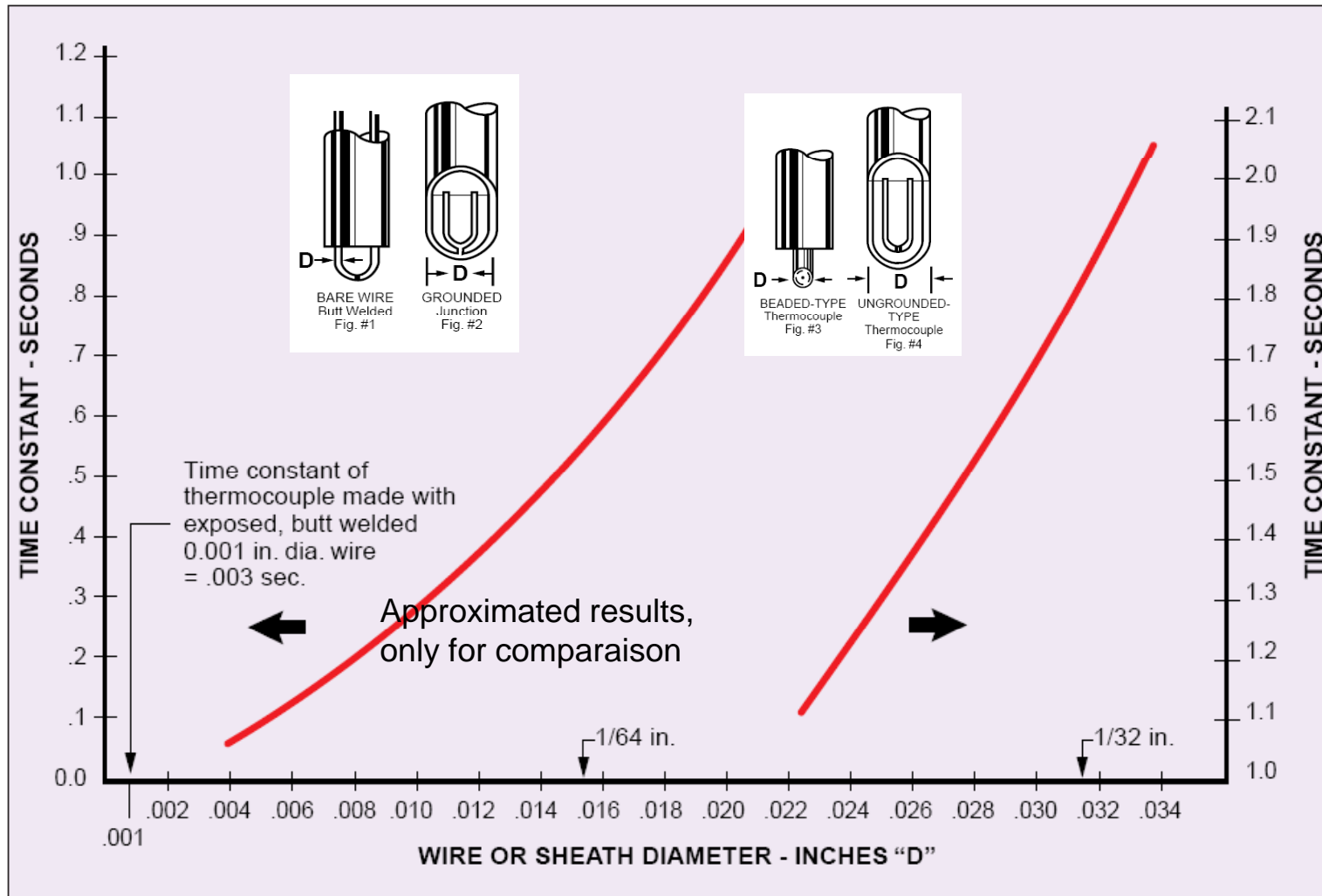


Example from Omega[®]

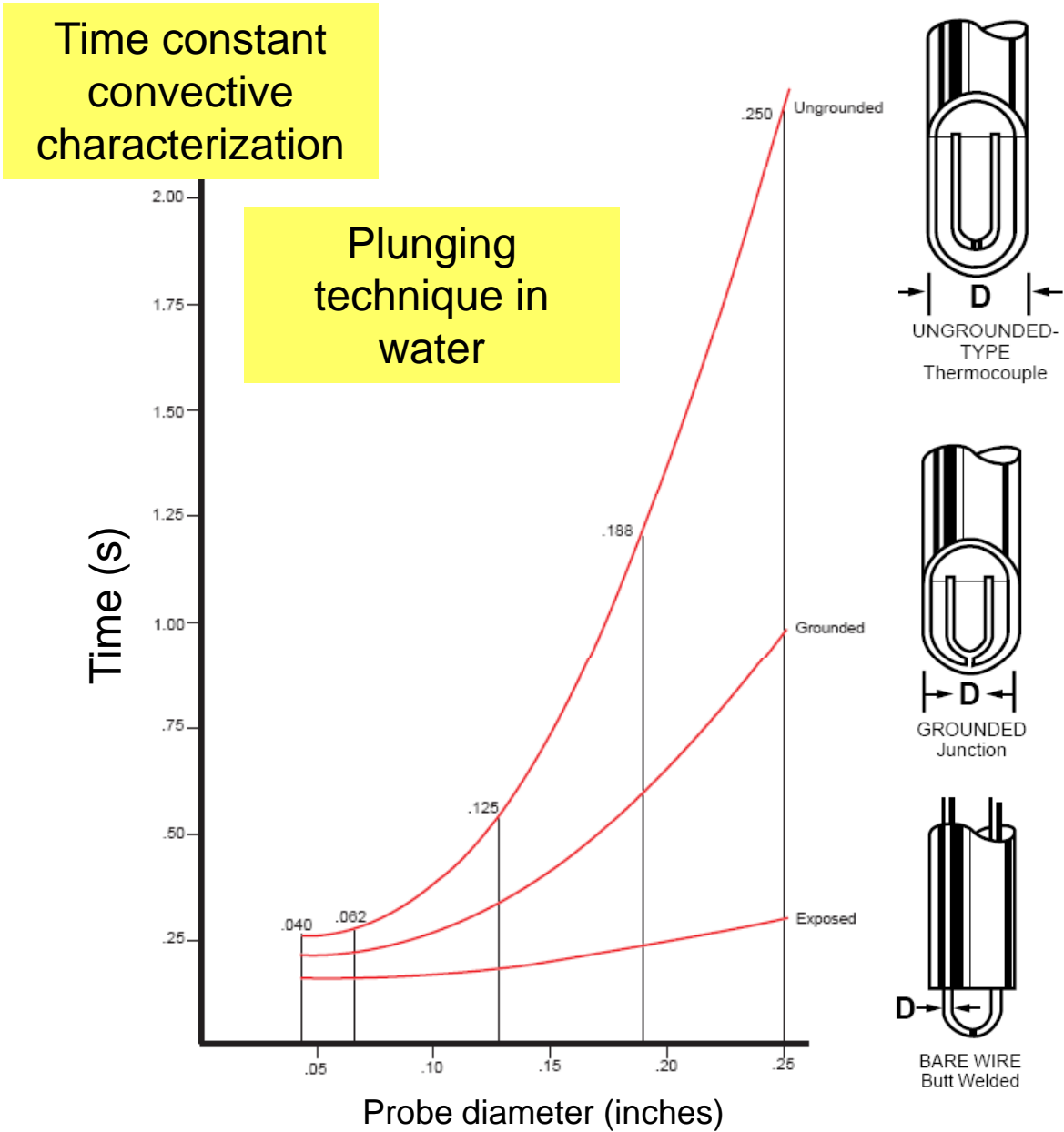
Time constant
convective
characterization



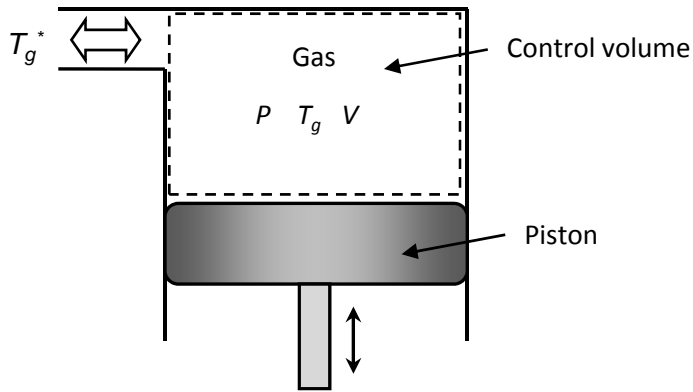
Air flow = 1.8 m.s⁻¹
at room temperature and atmospheric pressure



Example from Omega[©]



Measurements in a heat engine cylinder : heat density $q''(t) = ??$

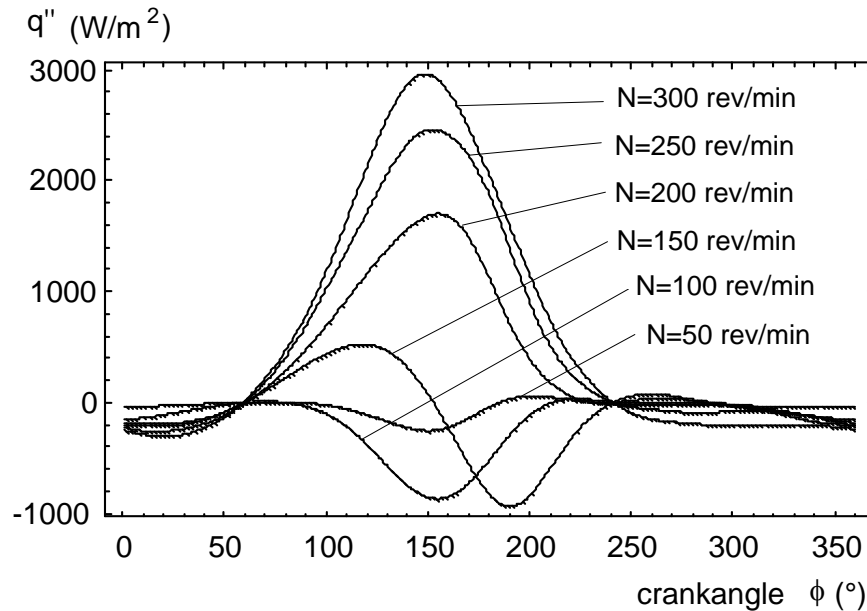
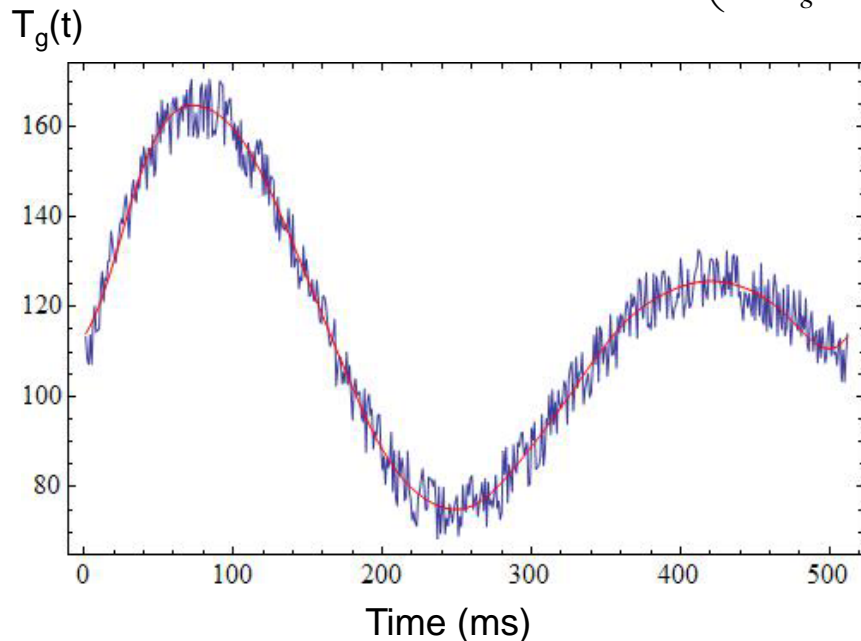


Measurements : $P(t), T_g(t), T_g^*(t)$ and $V(t)$

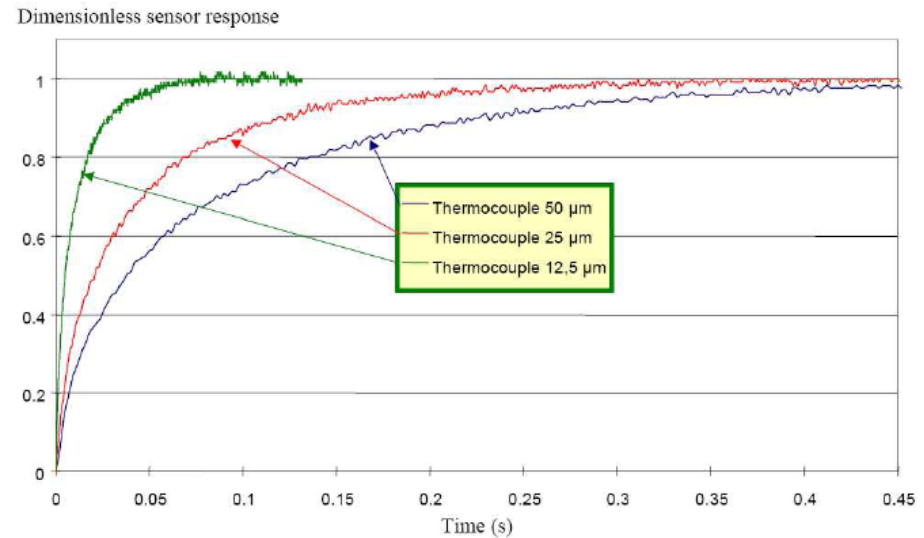
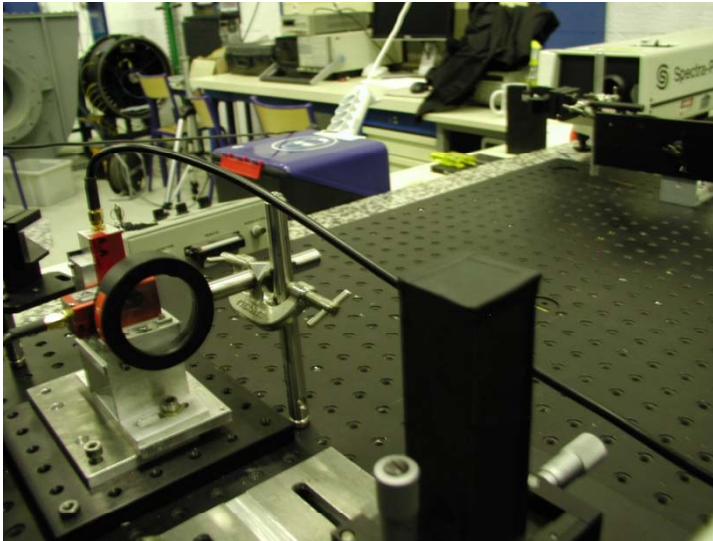
Determination of smoothed values for

$$\frac{dP(t)}{dt} \quad \frac{dV(t)}{dt} \quad \frac{dT_g(t)}{dt}$$

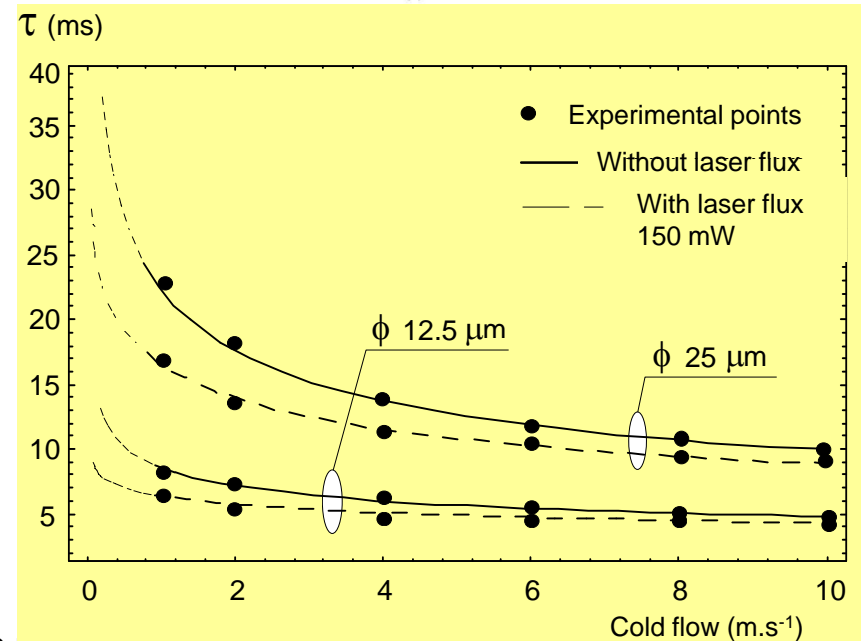
$$\Rightarrow q''(t) = \frac{\gamma}{\gamma - 1} \left(\frac{T_g^* - T_g}{T_g} \right) P dV + \left(\frac{\gamma T_g^* - T_g}{(\gamma - 1) T_g} \right) V dP - \frac{\gamma}{\gamma - 1} \left(\frac{T_g^*}{T_g} \right) P V \frac{dT_g}{T_g}$$



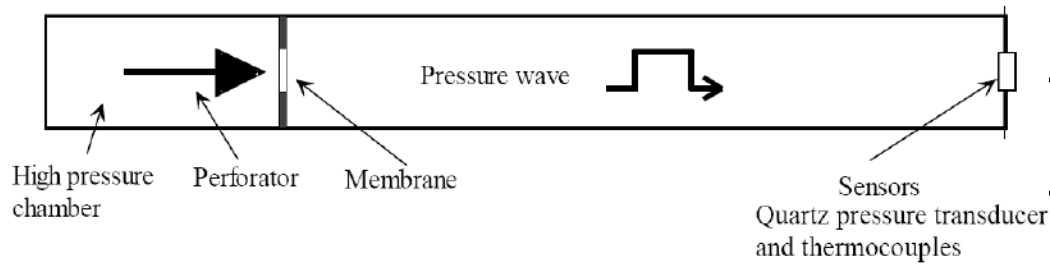
② Radiative calibration



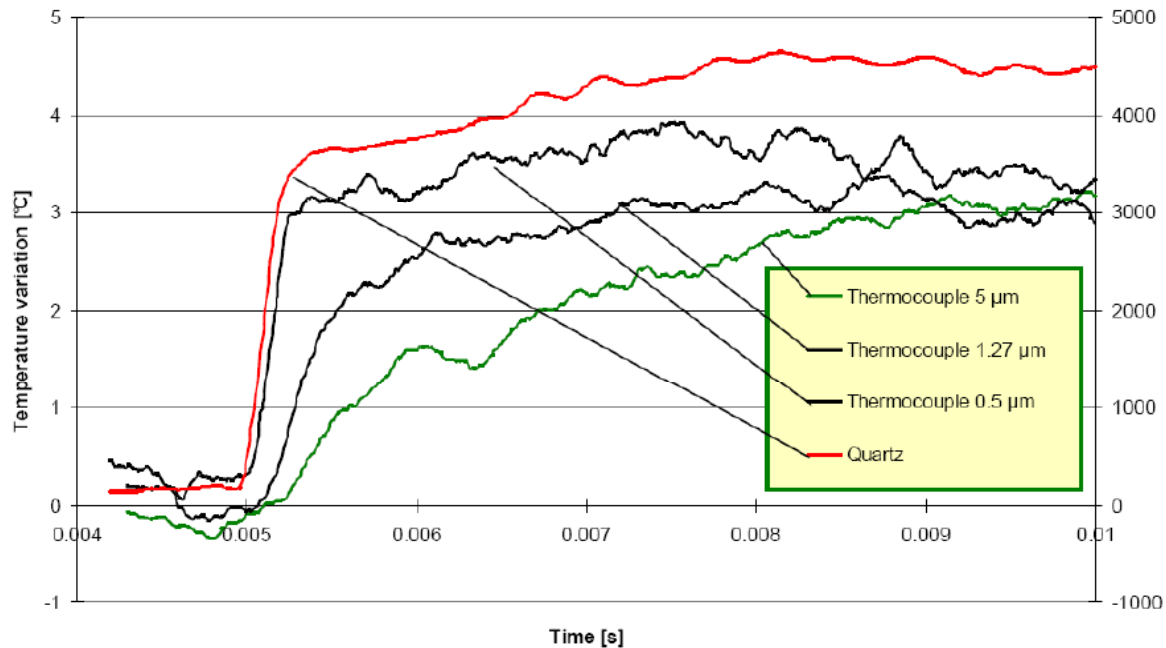
	Junction diameter d (μm)	Radiative time constant τ_{rad} (ms)	Bandwidth Δf (Hz)
S	0.5	0.07	2274
	1.27	0.18	884
	5	1.3	123
K	12.7	8.5	19
	25	34	5
	50	64.5	2.5



③ Shock tube calibration



	Junction diameter	Pseudo-convective time constant	Bandwidth
	d (μm)	τ_{pc} (ms)	Δf (Hz)
S	0.5	0.21	758
	1.27	0.45	354
	5	1.50	106
K	12.7	—	—
	25	—	—
	50	—	—



- And more ?

Thermoelectric anemometry

« Active »
thermocouple

- Heating by Joule effect
- Cooling by the fluid (relaxation)

Simultaneous measurements
temperature/flow (velocity)

Simultaneous measurements
temperature/pressure



3 methods

- Relaxation frequency
- Flying time
- Phase



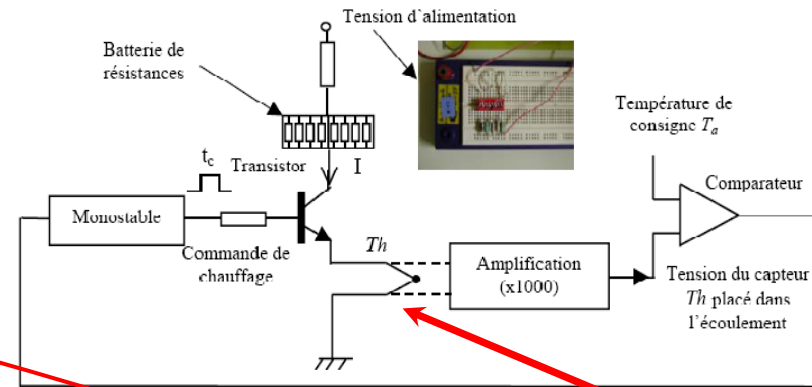
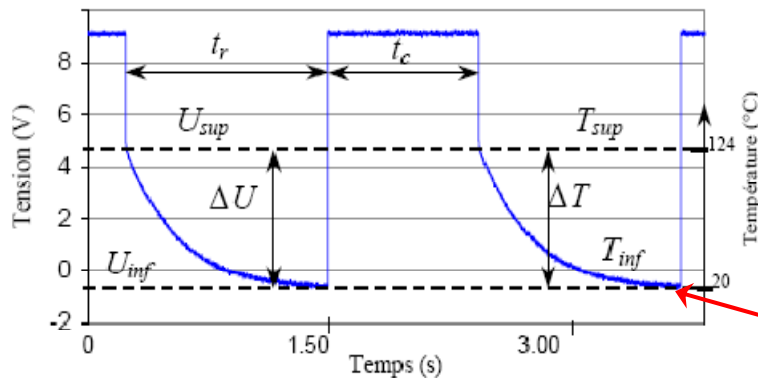
1 method

- Relaxation frequency

1 Relaxation frequency method

Simultaneous measurements
temperature/flow (velocity)

Simultaneous measurements
temperature/pressure



Heating t_c Relaxation t_r

Fixed duration :
Tension,
Resistance

Variable duration :
 $f(\text{state of the fluide}) =$
flow V or pressure P

Oscillation function of
the velocity or the
pressure

$$f = \frac{1}{t_c + t_r}$$

Temperature
measurement at
the end of the
relaxation

Thermocouple Th_1
Type K, $d = 25.4 \mu\text{m}$



Simultaneous measurements temperature/flow (velocity)

Oscillation frequency

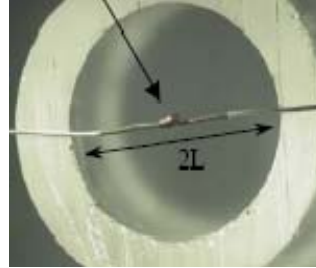
$$f = \frac{1}{2t_h - \tau_g^* \ln\left(\frac{T_{inf} - T_f}{T_{sup} - T_f}\right)}$$

$$\frac{1}{\tau_g^*} = \frac{1}{\tau_{cv}} + \frac{1}{\tau_{rad}}$$

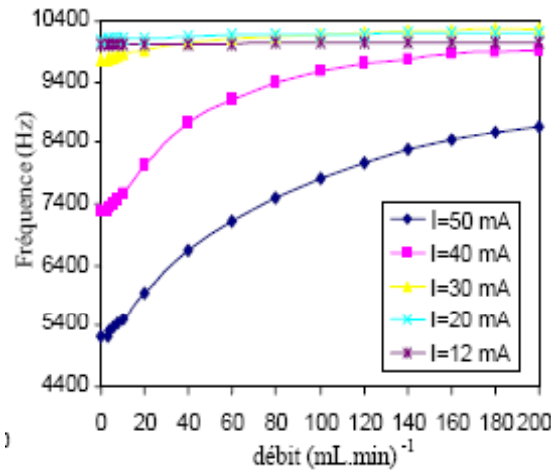
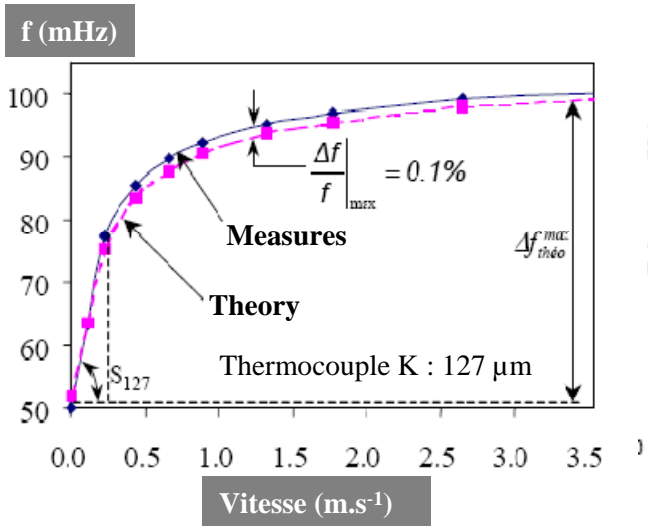
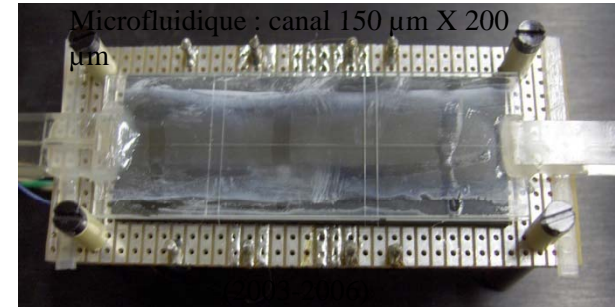
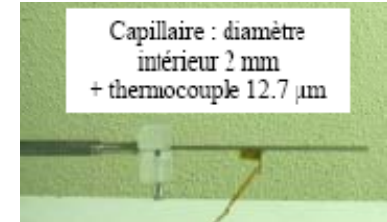
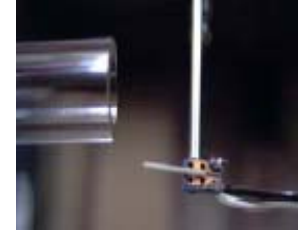
Étalon = débitmètre massique

Velocity V

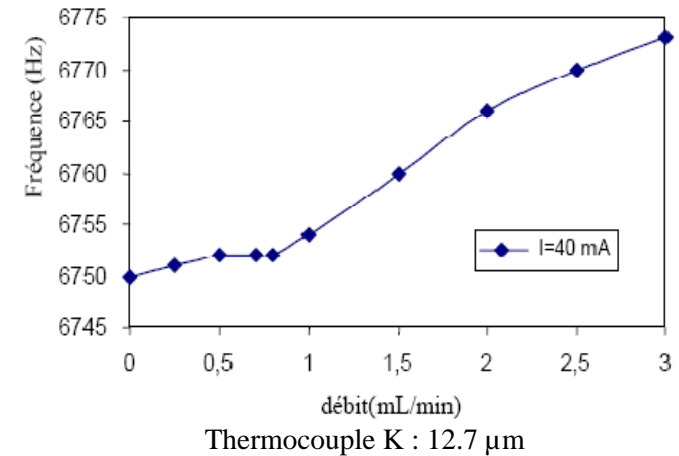
Thermocouple K : 127 μm



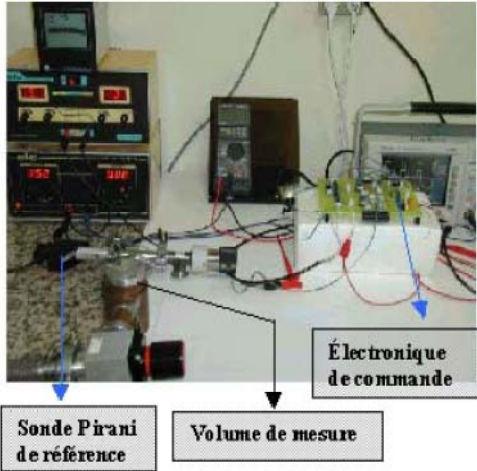
Thermocouple K : 25.4 μm



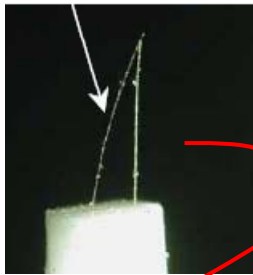
Thermocouple K : 12.7 μm



Simultaneous measurements temperature/pressure



Thermocouple Th_1
Type K, $d = 25.4 \mu\text{m}$



Volume expérimental
(cylindre de 90 cm^3)

Heating

$$\frac{dT}{dt} + (T - T_f) \left(K(P)(T - T_f)^m + \frac{1}{\tau_{rad}} - \frac{1}{\tau_{cl}} \right) - AI^2 = 0$$

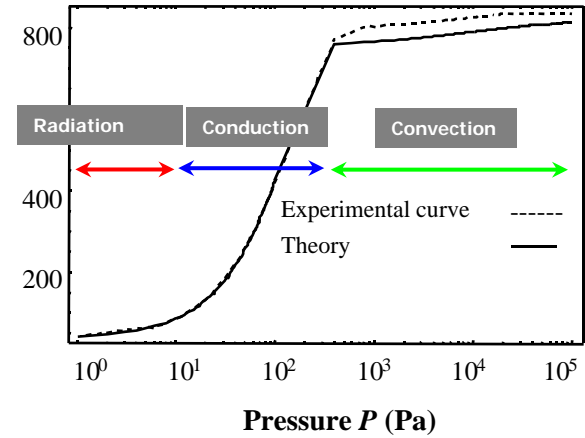
$$K(P) = \frac{4\lambda_f C}{\rho c_p d^2} \left(\frac{g c_{pf} d^3}{T_f^2 \lambda_f \nu_f} P \right)^m \frac{1}{\tau_{cv}} = K(P)(T - T_f)^m$$

Cooling

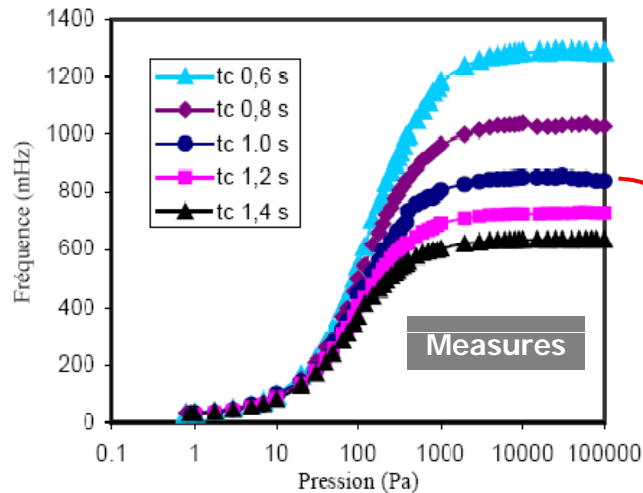
$$\frac{dT}{dt} + (T - T_f) \left(K(P)(T - T_f)^m + \frac{1}{\tau_{rad}} \right) = 0$$

Pressure

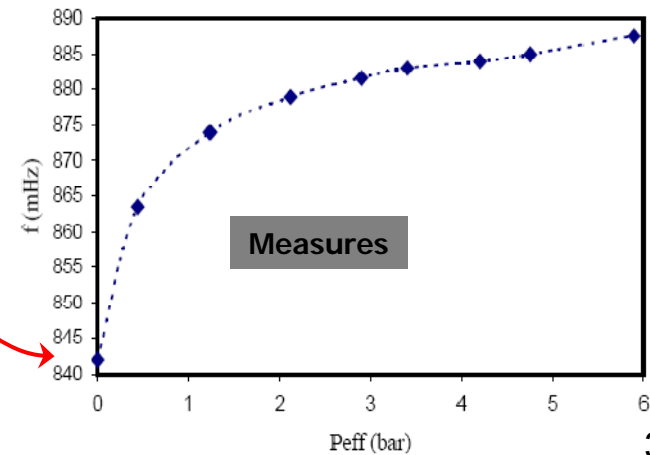
Oscillation frequency f (mHz)



Low pressure (0.8 Pa – 10^5 Pa)



High pressure (10^5 Pa – $5 \cdot 10^5$ Pa)



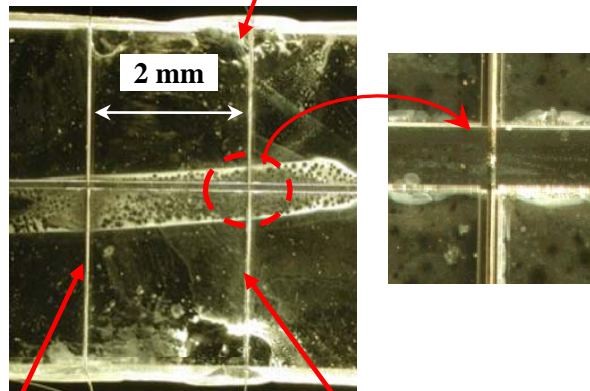
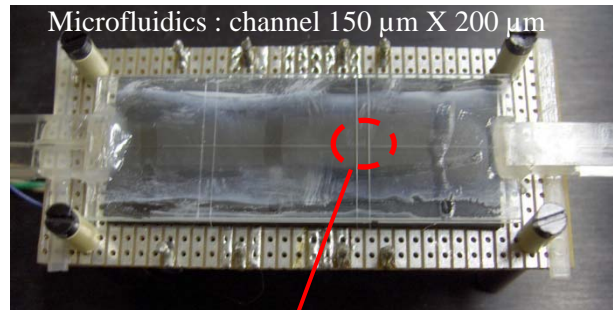
② Flying time method

Simultaneous measurements
temperature/flow (velocity)

Principe

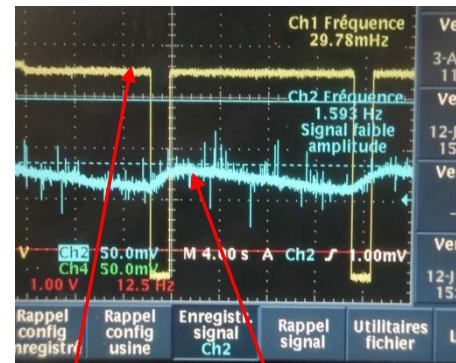
$$\text{Velocity} = \frac{\text{Distance Emission-Reception}}{\text{Duration of the transport phenomena (heat flux in fluid)}}$$

$$V_{\text{mes}} \approx 3 \text{ mm.s}^{-1}$$



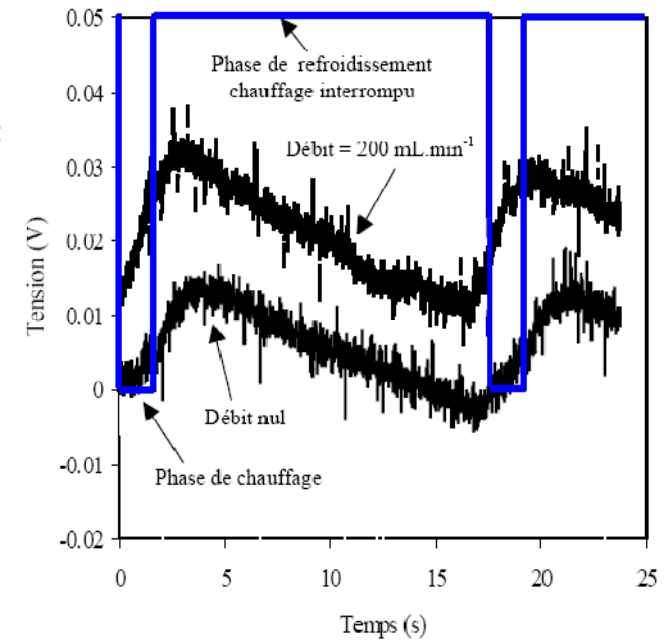
Emission :
Chromel wire
25.4 μm heated by
Joule effect with
step unit response

Reception :
K thermocouple
25.4 μm



Emission

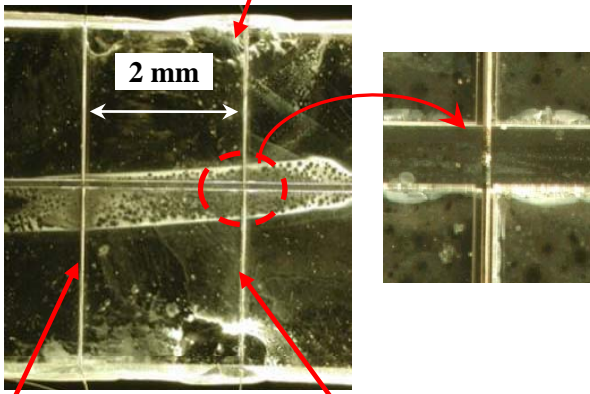
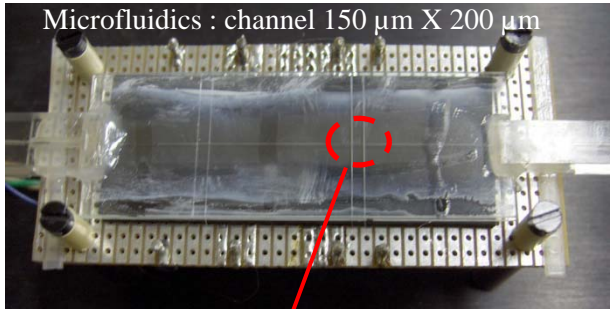
Reception



Prospective work...

3 Phase method

Simultaneous measurements temperature/flow (velocity)



Emission :
Chromel wire
25.4 μm heated by
Joule effect with
sinusoidal signal

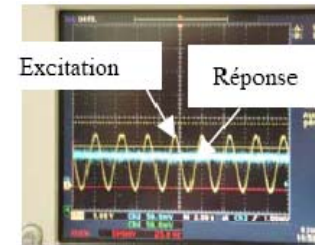
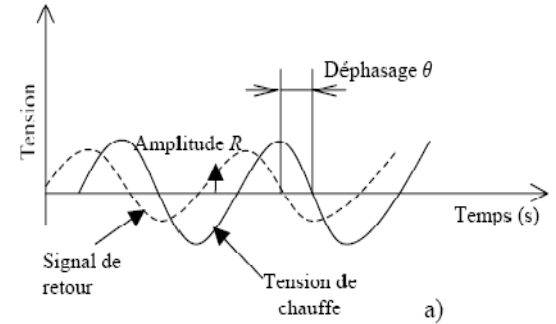
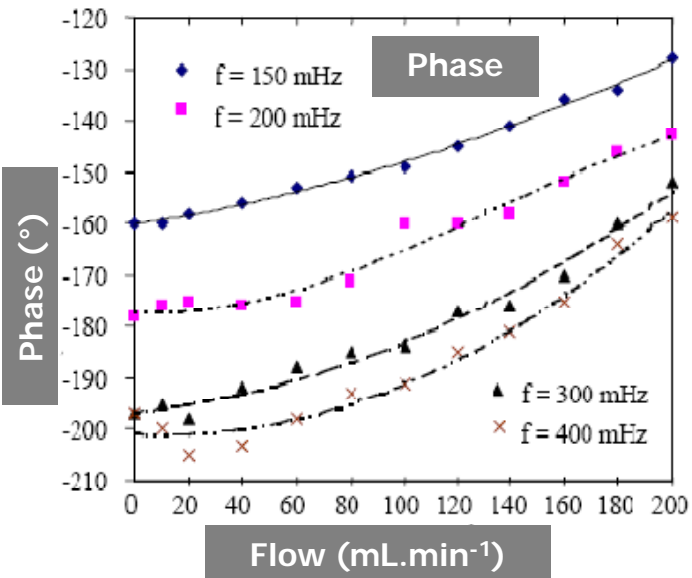
Reception :
K thermocouple
25.4 μm

Method

Emission = periodic heating

Reception = measure of a temperature phase lag

Velocity information is present in the phase !!



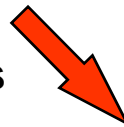
Conclusion

Micronic and sub-micronic thermocouples

- S type : ϕ 0.5, 1.27 and 5.3 μm
- K type : ϕ 7.6, 12.7, 25.4 and 53 μm

Spatial resolution and dynamic response

Problem : robustness



with



dimensions

Applications :

- fluctuations measurements
- photothermal microscopy
- acoustic
- thermal phenomena

} Micro
thermocouples

Lecture 5-A

Part 2 : B. Garnier
**Measurements with contact :
temperature and heat flux**

- Whatever the selected temperature measurement method, one have *parasitic effects*
- Two type of errors
 - ✓ thermometric phenomenon
 - ✓ interaction between sensor, medium and environment which involves a local disturbance of the temperature field.

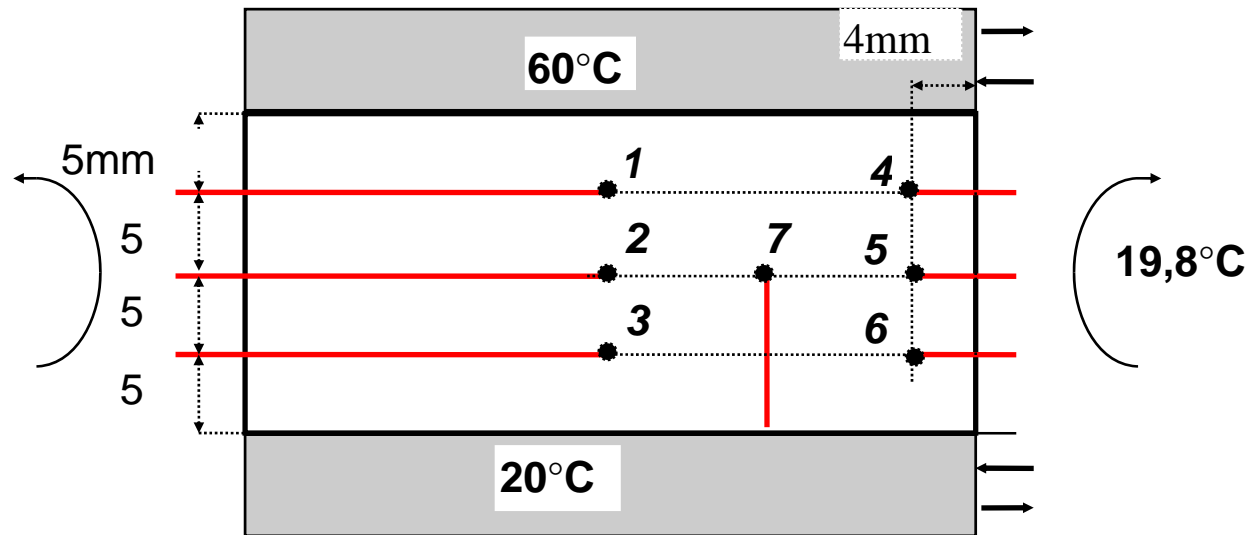


Fig.1 : instrumented PMMA sample with 0.2mm dia. type K thermocouple

Table 3 : steady state temperature measurements

δ^* , mm	#	T, °C	#	T, °C	#	T, °C
5	1	49,9	4	43,5		
10	2	40,5	5	35,4	7	34,8
15	3	31,5	6	27,7		

$$T_7 - T_2 = 5.7^\circ\text{C} !$$

2.4. Error introduced by the disturbance of the local temperature using direct contact temperature measurement

2.4.1. Introduction

2.4.2 Error analysis and model

2.4.2.1 Surface temperature measurement

2.4.2.2 Temperature measurement within a volume

2.4.2.3 Error model

2.4.3. Practical consequence and examples, semi intrinsic thermocouples

2.4.3.1. Practical consequences

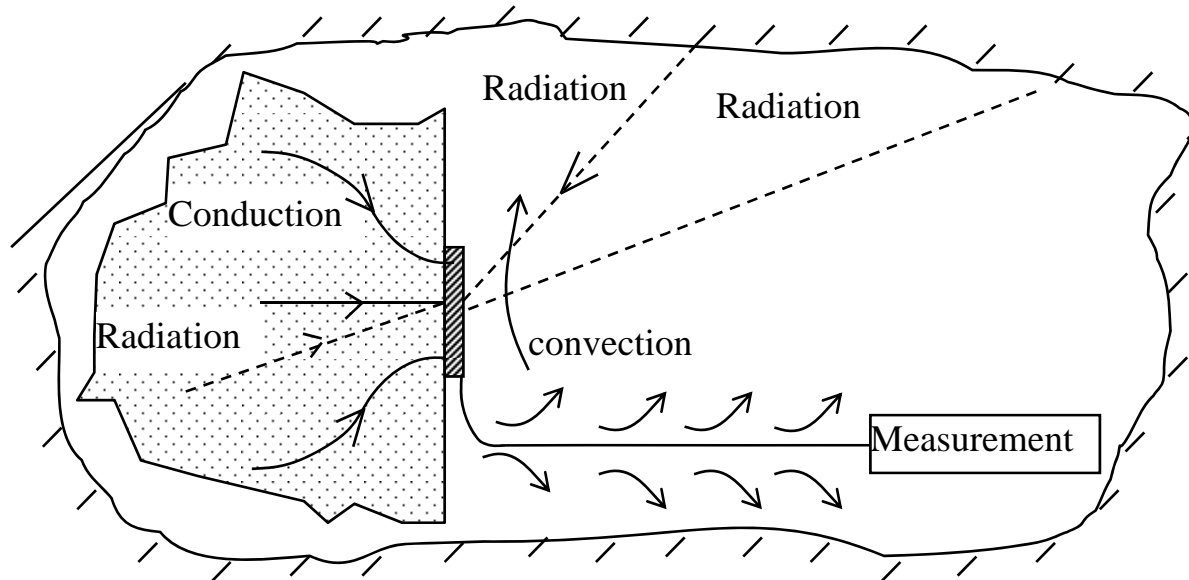
2.4.3.2. Application for a thermocouple with and without a contact disc

2.4.3.3. Temperature measurement with semi intrinsic thermocouple

2.5. Heat flux measurement: direct methods

2.4.2.1 Surface temperature measurement

Bardon 1999, Cassagne 1980 & 1986



For an opaque medium:

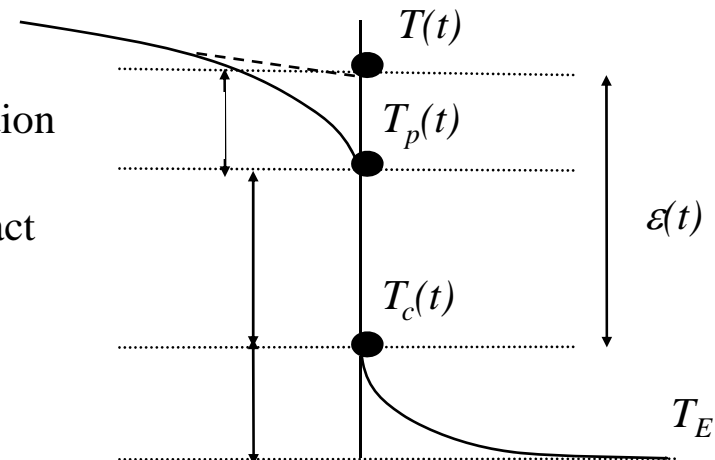
3 effects

- Macroconstriction
- Thermal contact resistance

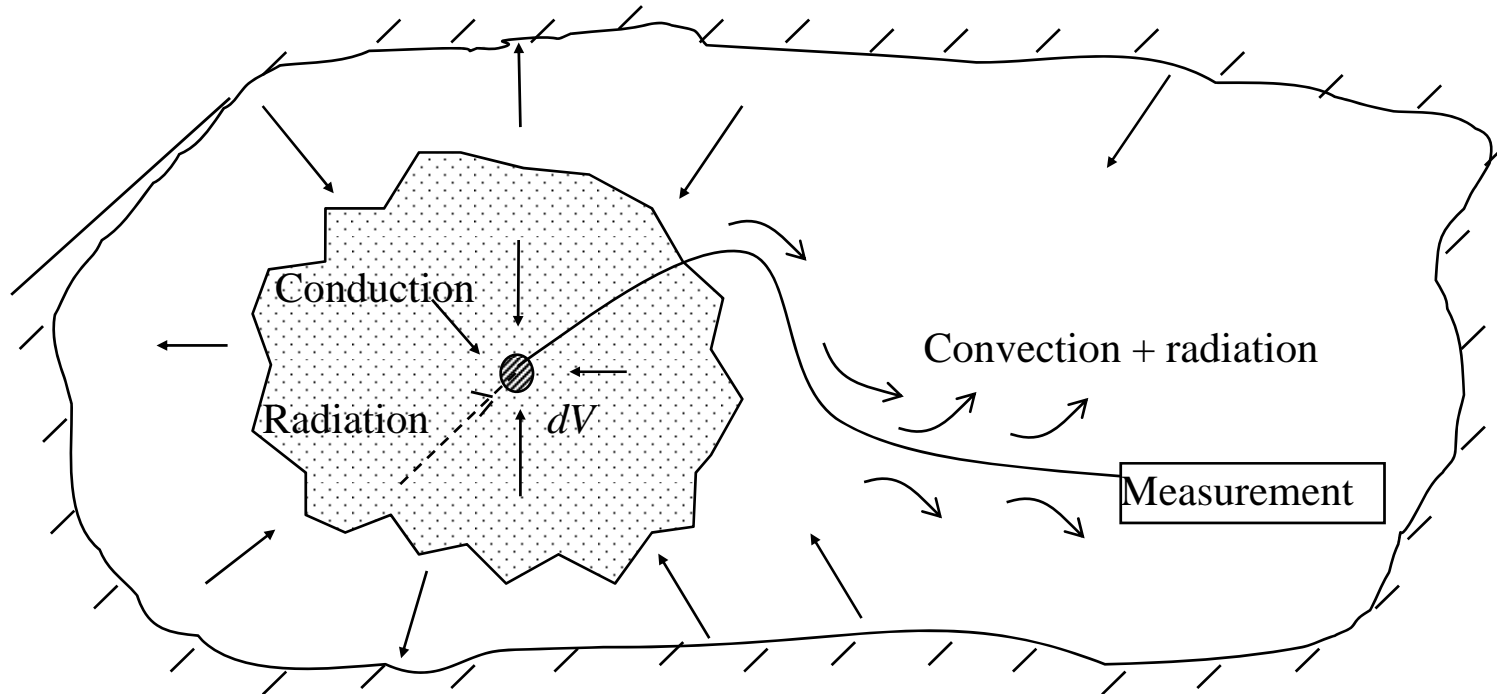
→ Measurement error :

$$\varepsilon(t) = T^{\text{Fin}}(t) - T_c(t)$$

Metti⁵ Roscoff June 13-18 2011



2.4.2.2 Temperature measurement within a volume

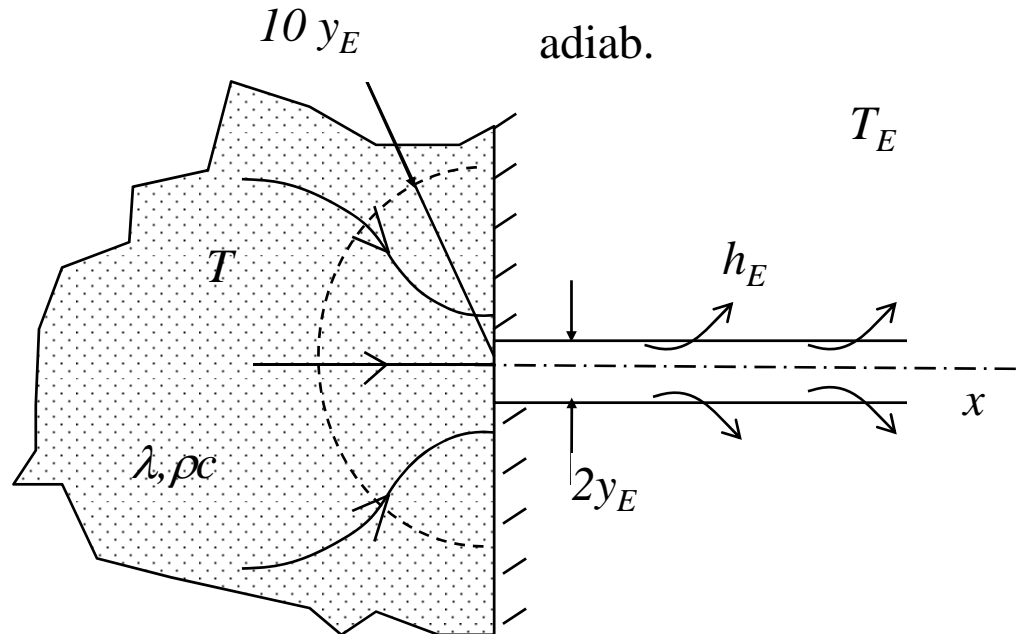


- Same 3 effects:
- Macroconstriction
 - Thermal contact resistance
 - Fin

→ Measurement error : $\varepsilon(t) = T(t) - T_c(t)$

2.4.2.3 Error model

- Steady state surface temperature measurement of an opaque medium



$$h_E = h_c + h_r$$

$$T_E = \frac{h_c T_f + h_r T_o + F}{h_E}$$

λ : thermal conductivity

a) Macroconstriction effect

:

$$T - T_p = r_M \frac{\phi}{\lambda}$$

with $r_M = \frac{1}{4y_E \lambda}$

for a disc of radius y_E

→ 96% of the $T - T_p$ temperature drop is within an hemisphere of center

0 and radius $10 y_E$
Metti⁵ Roscoff June 13-18 2011

b) The contact resistance effect

$$T_p - T_c = r_c \phi$$

$$r_c = R_c / S$$

$$R_c \text{ (m}^2 \text{ K W}^{-1} \text{)}$$

c) The fin effect:

$$T_c - T_E = r_E \phi$$

thermocouple assumed as a rod of radius y_E

$$r_E = 1 / (\pi y_E \sqrt{2h_E \lambda_E y_E})$$

Measurement error $\varepsilon = T - T_c$?

$$T - T_p = r_M \phi$$

$$T_p - T_c = r_c \phi$$

$$T_c - T_E = r_E \phi$$

$$T - T_c = (r_M + r_c) \phi$$

$$\phi = \frac{T - T_E}{r_M + r_c + r_E}$$

$$\varepsilon = T - T_c = K (T - T_E) \text{ with}$$

$$K = \frac{1}{1 + \frac{r_E}{r_c + r_M}}$$

$$\varepsilon = T - T_c = K (T - T_E)$$

with

$$K = \frac{l}{1 + \frac{r_E}{r_c + r_M}}$$

Discussion:

- ε small if: {
- $T - T_E$ small
 - K small

$$r_E \gg r_c + r_M$$

$$r_M = \frac{1}{4y_E \lambda}$$

✓ high thermal conductivity medium

$$r_M \ll r_c$$

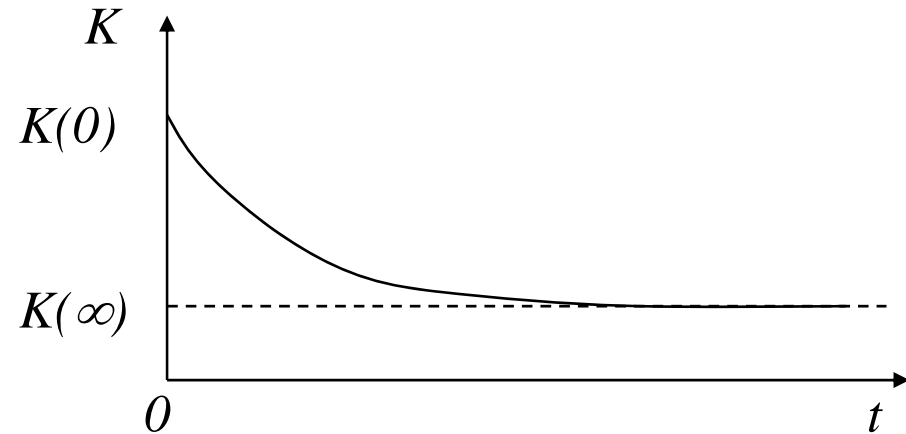
✓ low thermal conductivity medium

$$r_M \gg r_c$$

Transient surface temperature measurement

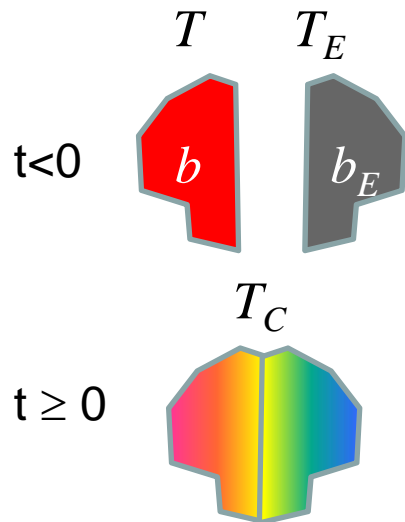
and

$$\varepsilon(t) = K(t) [T(t) - T_E]$$



$K(0)$?

- If $r_c \neq 0$, $K(0)=1$, the error is about 100% at $t=0$
- If $r_c = 0$ (perfect contact), the initial error is smaller:



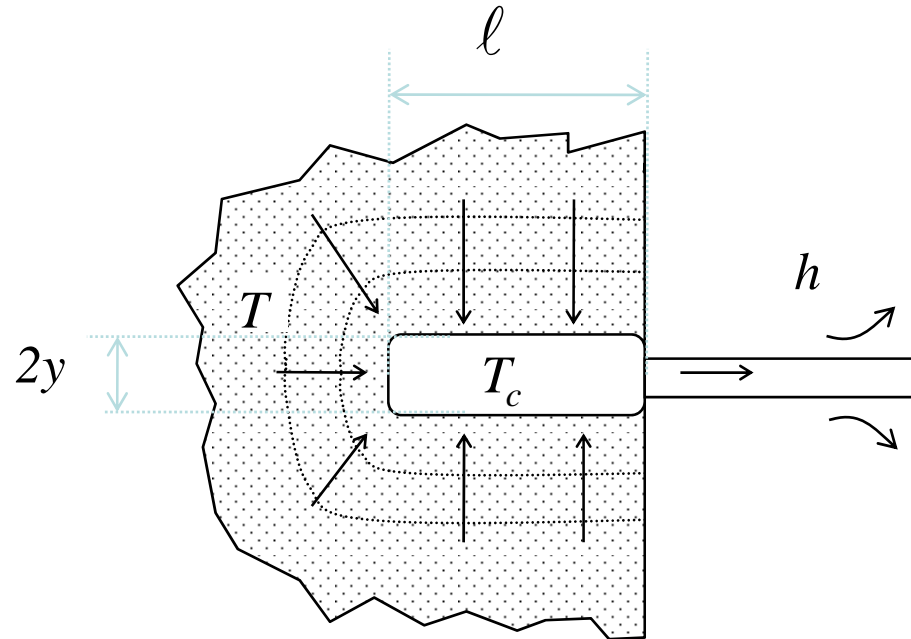
$$\frac{T - T_C}{T_C - T_E} = \frac{b_E}{b} \quad \longrightarrow \quad \varepsilon(0) = T - T_C = \frac{b_E}{b} [(T_C - T) + (T - T_E)]$$

$$\varepsilon(0) = T - T_C = \frac{b_E}{b + b_E} (T - T_E) \quad \longrightarrow \quad K(0) = \frac{b_E}{b + b_E} < 1$$

$$b = \sqrt{\lambda \rho c} \quad b_E = \sqrt{\lambda_E \rho_E c_E}$$

effusivities

Temperature measurement within a volume



Temperature measurement with a cylindrical sensor inside the medium

- $r_c = R_c / S$ $S = 2\pi y l$

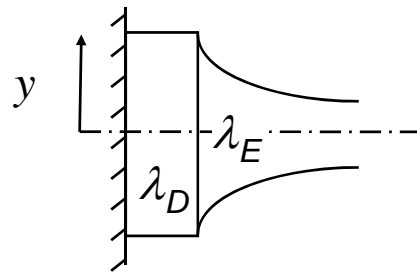
Same error model but with :

- $r_M = \frac{1}{2\pi\lambda l} \text{Log} \frac{2l}{y}$ $l \gg y$

2.4.3. Practical consequence and examples, semi intrinsic thermocouples

• Practical consequences :

1. even for perfect contact $r_c = 0$ there is an error which depends on the ratio r_M/r_E .
2. For high thermal conductivity material, $r_M \ll r_c$. Thus, one must take care that r_c is small and remains stable. The contact pressure will have to be high and constant, surface will have to be plane without waviness, the interstitial medium with the highest possible thermal conductivity (welding, grease...). In addition, one should avoid oxide films as well as mechanical shocks and vibrations which can modify considerably r_c and consequently the measurement error.
3. For low thermal conductivity material, $r_M \gg \gg r_c$. One can reduce macrostriction effect by increasing the radius of the sensitive element without increasing the section of the connections. A contact disc of high thermal conductivity material will be used.



4. Whatever the type of measurement, the fin thermal resistance r_E should be as high as possible. The transversal area, the conductivity, the heat transfer coefficient have to be chosen the smallest possible. One also should have low emissivity surface, connection protected from high temperature fluids movements or radiation, T_E being modified in those situations.
5. Finally, the error is all the more small as T_E should be as close as possible to the temperature T to measure . At the price of a technological complication, one can add an external heat source on the connection so that its temperature T_E is controlled in order to stay as close as possible as T “**compensated heat flux sensors**”. However for correct measurement, the thermal resistance r_E should stay high in order to prevent the compensation heating from disturbing the temperature field in the medium.

• **Application -for steady state temperature measurement** using a thermocouple with and without a contact disc

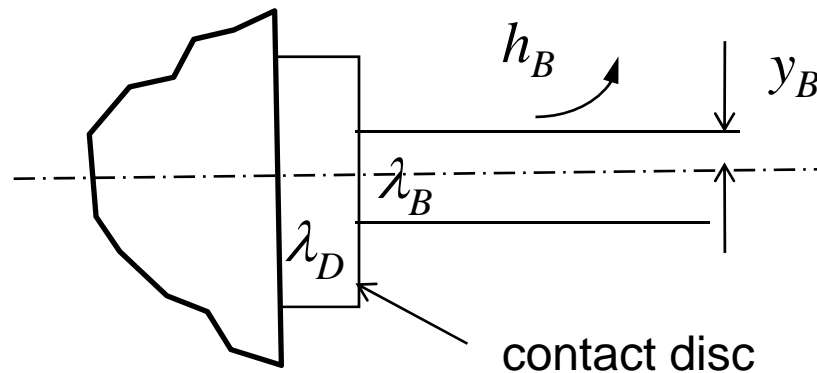
- thermocouple \rightarrow unique rod with a radius $y_B = 0.5$ mm, an infinite length, $\lambda_B = 15$ W.m⁻¹.K⁻¹ and $h_B = 5$ W.m⁻²K⁻¹.

- r_E ?

✓ $r_E = r_B$ without contact disc,

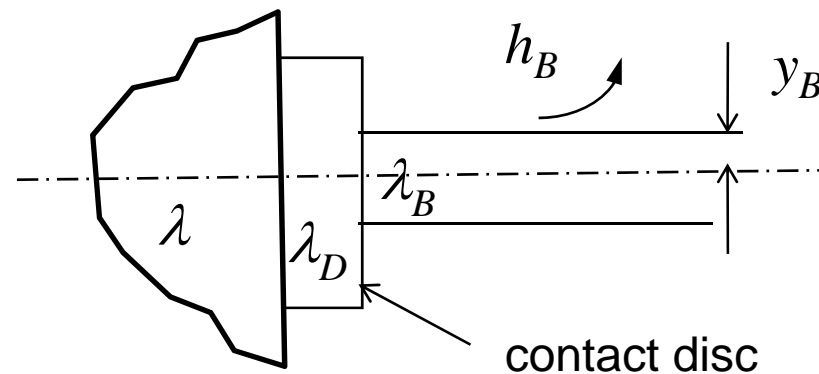
$$r_B = \frac{l}{\pi y_B \sqrt{2h_B y_B \lambda_B}}$$

✓ $r_E \approx r_B + \frac{l}{4y_B \lambda_D}$ with contact disc



Tab 1. Effect of the thermal conductivities of the medium and of the disc on r_M , r_c , r_E and K

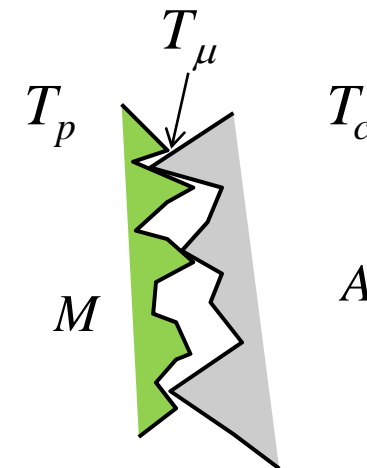
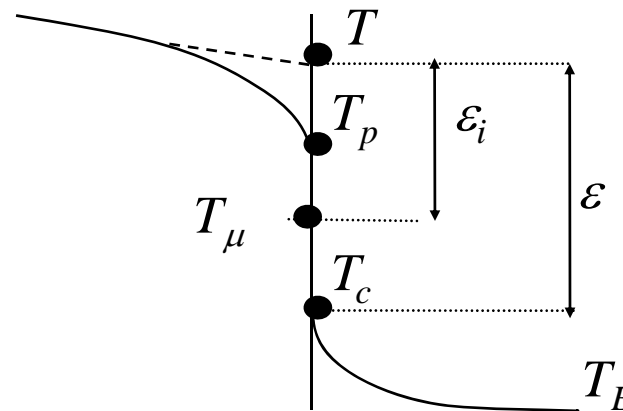
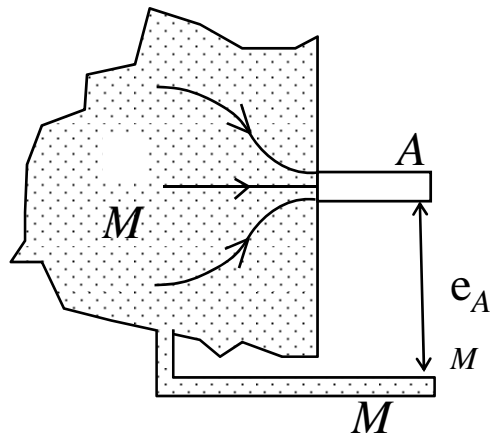
	Low thermal conductivity $\lambda=10^{-1} \text{ W.m}^{-1}.\text{K}^{-1}$		High thermal conductivity $\lambda=100 \text{ W.m}^{-1}.\text{K}^{-1}$	
	without disc	with disc	without disc	with disc
$r_M (\text{K.W}^{-1})$	5000	250	5	0.25
$R_c (\text{K.W}^{-1}\text{m}^2)$	10^{-3}	10^{-3}	10^{-4}	10^{-4}
$r_c (\text{K.W}^{-1})$	1270	3,18	125	0.31
$r_E (\text{K.W}^{-1})$	1700	1733	1700	1733
K	0.786	0.127	0.072	0.0003



- **Temperature measurement with semi intrinsic thermocouple**

Medium M itself (presumably electrically conducting) is used as one wire of the thermocouple

- ✓ it has only one connection wire instead of two, thus r_E is twice larger
- ✓ the measured temperature T_μ is intermediate between T_p and T_c



Semi intrinsic thermocouple $\varepsilon_i = T - T_\mu = K_i(T - T_E)$

$$\frac{T_p - T_\mu}{T_\mu - T_c} = \frac{\lambda_A}{\lambda_M}$$

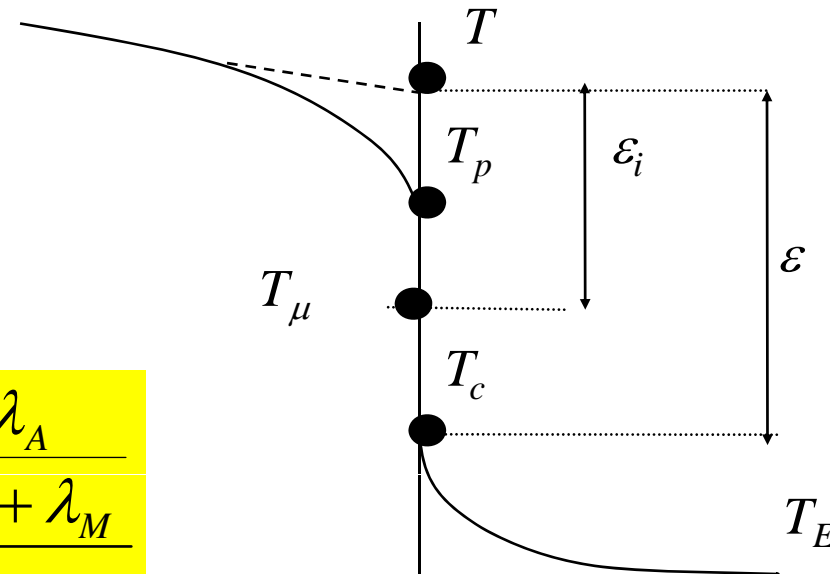
Semi intrinsic

$$K_i = \frac{r_M + r_c \frac{\lambda_A}{\lambda_A + \lambda_M}}{r_M + r_c + r_E}$$

Traditional

$$K = \frac{r_M + r_c}{r_M + r_c + r_E}$$

$$K_i < K$$



Semi intrinsic thermocouple :

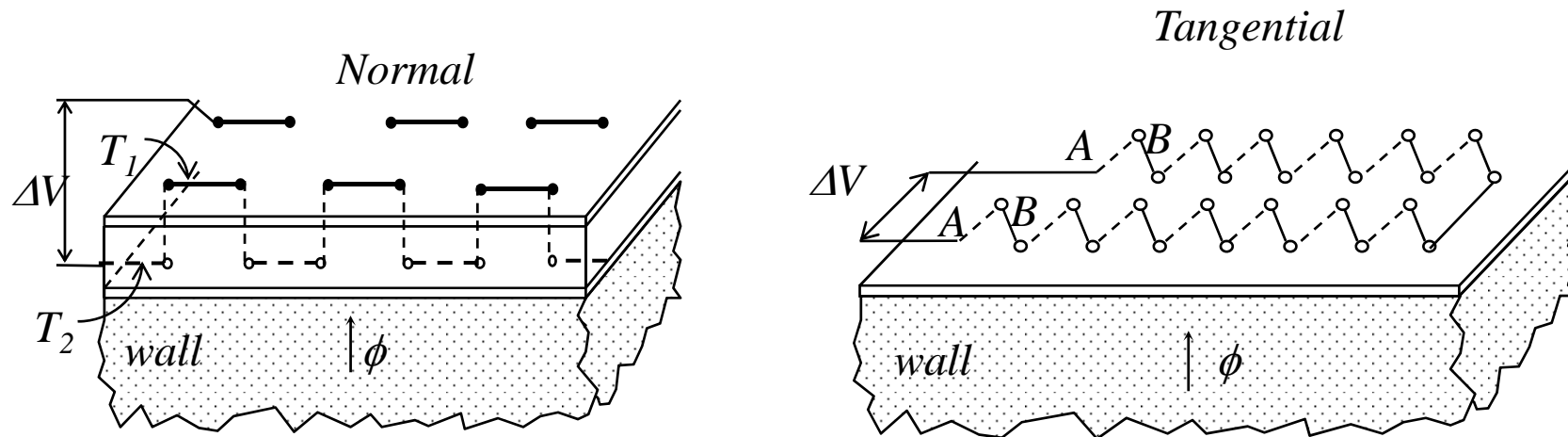
- Error is considerably lower than with a traditional thermocouple (2 to 5 times)
- In transient mode, error and thermal inertia are greatly reduced (Cassagne 1986).
- Calibration of the semi intrinsic thermocouple is almost always required.

2.5. Heat flux measurement: direct and indirect methods

2.5.1. Heat flux sensor with gradient

Principles :

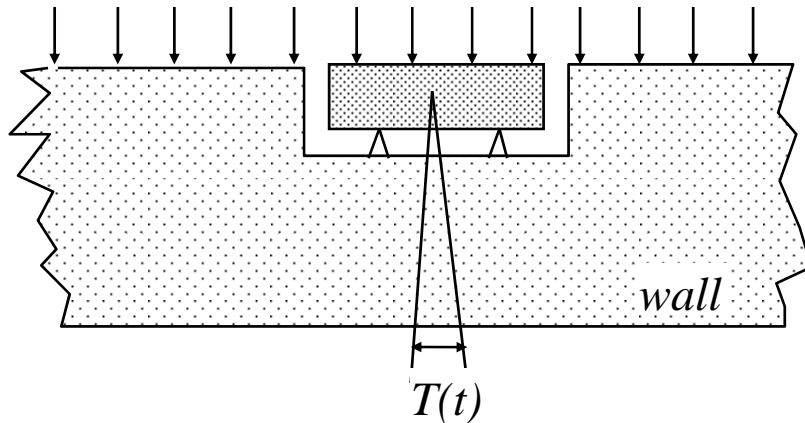
measurement of the temperature difference within the wall itself (intrinsic method) or by covering it with an additional wall (heat flux sensor-HFS-)+ Fourier's law



→ work whatever the heat flux direction with steady state or for slowly variable temperature.

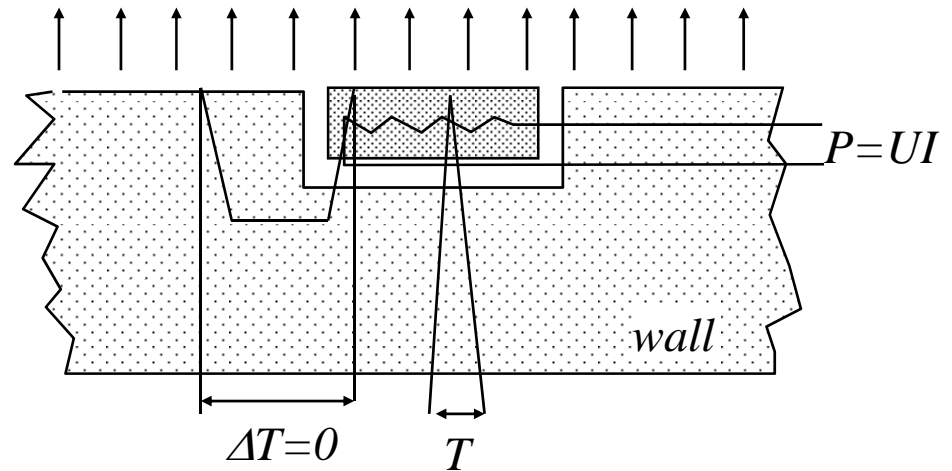
Normal gradient : $\varepsilon \approx 8 \%$ Khaled 2009

2.5.2. Inertia heat flux sensor and heat flux sensor with electric dissipation (zero method)



Inertia heat flux sensor

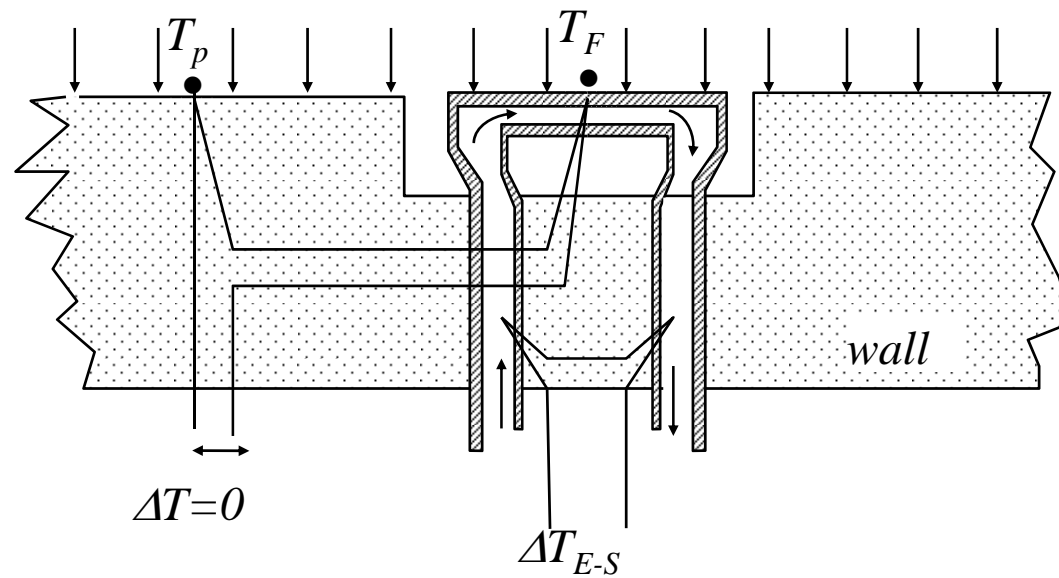
works for heat flux coming from the environment



heat flux sensor with electric dissipation

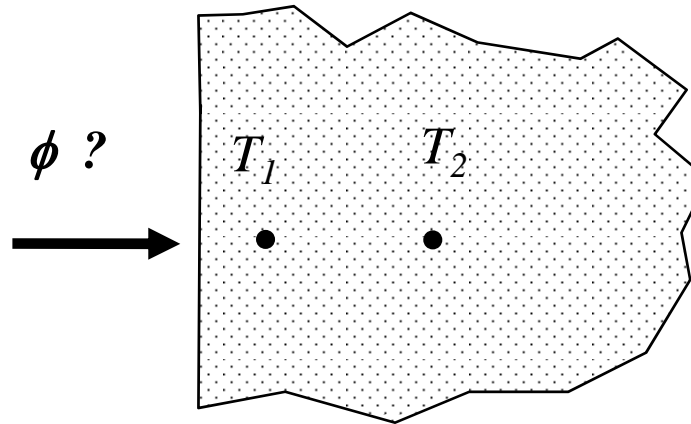
works only for heat flux leaving the wall and for steady state or slowly variable temperature.

2.5.3. Enthalpic heat flux sensor



works for heat flux coming from the environment

2.5.2. Indirect measurement (inverse method)

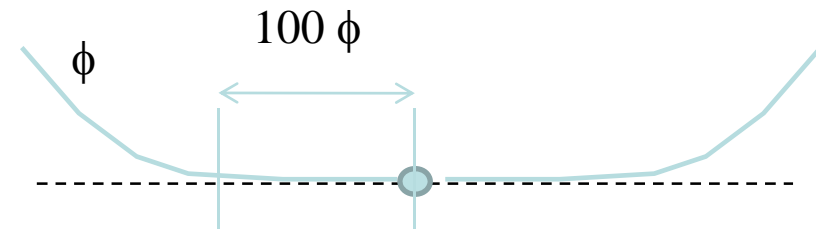


- Transient temperature measurement with embedded thermocouples
- Heat transfer model + inverse methods
- criteria for correct locations of thermocouples (→ Tutorial 4)

$\varepsilon \approx 2\%$ (th K 50 μm) LTN

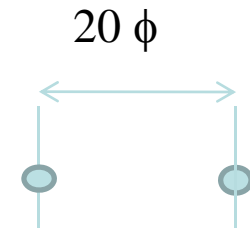
Conclusion

- ✓ Thermocouples should be mounted along isothermal lines (100ϕ)



- ✓ Thermocouples disturbance \rightarrow hemisphere of radius 10ϕ

\rightarrow Thermocouples should not be too close



- ✓ Error model

$$\varepsilon = \varepsilon (r_M, r_c, r_E, T - T_E)$$

- ✓ Semi intrinsic thermocouples \rightarrow low inertia, reduced errors

Thank you for your attention....